





# Modelling the Economic Viability of Grid Expansion, Energy Storage, and Demand Side Management Using Real Options and Welfare Analysis

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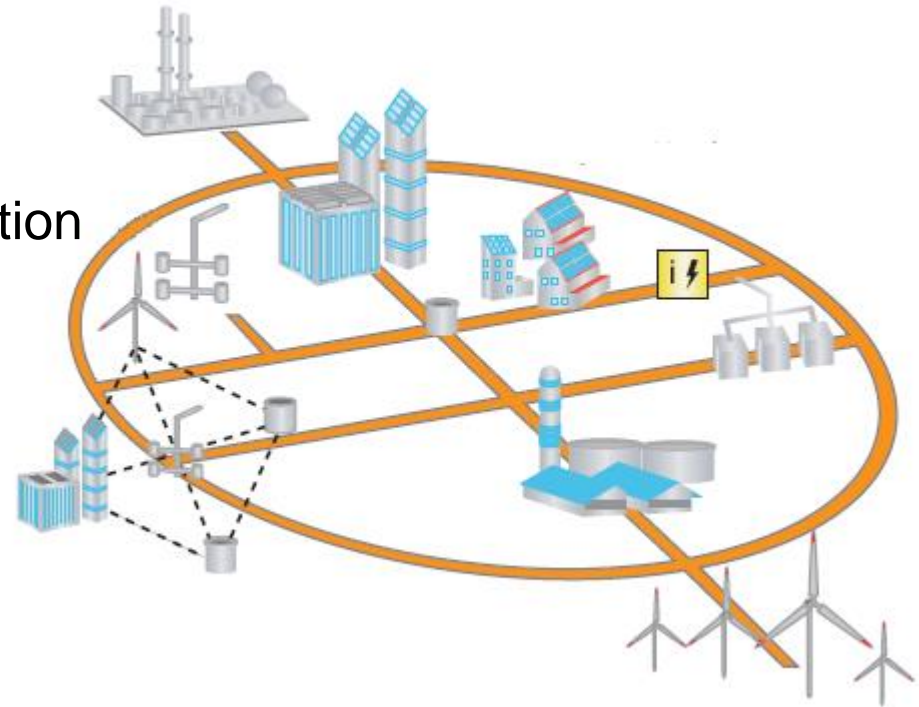


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# Structure of the presentation

1. Fundamentals
2. Market characteristics & Motivation
3. Model specifics
4. Simulation results
5. Conclusion & Summary



Source: elektroniknet.de

# 1. Fundamentals – Cost benefit analysis

Cost benefit analysis uses a one-dimensional decision variable

$$NPV = \sum_{t=0}^T \frac{E(B_t) - E(C_t)}{(1 + r)^t}$$

*NPV*: Discounted difference between the present values of its benefits and costs

where:

$r$  : Market-specific discount rate

$B_t$  : Benefits in time period  $t$

$C_t$  : Costs in time period  $t$

$T$ : Lifetime of the asset

# 1. Fundamentals – Real options analysis

Managerial flexibility is represented by the adjusted present value:

$$APV = NPV(\text{Investment}) + \text{Option Value}$$

The option type used here is the call option which is computed using the Black-Scholes formula

$$\begin{aligned} \text{Value of call option} &:= \text{Call}(P, t, r_f, \sigma, EX) \\ &= [\text{delta} * \text{share price}] - [\text{bank loan}] \\ &= [N(d_1) * P] - [N(d_2) * PV(EX)] \end{aligned}$$

where:

$$d_2 = d_1 - \sigma\sqrt{t}$$

$$d_1 = \frac{\ln[P/PV(EX)]}{\sigma\sqrt{t}} + \frac{\sigma\sqrt{t}}{2}$$

$P$ : Current price of stock  
 $t$ : Number of periods till maturity  
 $r_f$ : Risk free interest rate  
 $\sigma$ : Standard deviation per period  
 $EX$ : Exercise price

