

Erläuterung zu Stoff, S. 343 f.

Lerner-Index (Monopol):
$$L_x = \frac{p - GK}{p} = -\frac{1}{e}$$

Beweis:

$$\begin{aligned} \pi &= p(x)x - C(x) \\ \frac{\partial \pi}{\partial x} &= \frac{\partial p}{\partial x}x + p - C'(x) \stackrel{!}{=} 0 \quad \left| + C'(x) \right|; p \\ \frac{\partial p}{\partial x} \frac{x}{p} + 1 &= \frac{C'(x)}{p} && \left| -1; C'(x) = GK \right. \\ \frac{\partial p}{\partial x} \frac{x}{p} &= \frac{GK}{p} - 1 = \frac{GK - p}{p} && \left. \left| \frac{\partial p}{\partial x} \frac{x}{p} = \frac{1}{e} \right| \cdot (-1) \right. \\ -\frac{1}{e} &= \frac{p - GK}{p} = L_x \end{aligned}$$

Lerner-Index (Cournot-Oligopolist):

$$L_x = -\frac{s_i}{e} \quad s_i = \frac{x}{X}$$

Beweis:

$$\begin{aligned} \pi &= p(x)x - C(x) \\ \frac{\partial \pi}{\partial x} &= \frac{\partial p}{\partial x}x + p - C'(x) \stackrel{!}{=} 0 \quad \left| + C'(x) \right|; p \\ \frac{\partial p}{\partial x} \frac{x}{p} + 1 &= \frac{C'(x)}{p} && \left| -1 \right|; \frac{X}{X}; C'(x) = GK \\ \frac{x}{X} \frac{\partial p}{\partial x} \frac{X}{p} &= \frac{GK - p}{p} && \left| \frac{\partial p}{\partial x} \frac{x}{p} = \frac{1}{e} \right| \cdot (-1); \frac{x}{X} = s_i \\ -\frac{s_i}{e} &= \frac{p - GK}{p} = L_x \end{aligned}$$