

# Vacuum Technology WS 20/21 Virtually presented Lecture 8, Dec. 15, 2020

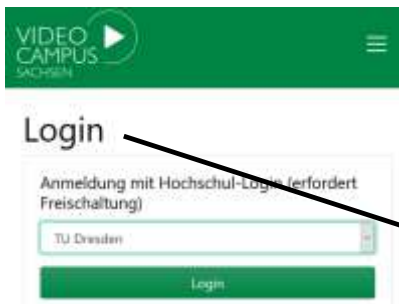
Prof. Dr. Johann W. Bartha

Inst. f. Halbleiter und Mikrosystemtechnik  
Technische Universität Dresden

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## 0. Introduction

Air pressure as a force to the walls of an empty container

## 1. Gas kinetic

Pressure as momentum transfer, Mol & Molvolume, Pressure units, Partial pressure, Boltzmann Velocity&Energy distribution, Impingement rate, monolayer coverage time, mean free path

## 2. Pressure Ranges

## 3. Vacuum technical terms

## 4. Vacuum generation

## 5. Pressure measurement

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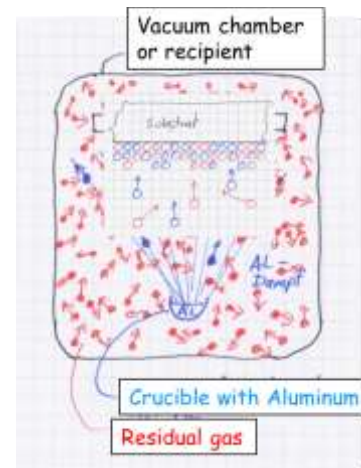
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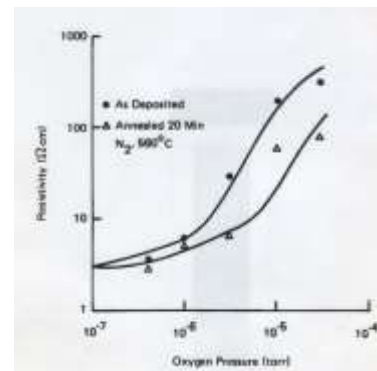
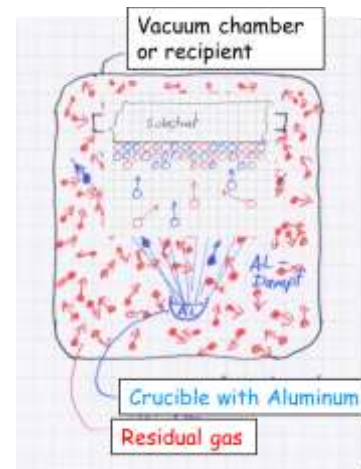
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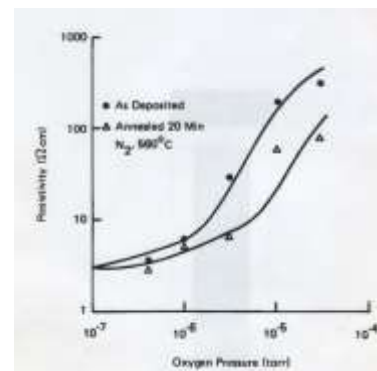
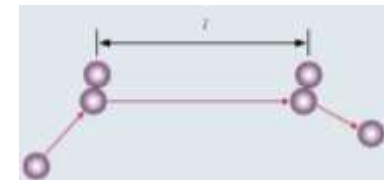
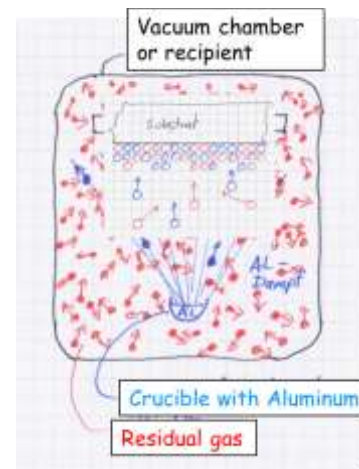
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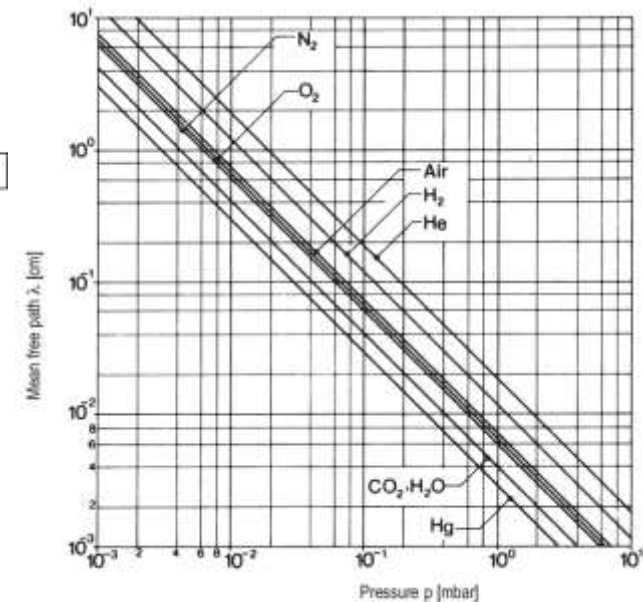
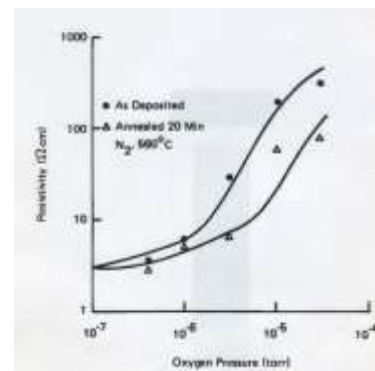
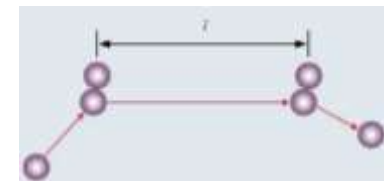
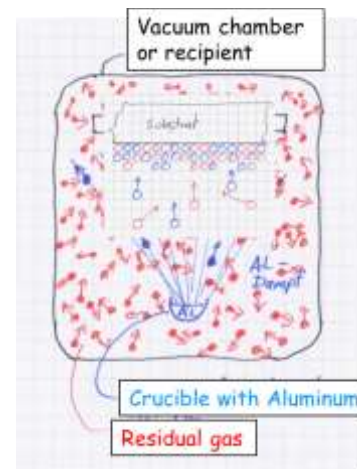
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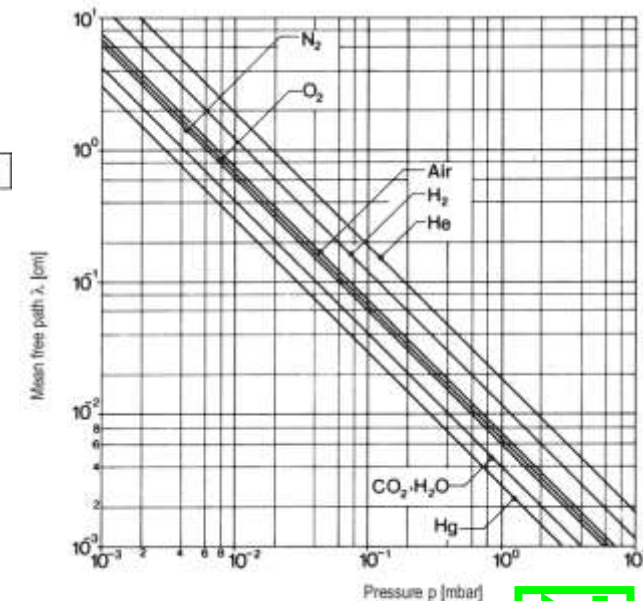
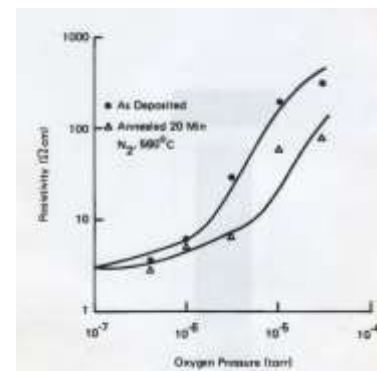
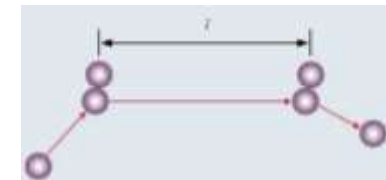
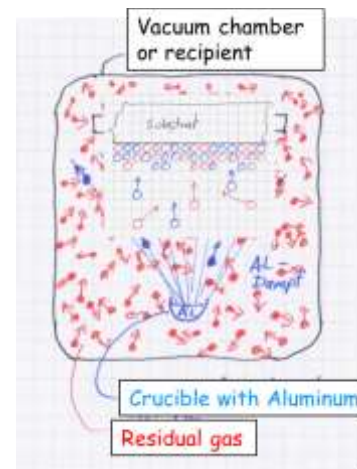
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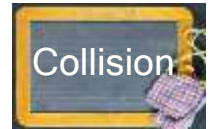
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## Collision rate:

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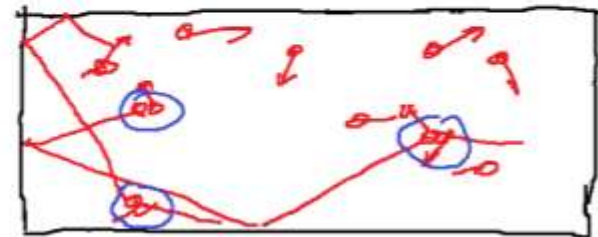
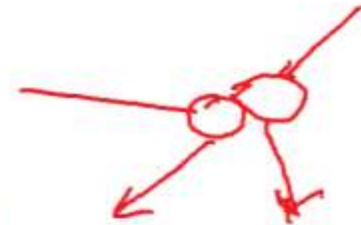
Collision rate: Number of collisions of a single particle per time unit

$$Z_p = \frac{\bar{u}}{\lambda}$$



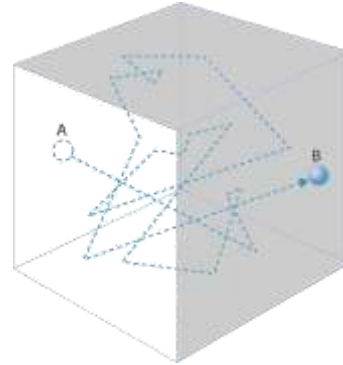
Volume collision rate: Number of collisions of all particles per time and volume unit (collision frequency)

$$Z_v = \frac{n}{2} Z_p = \frac{p}{2kT} Z_p$$



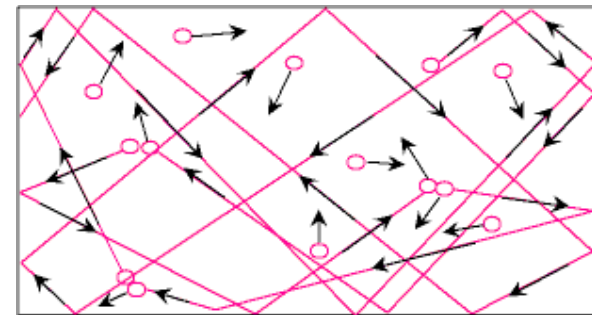
**Collision rate:** Number of collisions of a **single** particle per time unit

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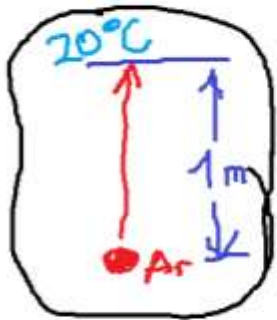
!:  $n/2$  because a collision of 2 particles counts as one collision!

Question: An Ar atom "travels" within a vacuum chamber at  $20^{\circ}\text{C}$  vertically 1 m upwards. Which fraction of its kinetic energy is transferred to potential energy?

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$$E_{\text{pot}} = mg \Delta x = \frac{40 \cdot 10^{-3} \cdot 9.81 \cdot 1}{6^2} = 6.5 \cdot 10^{-25} \text{ J}$$

$$E_{\text{kin}} = \frac{3}{2} kT = 6.06 \cdot 10^{-21} \text{ J}$$

$$\frac{E_{\text{pot}}}{E_{\text{kin}}} \approx 1 \cdot 10^{-4} \Rightarrow \text{Gravit. / can be neglected !}$$

Question: An Ar atom "travels" within a vacuum chamber at 20°C vertically 1m upwards. Which fraction of its kinetic energy is transferred to potential energy?

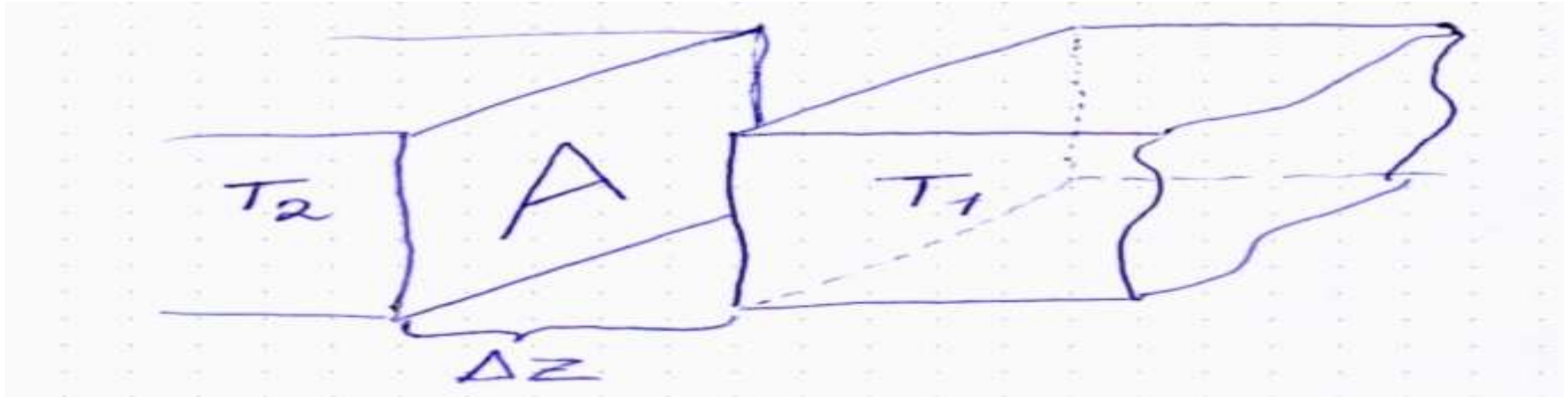
$$E_{\text{pot}} = mg \Delta X = \frac{40 \cdot 10^{-3} \frac{\text{kg}}{\text{mol}} \cdot 9,81 \frac{\text{m}}{\text{s}^2} \cdot 1 \text{ m}}{N_A} = 6,5 \cdot 10^{-25} \text{ J}$$