## 2. Market characteristics & Motivation



Source: dena.de

- Increase in renewable electricity production (25% in 2014 → 80% in 2050)
  - Higher variability of production
- Reduced grid stability

- Merit order system and priority dispatch penalize conventionals

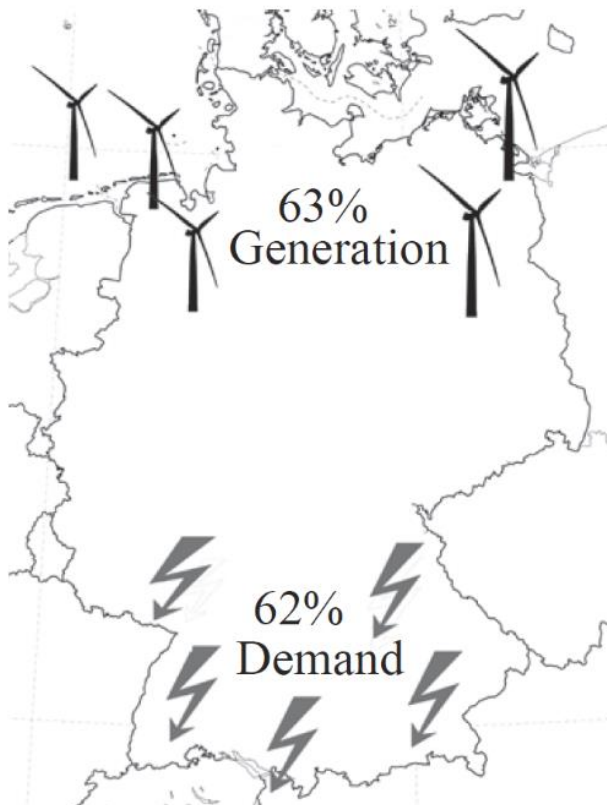
→ Reduced electricity production by conventional power plants

→ Reduced supply security



Source: brd.nrw.de

## 2. Market characteristics & Motivation



- Local clustering of renewable production in northern Germany
  - High electricity demand in southern Germany
  - Shut-down of conventional power plants mainly in southern Germany
- High locational disparity of supply and demand

Source: Schröder et al. (2012)

### 3. Model specification: General characteristics

- The model consists of three parts
- One part for each respective investment opportunity (Grid, Storage, DSM)
- The resulting option values and NPVs are computed and then compared
- Stochastic processes are modeled using a geometric Brownian motion (GBM)

with Ito's lemma:  $p_t = p_0 \cdot e^{\left(\left(\alpha - \frac{\sigma^2}{2}\right)t + \sigma\sqrt{t}z\right)}$

### 3. Model specification: Fundamental real model equations

$$V_{j,t} = \max[PV_{j,t} - I_j + \text{Variable } j, Q_{j,t}]$$

$V_{j,t}$  : Option value at time  $t$

$$Q_{j,t} = \frac{E[V_{j,t+1}]}{1 + r_j}$$

$Q_{j,t}$  : Expected discounted option Value at time  $t+1$

$$Q_{j,T} = 0$$

$Q_{j,T}$  : Value of waiting at the expiration date of the option

$$PV_{j,t} = \sum_{\tau=t+T_{C,j}}^{t+T_{C,j}+L_j} \frac{(R_{j,\tau} - C_{j,\tau})}{(1 + r_j)^{\tau-t}}$$

$PV_{j,t}$ : Present value of the investment consisting of the sum of (discounted) revenues and costs



### 3. Model specification: Real options model specifics, components

Variable	Grid expansion	Energy storage	DSM
Variable $j$	$-C_{\text{Prep,Grid}}$	$\text{Call}_{\text{ESS},i+1,t}$	0
Modularity	No	$j = \text{ESS}, i$ for $i = 1, \dots, n$ & $\text{Call}_{\text{ESS},i+1,t}$	No
Lumpiness	$I_{\text{Grid}} = \text{Lump}_{\text{Grid}} \cdot I_{\text{Grid},\text{km}}$	No	No
Discount factor	$r_f$	$r_{\text{ESS}}$	$r_{\text{DSM}}$
Learning-by-using	No	No	Simple model

