Module BIW-MA-AC-O-02: CONTINUUM MECHANICS, TENSOR CALCULUS

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Prerequisite Knowledge

Basic knowledge in the fields of linear algebra and multidimensional analysis as well as knowledge of engineering mechanics, especially in the fields of linear elasticity theory and strength of materials theory at the bachelor's level are required.

Literature

A. Bertram – Elasticity and Plasticity of Large Deformations, Springer-Verlag
G.A. Holzapfel – Nonlinear Solid Mechanics, John Wiley & Sons, Inc.
P. Wriggers – Nonlinear Finite Element Methods, Springer-Verlag

Project and Master Thesis

Please contact the Institute of Mechanics and Shell Structures for possible topics.