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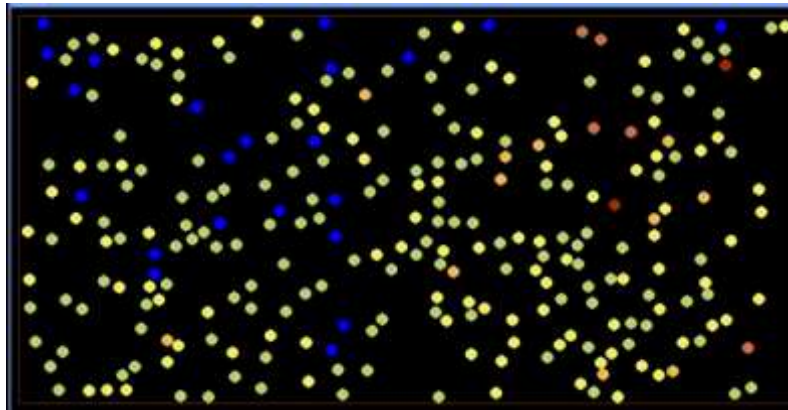
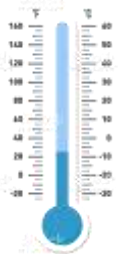
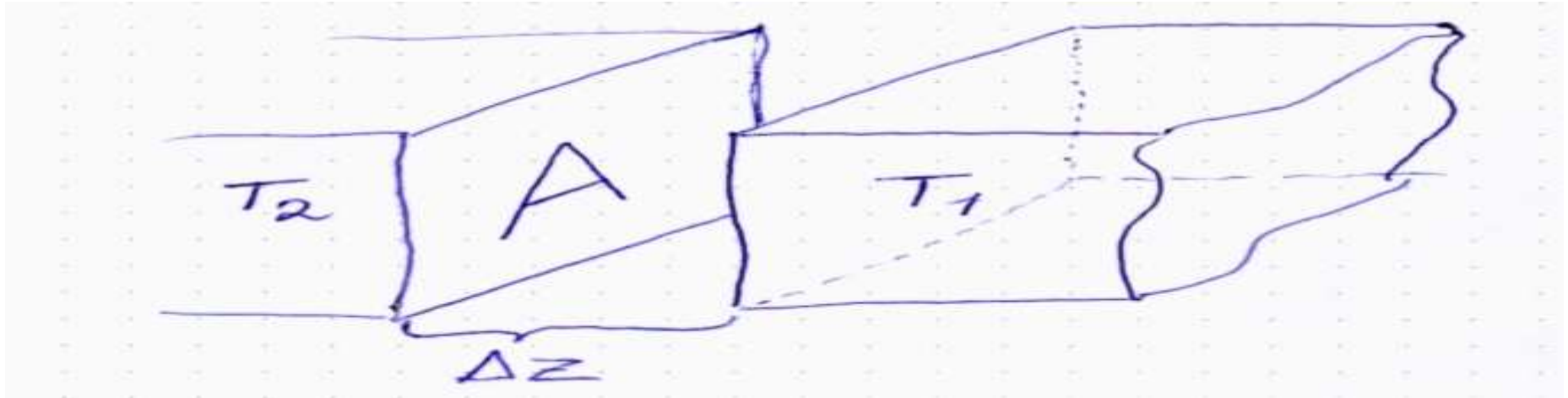
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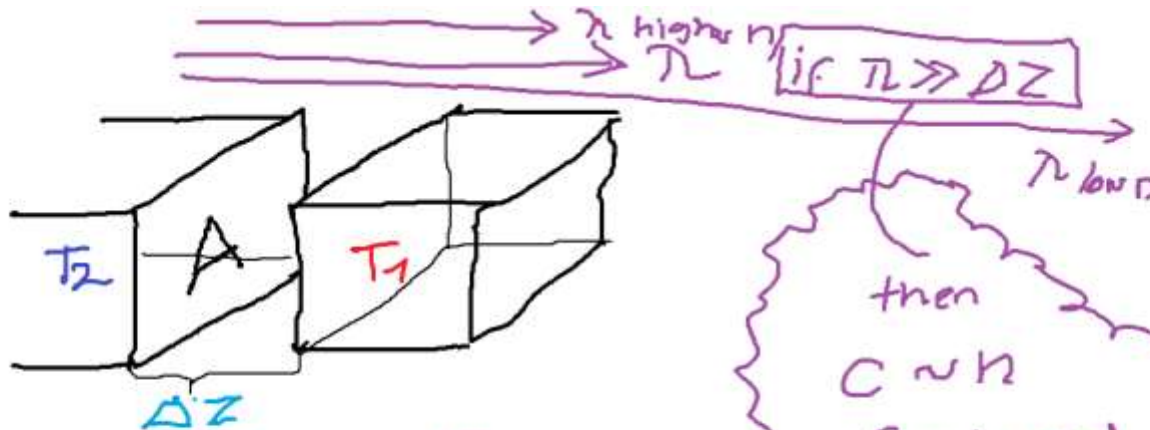


# Heat conduction in a gas and pressure?



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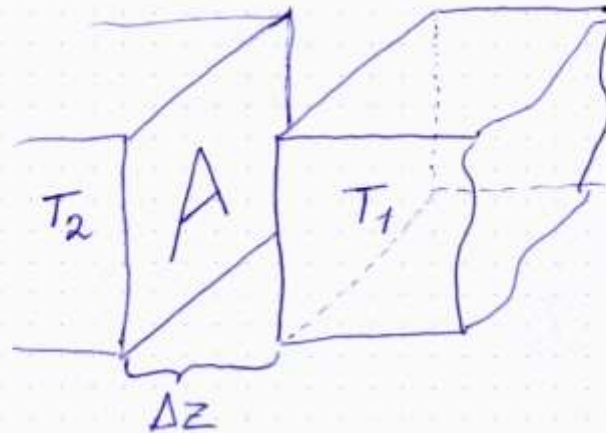
Heat flow:  $\frac{\Delta Q}{\Delta t} = C \frac{\Delta T}{\Delta z} A$

then  
 $C \sim \eta$   
Can be used for pressure  
measurement !!

Heat flow conductivity:  $\frac{p}{RT} \rightarrow \eta \sim \frac{\sqrt{RT}}{\sigma m} \sim \frac{RT}{p \lambda \pi^2 \Delta z}$

- $C \sim \sqrt{T}$
- independent on pressure !!

Heat conduction in a gas:



Heat flow:  $\frac{\Delta Q}{\Delta t} = C \frac{\Delta T}{\Delta z} A$

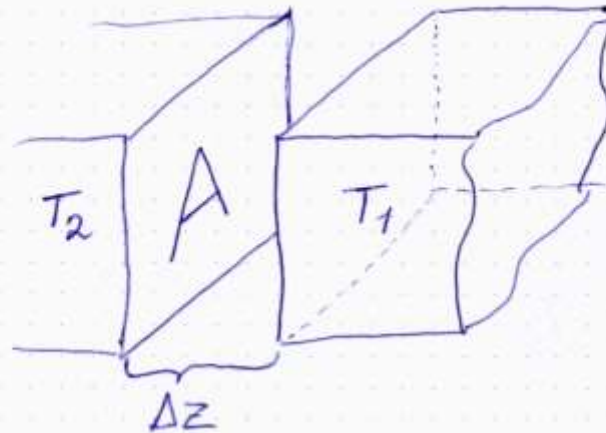
Heat flow conductivity:  $C \sim n \cdot \bar{u} \cdot \bar{\lambda}$

$\frac{p}{kT}$        $\sqrt{\frac{8kT}{\pi m}}$        $\frac{kT}{p \sqrt{4\pi} \lambda^2 \sqrt{2}}$

Heat flow conductivity increases by  $\sqrt{T}$  but is independent from Pressure!

However only as long as  $\lambda < \Delta z$  !!

## Heat conduction in a gas:



Heat flow:  $\frac{\Delta Q}{\Delta t} = C \frac{\Delta T}{\Delta z} A$

Heat flow conductivity:  $c \sim n \cdot \bar{u} \cdot \lambda$

$\frac{P}{kT}$        $\uparrow$        $\sqrt{\frac{8kT}{\pi m}}$        $\leftarrow$        $\frac{kT}{P \sqrt{4\pi} r^2 \sqrt{2}}$

Heat flow conductivity increases by  $\sqrt{T}$  but is independent from Pressure!

However only as long as  $\lambda < \Delta z$  !!

In case  $\lambda > \Delta z$   
we find  $c \sim n \sim P$

⇒ Method for pressure determination!

| Designation,<br>alphabetically         | Symbol           | Value and<br>unit  | Remarks   |
|--|------------------|--|---|
| Atomic mass unit                       | $m_u$            | $1.6605 \cdot 10^{-27} \text{ kg}$   |   |
| Avogadro constant                      | $N_A$            | $6.0225 \cdot 10^{23} \text{ mol}^{-1}$  | Number of particles per mol,<br>formerly: Loschmidt number                      |
| Boltzmann constant                     | $k$              | $1.3805 \cdot 10^{-23} \text{ J} \cdot \text{K}^{-1}$<br>$13.805 \cdot 10^{-23} \frac{\text{mbar} \cdot \text{l}}{\text{K}}$     |   |
| Electron rest mass                     | $m_e$            | $9.1091 \cdot 10^{-31} \text{ kg}$   |   |
| Elementary charge                      | $e$              | $1.6021 \cdot 10^{-19} \text{ A} \cdot \text{s}$   |   |
| Molar gas constant                     | $R$              | $8.314 \text{ J} \cdot \text{mol}^{-1} \text{ K}^{-1}$<br>$= 83.14 \frac{\text{mbar} \cdot \text{l}}{\text{mol} \cdot \text{K}}$ | $R = N_A \cdot k$   |
| Molar volume of<br>the ideal gas       | $V_o$            | $22.414 \text{ m}^3 \text{ kmol}^{-1}$<br>$22.414 \text{ l} \cdot \text{mol}^{-1}$   | DIN 1343; formerly: molar volume<br>at $0 \text{ }^\circ\text{C}$ and 1013 mbar |
| Standard acceleration of free fall     | $g_n$            | $9.8066 \text{ m} \cdot \text{s}^{-2}$   |   |
| Planck constant                        | $h$              | $6.6256 \cdot 10^{-34} \text{ J} \cdot \text{s}$   |   |
| Stefan-Boltzmann constant              | $\sigma$         | $5.669 \cdot 10^{-8} \frac{\text{W}}{\text{m}^2 \text{ K}^4}$  | also: unit conductance, radiation constant                                      |
| Specific electron charge               | $\frac{-e}{m_e}$ | $-1.7588 \cdot 10^{11} \frac{\text{A} \cdot \text{s}}{\text{kg}}$  |   |
| Speed of light in vacuum               | $c$              | $2.9979 \cdot 10^8 \text{ m} \cdot \text{s}^{-1}$  |   |
| Standard reference density<br>of a gas | $\rho_n$         | $\text{kg} \cdot \text{m}^{-3}$  | Density at $\vartheta = 0 \text{ }^\circ\text{C}$ and $p_n = 1013 \text{ mbar}$ |
| Standard reference pressure            | $p_n$            | $101.325 \text{ Pa} = 1013 \text{ mbar}$   | DIN 1343 (Nov. 75)  |
| Standard reference temperature         | $T_n$            | $T_n = 273.15 \text{ K}, \vartheta = 0 \text{ }^\circ\text{C}$   | DIN 1343 (Nov. 75)  |