- Grid expansion: Additional investment costs, changed discount factor
- Energy storage: Modularity
- DSM: Learning-by-using, large number of stochastic variables

### 3. Model specification: Real options model specifics, Grid expansion

#### Grid expansion model equations

$$V_{\text{Grid},t} = \max[\text{PV}_{\text{Grid},t} - I_{\text{Grid}} - C_{\text{Prep,Grid}}, Q_{\text{Grid},t}]$$

$$Q_{\text{Grid},t} = \frac{E[V_{\text{Grid},t+1}]}{1 + r_{\text{Grid}}} \quad Q_{\text{Grid},T} = 0$$

$$\text{PV}_{\text{Grid},t} = \sum_{\tau=t+T_{\text{C,Grid}}}^{t+T_{\text{C,Grid}}+L_{\text{Grid}}} \frac{p_{\text{Grid},\tau} \cdot U_{\text{Grid},\tau} - OC_{\text{Grid},\tau}}{(1 + r_f)^{\tau-t}}$$

### 3. Model specification: Real options specifics, DSM

#### Demand side management model equations

$$V_{\text{DSM},t} = \max[PV_{\text{DSM},t} - I_{\text{DSM}}, Q_{\text{DSM},t}]$$

$$Q_{\text{DSM},t} = \frac{E[V_{\text{DSM},t+1}]}{1 + r_{\text{DSM}}} \quad Q_{\text{DSM},T} = 0$$

$$PV_{\text{DSM},t} = \sum_{\tau=t+T_{\text{C,DSM}}}^{t+T_{\text{C,DSM}}+L_{\text{DSM}}} \frac{\text{LBU}_{\tau} \cdot (R_{\text{DSM},\tau} - C_{\text{DSM},\tau})}{(1 + r_{\text{DSM}})^{\tau-t}}$$

### 3. Model specification: Real options specifics, Energy storage

#### Energy storage model equations

$$V_{ESS,i,t} = \max[PV_{ESS,i,t} - I_{ESS,i} + Call_{ESS,i+1,t}, Q_{ESS,i,t}]$$

$$Q_{ESS,i,t} = \frac{E[V_{ESS,i,t+1}]}{1 + r_{ESS}} \quad Q_{ESS,i,T-(n-i)t} = 0$$

$$PV_{ESS,i,t} = \sum_{\tau=t+T_{C,ESS,i}}^{t+T_{C,ESS,i}+L_{ESS}} \frac{(R_{ESS,i,\tau} - C_{ESS,i,\tau})}{(1 + r_{ESS})^{\tau-t}}$$