| Variable  | General formula   | For easy calculation  | Value for air at 20°C   |
|---|---|---|---|
| Most probable speed of particles $c_w$ $\hat{=} \hat{u}$  | $c_w = \sqrt{\frac{2 \cdot R \cdot T}{M}} = \sqrt{\frac{2 k T}{m}}$   | $c_w = 1.29 \cdot 10^4 \sqrt{\frac{T}{M}} \left[ \frac{\text{cm}}{\text{s}} \right]$                      | $c_w = 410 \text{ [m/s]}$   |
| Mean velocity of particles $\bar{c}$ $\bar{u}$            | $\bar{c} = \sqrt{\frac{8 \cdot R \cdot T}{\pi \cdot M}} = \sqrt{\frac{8 k T}{\pi m}}$   | $\bar{c} = 1.46 \cdot 10^4 \sqrt{\frac{T}{M}} \left[ \frac{\text{cm}}{\text{s}} \right]$                  | $\bar{c} = 464 \text{ [m/s]}$   |
| Mean square of velocity of particles $\bar{c}^2$ $u_{ms}$ | $\bar{c}^2 = \frac{3 \cdot R \cdot T}{M} = \frac{3 k T}{m}$   | $\bar{c}^2 = 2.49 \cdot 10^6 \frac{T}{M} \left[ \frac{\text{cm}^2}{\text{s}^2} \right]$                   | $\bar{c}^2 = 25.16 \cdot 10^4 \left[ \frac{\text{cm}^2}{\text{s}^2} \right]$                |
| Gas pressure $p$ of particles                             | $p = n \cdot k \cdot T$<br>$p = \frac{1}{3} \cdot n \cdot m_T \cdot \bar{c}^2$<br>$p = \frac{1}{3} \cdot \rho \cdot \bar{c}^2$          | $p = 13.80 \cdot 10^{-20} \cdot n \cdot T \text{ [mbar]}$   | $p = 4.04 \cdot 10^{-17} \cdot n \text{ [mbar]}$ (applies to all gases)                     |
| Number density of particles $n$                           | $n = p/kT$  | $n = 7.25 \cdot 10^{19} \frac{p}{T} \text{ [cm}^{-3}\text{]}$   | $p = 2.5 \cdot 10^{16} \cdot n \text{ [cm}^{-3}\text{]}$ (applies to all gases)             |
| Area-related impingement $Z_A$                            | $Z_A = \frac{1}{4} \cdot n \cdot \bar{c}$<br>$Z_A = \sqrt{\frac{N_A}{2 \cdot \pi \cdot M \cdot k \cdot T}} p$                           | $Z_A = 2.63 \cdot 10^{22} \frac{p}{\sqrt{M \cdot T}} \cdot p \text{ [cm}^{-2} \text{ s}^{-1}\text{]}$     | $Z_A = 2.85 \cdot 10^{20} \cdot p \text{ [cm}^{-2} \text{ s}^{-1}\text{]}$ (see Fig. 78.2)  |
| Volume collision rate $Z_V$                               | $Z_V = \frac{1}{2} \frac{n \cdot \bar{c}}{\lambda}$<br>$Z_A = \frac{1}{c^*} \sqrt{\frac{2 \cdot N_A}{\pi \cdot M \cdot k \cdot T}} p^2$ | $Z_V = 5.27 \cdot 10^{22} \frac{p^2}{c^* \cdot \sqrt{M \cdot T}} \text{ [cm}^{-3} \text{ s}^{-1}\text{]}$ | $Z_V = 8.6 \cdot 10^{22} \cdot p^2 \text{ [cm}^{-3} \text{ s}^{-1}\text{]}$ (see Fig. 78.2) |
| Equation of state of ideal gas                            | $p \cdot V = \nu \cdot R \cdot T$   | $p \cdot V = 83.14 \cdot \nu \cdot T \text{ [mbar} \cdot \ell\text{]}$                                    | $p \cdot V = 2.44 \cdot 10^4 \nu \text{ [mbar} \cdot \ell\text{]}$ (for all gases)          |
| Area-related mass flow rate $q_{m,A}$                     | $q_{m,A} = Z_A \cdot m_T \sqrt{\frac{M}{2 \cdot \pi \cdot k \cdot T \cdot N_A}} p$  | $Q_{m,A} = 4.377 \cdot 10^{-2} \sqrt{\frac{M}{T}} \cdot p \text{ [g cm}^{-2} \text{ s}^{-1}\text{]}$      | $q_{m,A} = 1.38 \cdot 10^{-2} \cdot p \text{ g [cm}^{-2} \text{ s}^{-1}\text{]}$            |

|  |  |   |  |                                    |
|--|--|---|--|------------------------------------|
| $c^* = \lambda \cdot p$ in $\text{cm} \cdot \text{mbar}$<br>(see Tab. III) | $\lambda$ mean free path in cm                     | $N_A$ Avogadro constant in $\text{mol}^{-1}$        | $p$ gas pressure in mbar   | $T$ thermodynamic temperature in K |
| $k$ Boltzmann constant in $\text{mbar} \cdot \text{l} \cdot \text{K}^{-1}$ | $M$ molar mass in $\text{g} \cdot \text{mol}^{-1}$ | $n$ number density of particles in $\text{cm}^{-3}$ | $R$ molar gas constant in $\text{mbar} \cdot \text{l} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$ | $V$ volume in l                    |
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## 1. Gas kinetic

Pressure as momentum transfer, Mol & Molvolume, Pressure units Partial pressure, Boltzmann Velocity&Energy distribution, Impingement rate, monolayer coverage time, mean free path collision rate

## 2. Pressure Ranges

## 3. Vacuum technical terms

## 4. Vacuum generation

## 5. Pressure measurement

# 0. Introduction

Air pressure as a force to the walls of an empty container

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## 2. Pressure Ranges



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2 extreme cases  
in between

Viscous flow



$$\lambda \ll d$$

Particles collide (almost) only with particles  
wall collisions negligible!

Molecular flow



$$\lambda \gg d$$

Particles col d. (almost) only with the walls  
particle/particle collision negligible !