### 3. Model specification: Parameterization

Parameter	Value	Parameter	Value
$r_f$	0.015	$U_{High}$	60,000 MWh/Month
$i$	0.015	$RI$	57,500,000
$\beta$	0.779	$\eta_{HF} = \eta_{LF}$	0.33
$r_m$	0.05	$\eta_{ESS}$	0.7
$r_{Grid} = r_{DSM} = r_{ESS}$	0.039	$OC_{High}$	€ 4,750
$p_{HF,0}$	27.007 €/MWh	$OC_{Low}$	€ 5,650
$p_{LF,0}$	9.232 €/MWh	$SK_{High}$	€ 2,200
$p_{Grid,0}$	17.9 €/MWh	$SK_{Low}$	€ 7,750
$p_{E,High,0}$	55 €/MWh		
$\Delta p_{E,0}$	25 €/MWh	$L_{Grid} = L_{DSM} = L_{ESS}$	15 years
$\alpha_{P,Grid}$	0.011/year	$Lump_{Grid}$	100
$\alpha_{Grid}$	0/year	$OC_{Grid}$	€ 5,000
$\alpha_{PE}$	0.067/year	$C_{Prep,Grid}$	€ 100,000
$\alpha_{HF}$	0.059/year	$I_{Grid,km}$	7924.53 €/km
$\alpha_{LF}$	0.022/year	$T_{C,Grid}$	4 years
$\alpha_{\Delta}$	0.020		
$\sigma_{Grid}$	0.172	$OC_{DSM}$	€ 1,000
$\sigma_{PE}$	0.120	$I_{DSM}$	€ 8,000,000
$\sigma_{HF}$	0.540	$T_{C,DSM}$	1 year
$\sigma_{LF}$	0.405		
$\sigma_{\Delta}$	0.496	$OC_{ESS}$	€ 5,500
$\sigma_{ESS}$	0.355	$I_{ESS,i}$	€ 33.9 million
$\bar{U}_{Grid}$	6,000 MWh/Day	$T_{C,ESS,1}$	2 years
$U_{Low}$	60,000 MWh/Month	$T_{C,ESS,i>1}$	0.5 years

Sources: Frontier Economics (2010), European Energy Exchange AG (2014), BAFA (2014), Swider (2007); own compilation.

### 3. Model specification: Parameter sources

- The Parameters and numbers for computation are typical values found in (Swider, 2007) or real values provides by official institutions (See [www.bundesregierung.de](http://www.bundesregierung.de))
- Linear growth factors and standard deviations are computed using historical values
- The beta factor of RWE is taken for parameterizing the CAPM
  - ≡ Good representation of this industry branch

### 3. Model specification: Fundamental cost benefit model equations

$$B_{j,t} = NPV_{Inv,j,t} + NPV_{Non-Inv,j,t}$$

$B_{j,t}$  : Overall benefit for the investor and non-investor group

$$NPV_{Inv,j,t} = \sum_{\tau=t+T_{C,j}}^{t+T_{C,j}+L_j} \frac{(R_{j,\tau} - C_{j,\tau})}{(1 + r_{ESS})^{\tau-t}} - I_j$$

$NPV_{Investor,j,t}$  : NPV of the investor group consisting of discounted cash flows minus investment costs

$$SSE_j = RI \cdot SSEF_j$$

$SSE_j$  : Supply security factor

RI : Cost of alternative (replacement) investment (CHP plant)

$SSEF_j$  : Investment-specific supply security factor

### 3. Model specification: Cost benefit model, specifics

Variable	Grid expansion	Energy storage	DSM
$NPV_{Non-Inv,j,t}$	$SSE_{Grid}$	$SSE_{ESS}$	$\sum_{\tau=t+T_{C,DSM}}^{t+T_{C,DSM}+L_{DSM}} \frac{LBU_{\tau} \cdot (\Delta p_{E,\tau} \cdot U_{Low})}{(1 + r_{DSM})^{\tau-t}}$ $+ SSE_{DSM}$
$SSEF_j$	6.0	0.75	0.5

- Grid expansion: Supply security factor is significantly higher than in the energy storage and DSM cases
- Energy storage: No modularity for the cost benefit model
- DSM: Supply security impact low by comparison, Non-investor group benefits from lower electricity prices



# 3. Model specification: Supply security factors

- The supply security factors are different for each investment opportunity
  - ≡ Different technologies have a different impact on supply security
  - ≡ The investment is compared to an alternative (replacement) investment (RI) that provides the same amount electricity at a specified location
  
- Grid expansion: SSEF of 6
  - ≡ Has a considerably higher capacity than what the RI could provide
  - ≡ Connects two areas of potential supply and demand
  - ≡ Hence has a high SSEF
  
- Energy storage systems: SSEF of 0.75
  - ≡ Can store energy but also needs to have energy stored to supply
  - ≡ Supply and demand can be offset temporarily
  - ≡ Hence lower than 1 but still high
  