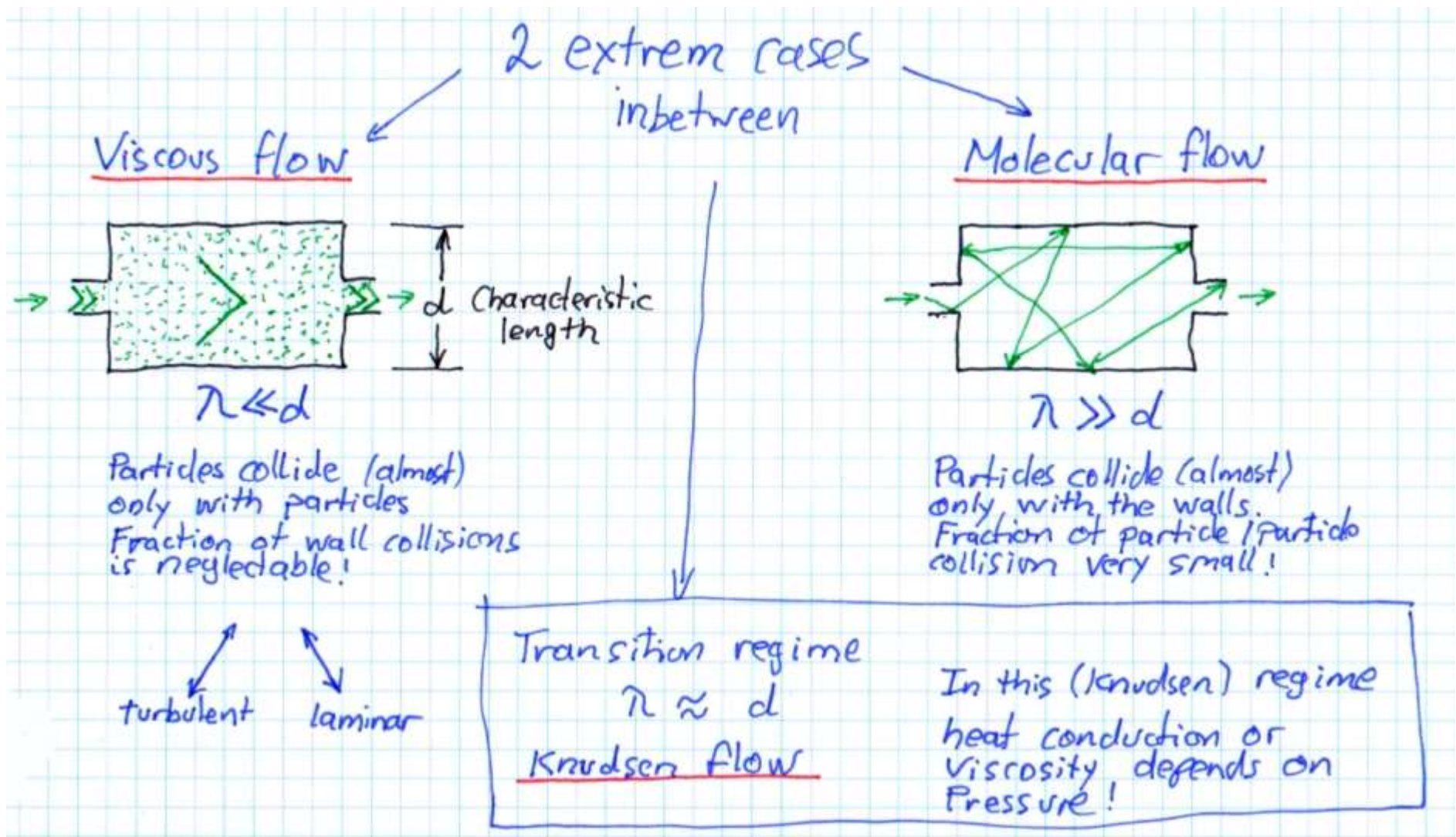
turbulent ↗  
laminar ↘

typical vacuum condition

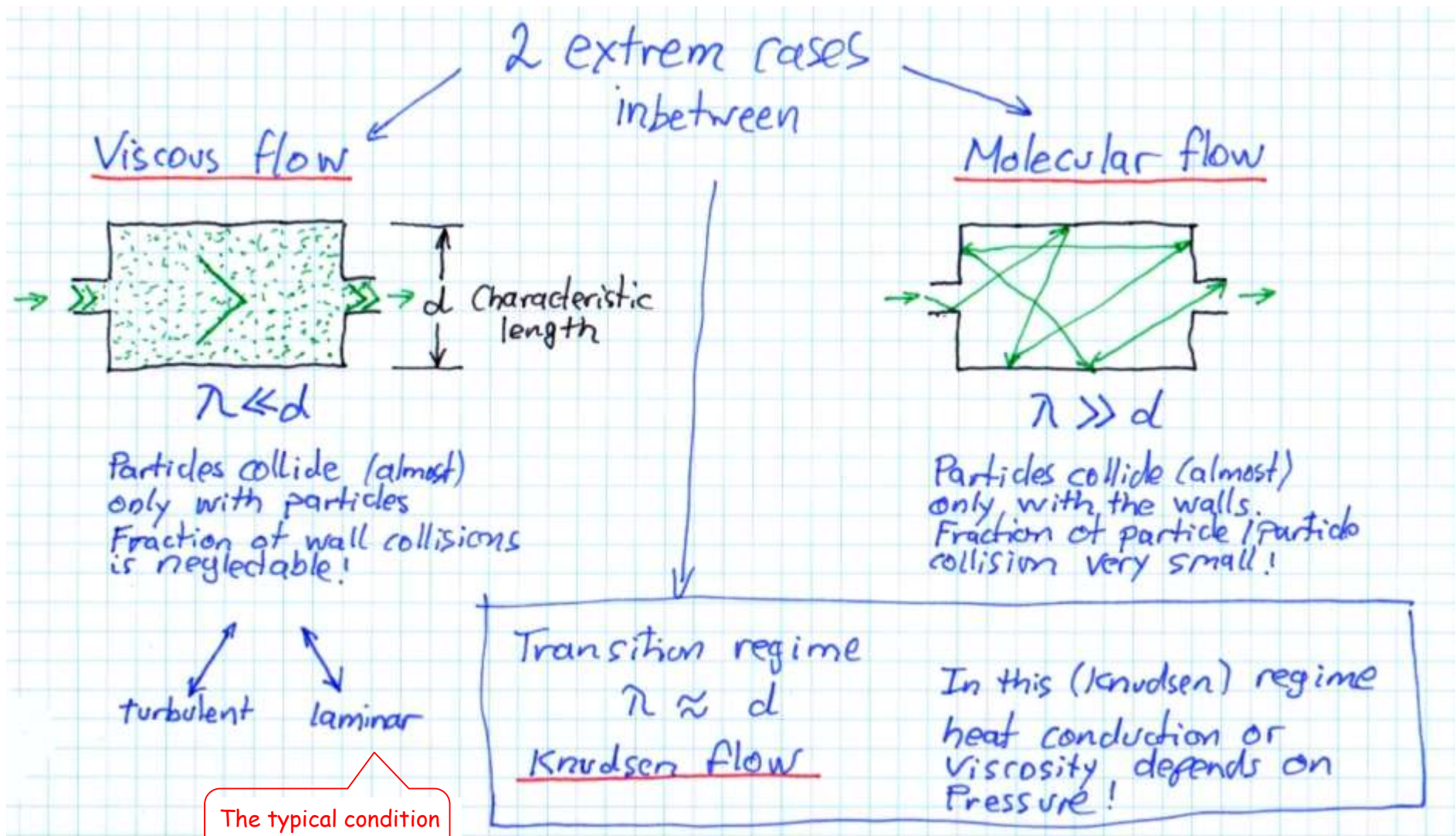
Transition regime  
 $\lambda \approx d$   
Knudsen flow

In the 'Knudsen' regime  
heat conductivity and  
viscosity depends on  
pressure

# Chapter. 2: Pressure ranges and their characteristics



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The plume from this candle flame goes from laminar to turbulent. The Reynolds number can be used to predict where this transition will take place.

For flow in a pipe or tube, the Reynolds number is generally defined as<sup>[10]</sup>

$$\text{Re} = \frac{\rho u D_H}{\mu} = \frac{u D_H}{\nu} = \frac{Q D_H}{\nu A},$$

where

$D_H$  is the **hydraulic diameter** of the pipe (the inside diameter if the pipe is circular) (m),

$Q$  is the **volumetric flow rate** (m<sup>3</sup>/s),

$A$  is the pipe's **cross-sectional area** (m<sup>2</sup>),

$u$  is the mean velocity of the fluid (m/s),

$\mu$  is the **dynamic viscosity** of the fluid (Pa·s = N·s/m<sup>2</sup> = kg/(m·s)),

$\nu$  (nu) is the **kinematic viscosity** ( $\nu = \frac{\mu}{\rho}$ ) (m<sup>2</sup>/s),

$\rho$  is the **density** of the fluid (kg/m<sup>3</sup>).

For flow in a pipe of diameter  $D$ , experimental observations show that for "fully developed" flow, laminar flow occurs when  $\text{Re}_D < 2300$  and turbulent flow occurs when  $\text{Re}_D > 2600$ .



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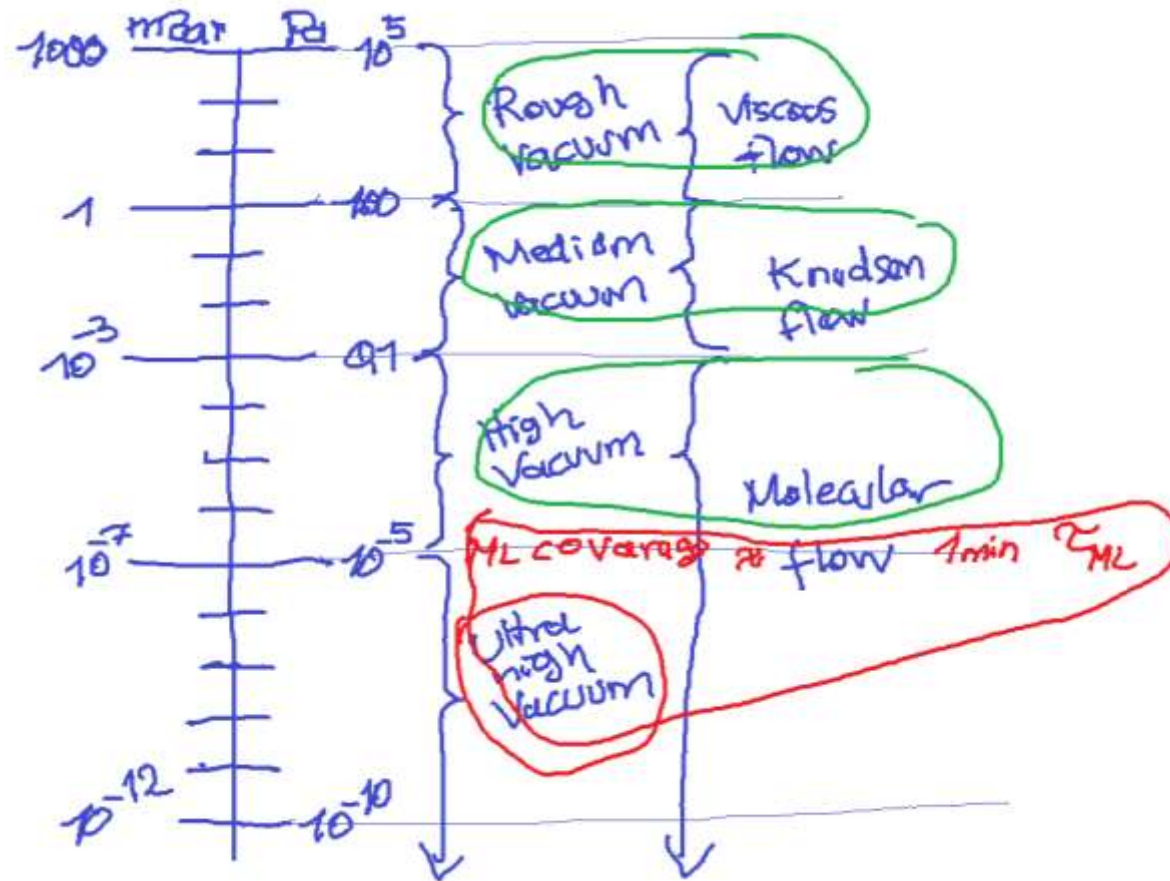
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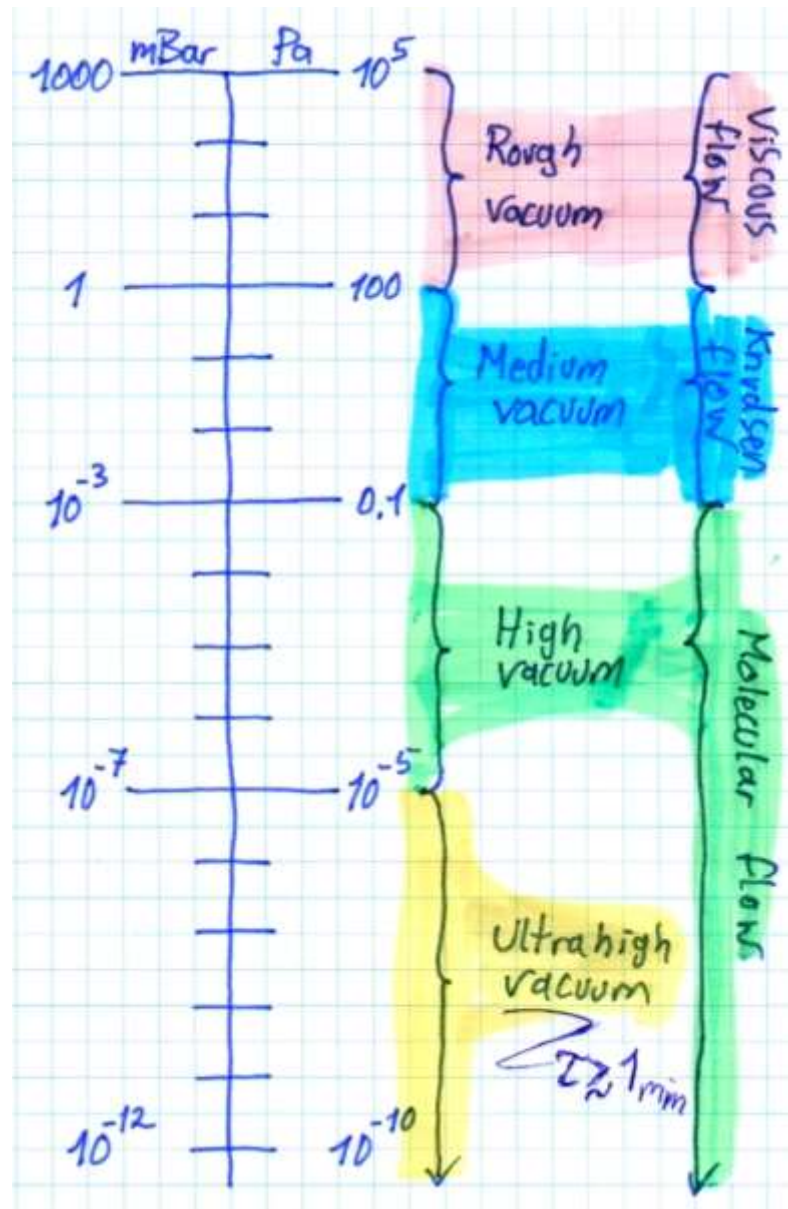
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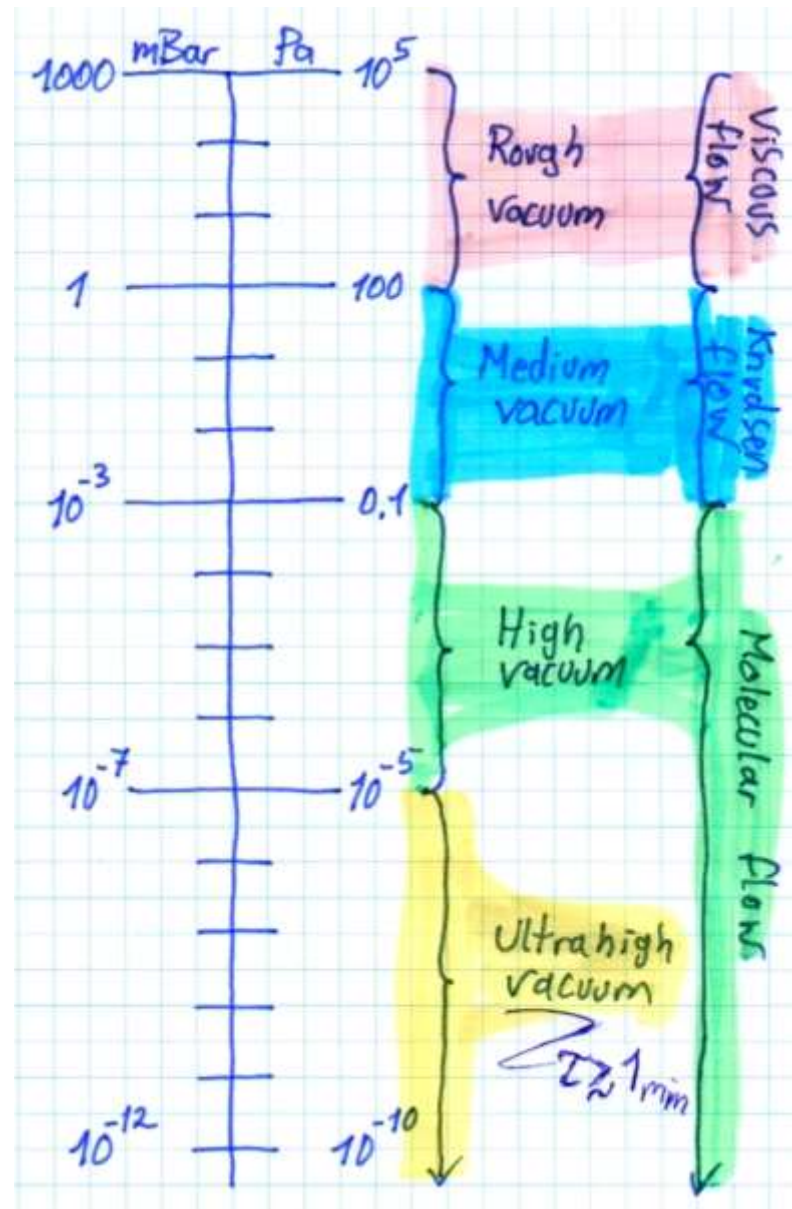