- Demand side management: SSEF of 0.5
  - ≡ Demand has to be managed short-term
  - ≡ Not always available
  - ≡ Lower availability than ESS hence lower SSEF

# 4. Results – Real options analysis

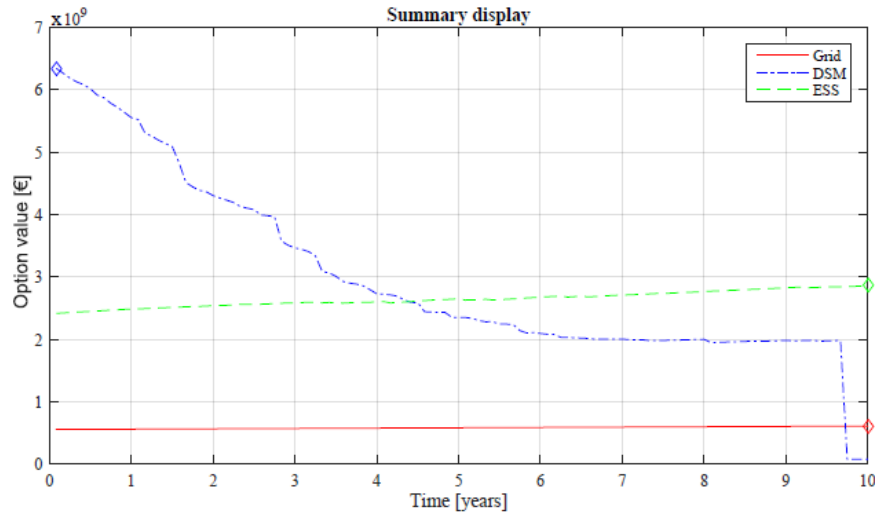


Figure 4.6: Summary display of the real options analysis for a finite time horizon.

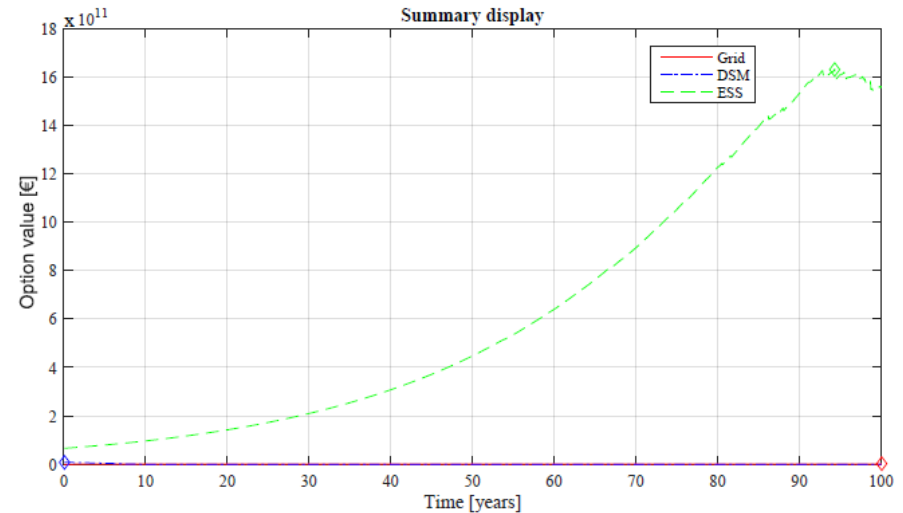


Figure 4.7: Summary display of the real options analysis for an infinite time horizon.