The definition of UHV is associated with the monolayer coverage time, while the other ranges are associated with the kind of gas flow.

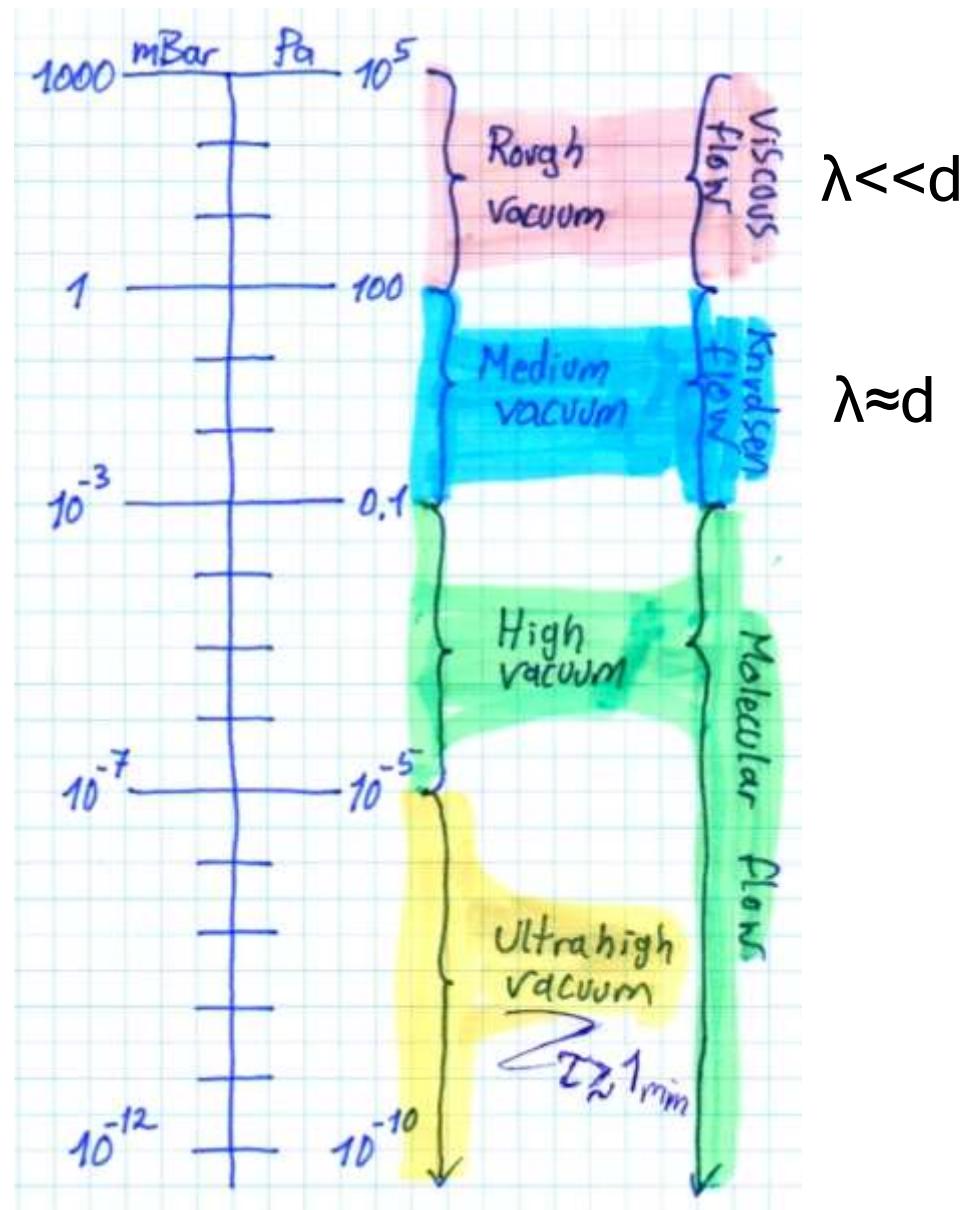


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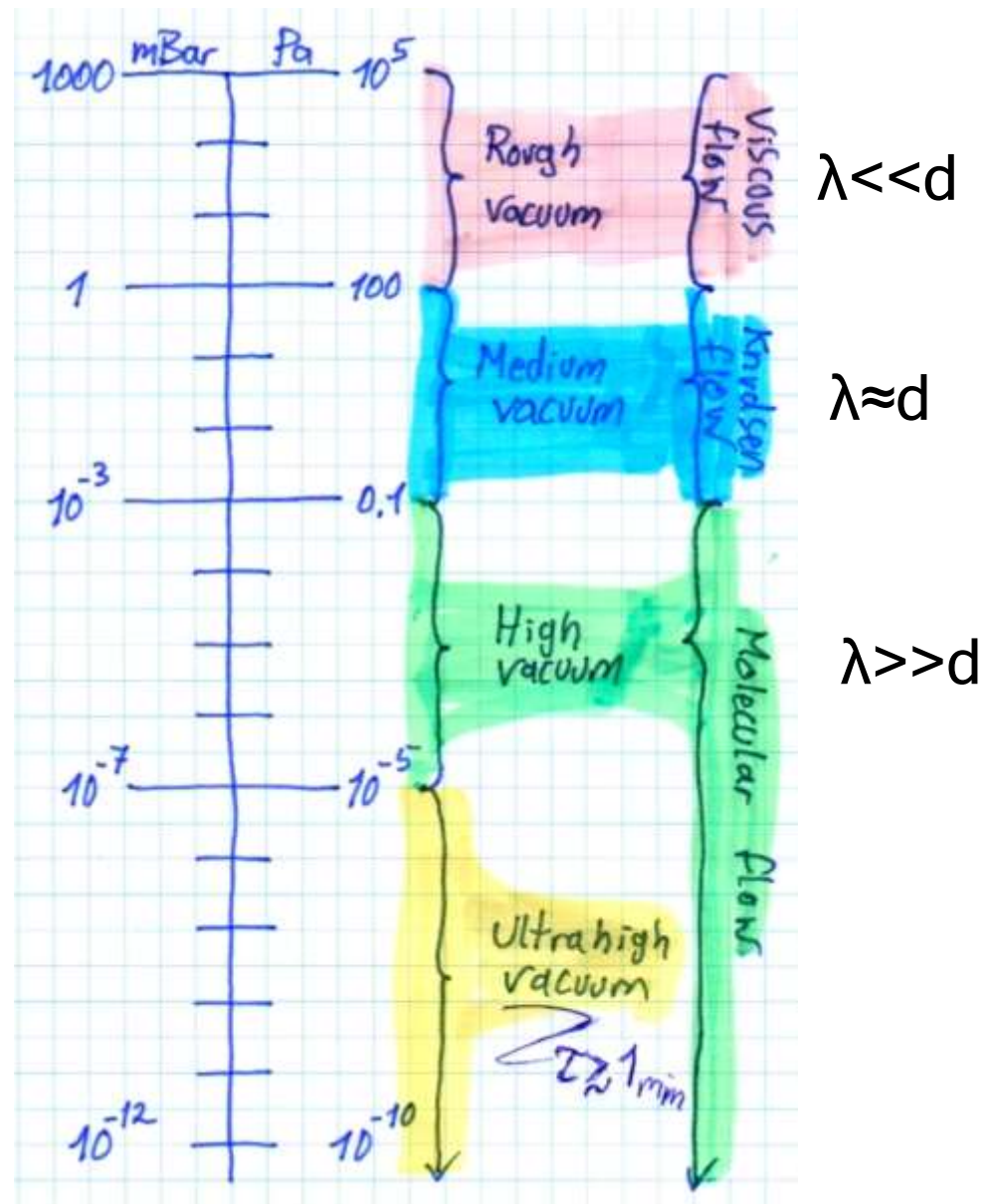