- DSM investment has high volatility caused by stochastic variables but the highest overall option value
- Energy storage investment is the best for an infinite time horizon
- Grid expansion investments have the highest stability
- All investments show positive option values

# 4. Results – Cost benefit analysis

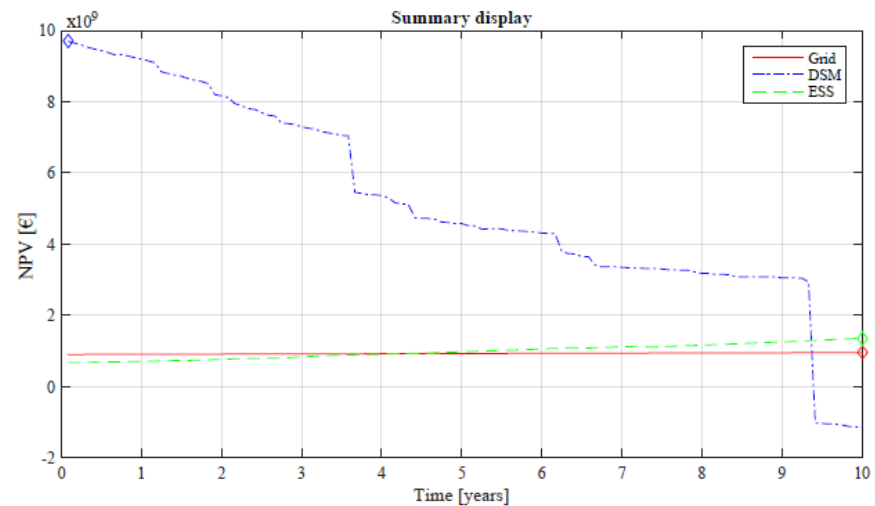


Figure 5.4: Summary display of investment NPVs.

Source: Own figure.

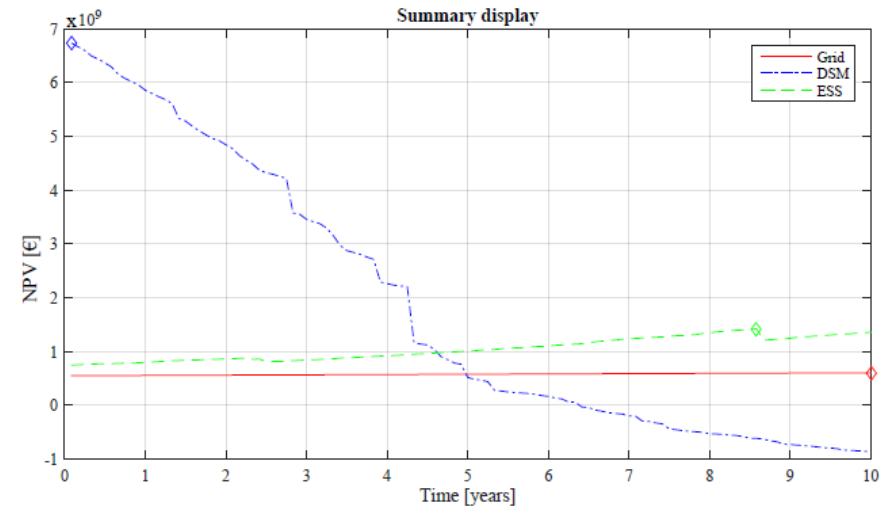


Figure 5.6: Summary display of NPVs without consideration for the value of supply security.

Source: Own figure.

- Supply security → Grid expansion has higher benefit than energy storage
- DSM investment stays volatile for the welfare analysis cases
- Comparison to ROA results show the value of modular investment options for the energy storage case

# 5. Summary & Conclusion

- The models presented are all heavily simplified representations of reality
  - ≡ Show principal value of model specifics considered
  - ≡ Can be extended at will
- All possible investment opportunities considered show positive results
  - ≡ With the data used
  - ≡ Option value & Overall benefit
- The demand side investment is prone to high volatility due to many stochastically changing price vectors
  - ≡ Has the potential for the highest benefit
- The real options analysis demonstrates the value of modular investments for the energy storage investment case
  - ≡ Option value increases significantly with the expiration time of the option
- The value of supply security should not be neglected in a cost benefit analysis of an energy investment
  - ≡ Grid expansion > Energy storage

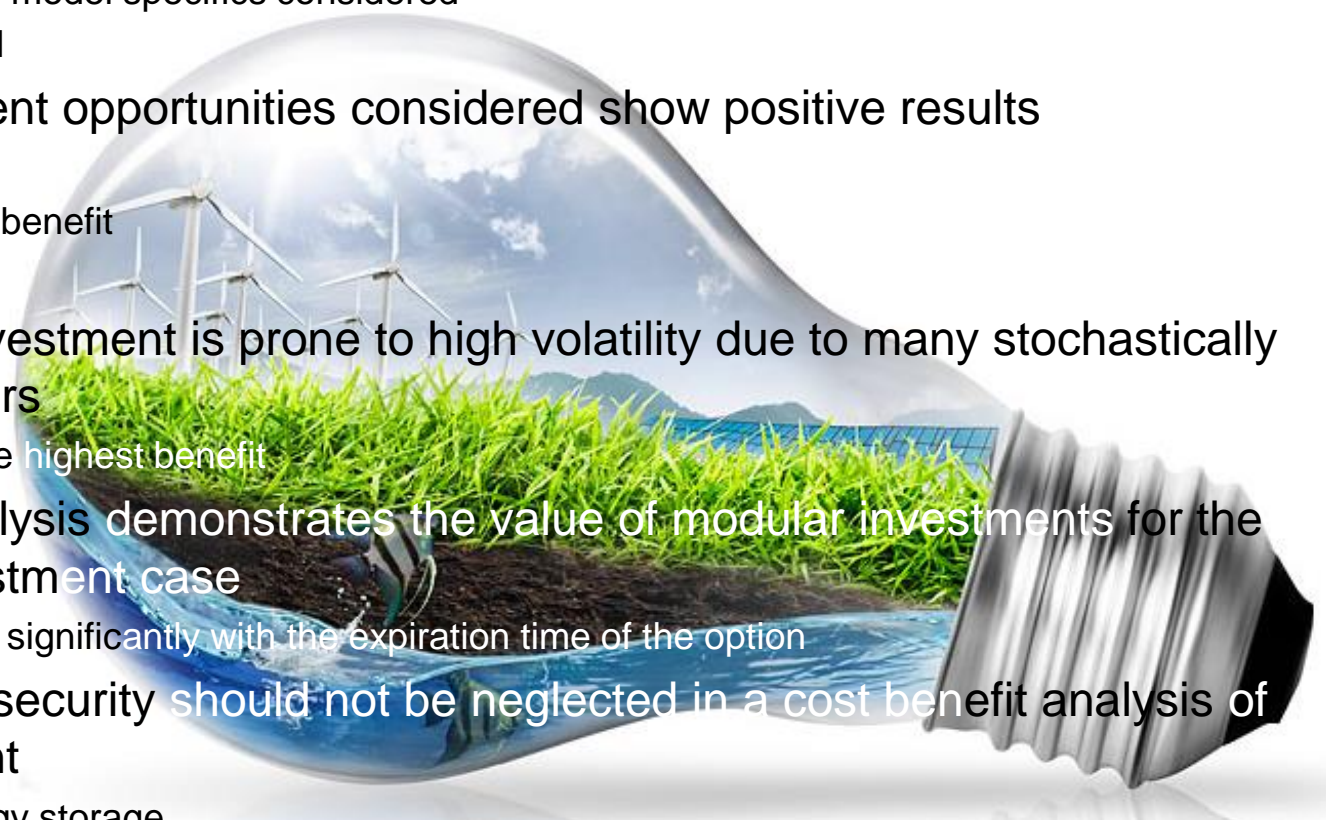


Image Source: finance-magazin.de

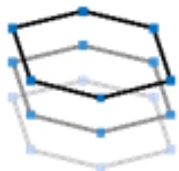
# Many thanks for your kind attention – any questions?

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