$$\lambda \ll d$$

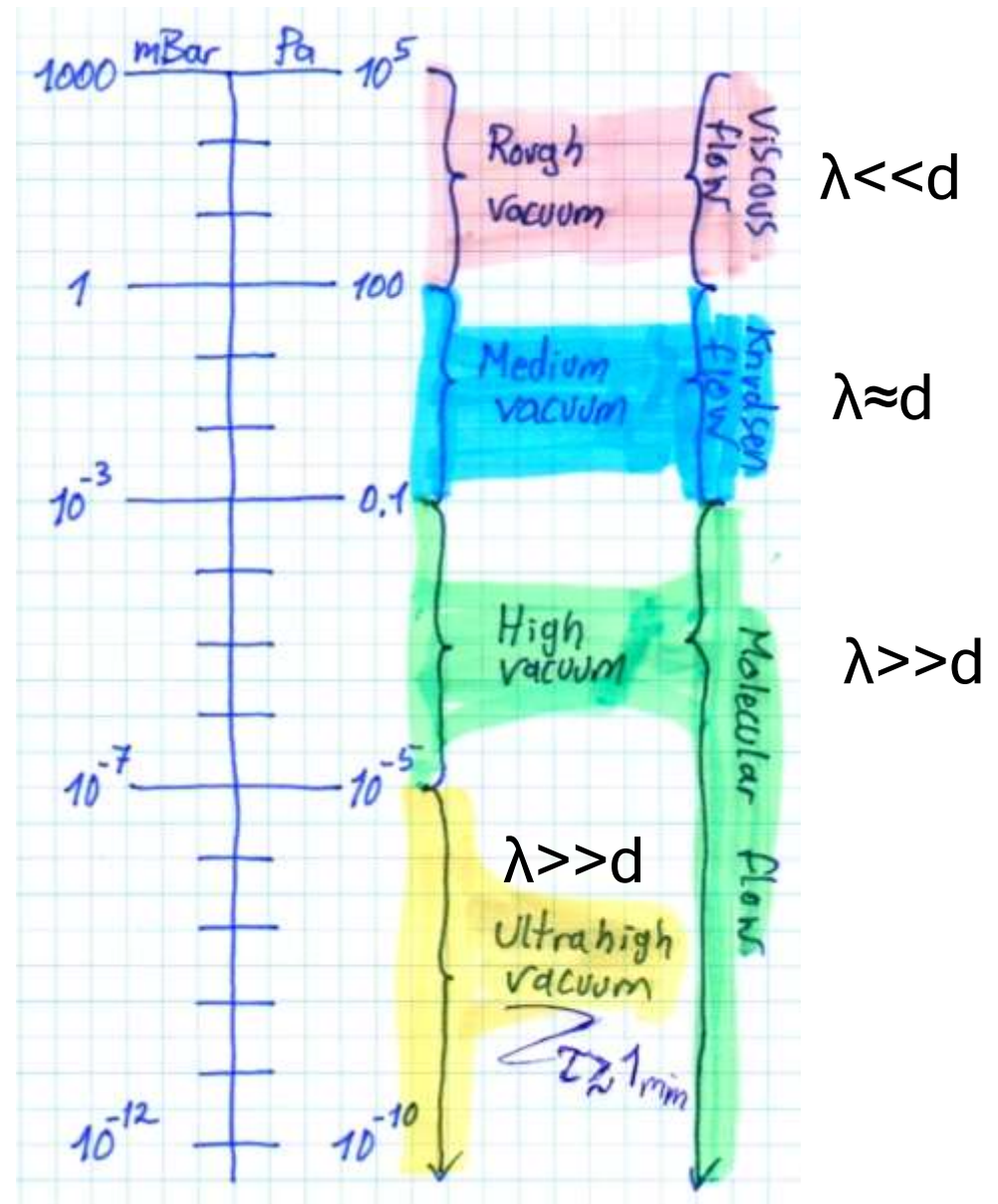
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# Pressure ranges in vacuum technology

|                             |  | Rough vacuum                     | Medium vacuum                                       | High vacuum  | Ultrahigh vacuum   |
|-----------------------------|--|----------------------------------|---|--|--|
| Pressure                    | $p$ [mbar]                                     | $10^{13} - 1$                    | $1 - 10^{-3}$                                       | $10^{-3} - 10^{-7}$                                    | $< 10^{-7}$  |
| Particle number density     | $n$ [ $\text{cm}^{-3}$ ]                       | $10^{19} - 10^{16}$              | $10^{16} - 10^{13}$                                 | $10^{13} - 10^9$                                       | $< 10^9$   |
| Mean free path              | $\lambda$ [cm]                                 | $< 10^{-2}$                      | $10^{-2} - 10$                                      | $10 - 10^5$  | $> 10^5$   |
| Impingement rate            | $Z_a$ [ $\text{cm}^{-2} \cdot \text{s}^{-1}$ ] | $10^{23} - 10^{20}$              | $10^{20} - 10^{17}$                                 | $10^{17} - 10^{13}$                                    | $< 10^{13}$  |
| Vol.-related collision rate | $Z_v$ [ $\text{cm}^{-3} \cdot \text{s}^{-1}$ ] | $10^{29} - 10^{23}$              | $10^{23} - 10^{17}$                                 | $10^{17} - 10^9$                                       | $< 10^9$   |
| Monolayer time              | $\tau$ [s]                                     | $< 10^{-5}$                      | $10^{-5} - 10^{-2}$                                 | $10^{-2} - 100$  | $> 100$  |
| Type of gas flow            |  | Viscous flow                     | Knudsen flow  | Molecular flow   | Molecular flow   |
| Other special features      |  | Convection dependent on pressure | Significant change in thermal conductivity of a gas | Significant reduction in volume related collision rate | Particles on the surfaces dominate to a great extent in relation to particles in gaseous space |

**Viscous flow:**  
**Mean free path  $\ll$  container dimension**  
**(Rough vacuum)**

**Knudsen flow:**  
**Mean free path  $\sim$  container dimension**  
**(Fine vacuum)**

**Molecular flow:**  
**Mean free path  $\gg$  container dimension**

**Monolayer coverage time  $> 1\text{min}$**

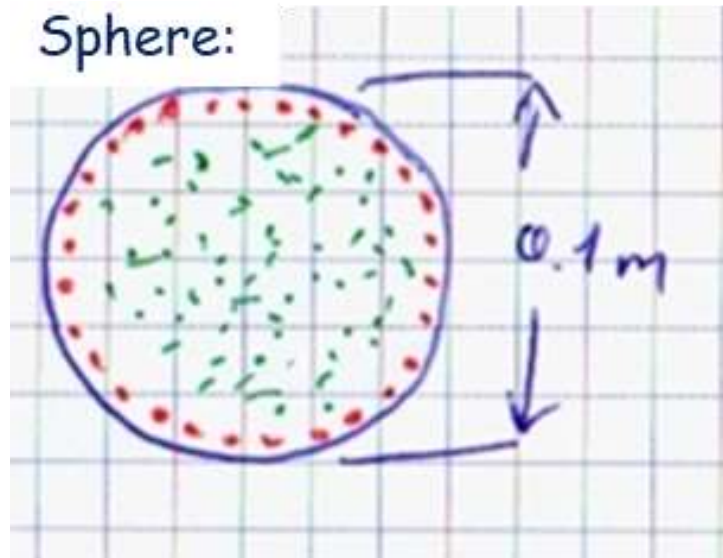
<http://www.falstad.com/gas/>

Example: We assume that the inner wall of a spherical vacuum chamber is covered by a monoatomic (gas) layer. The pressure inside is  $1 \cdot 10^{-3}$  mBar.

Q: How many particles are within the volume and how many of them are attached to the wall?

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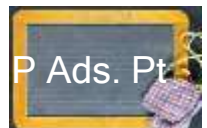
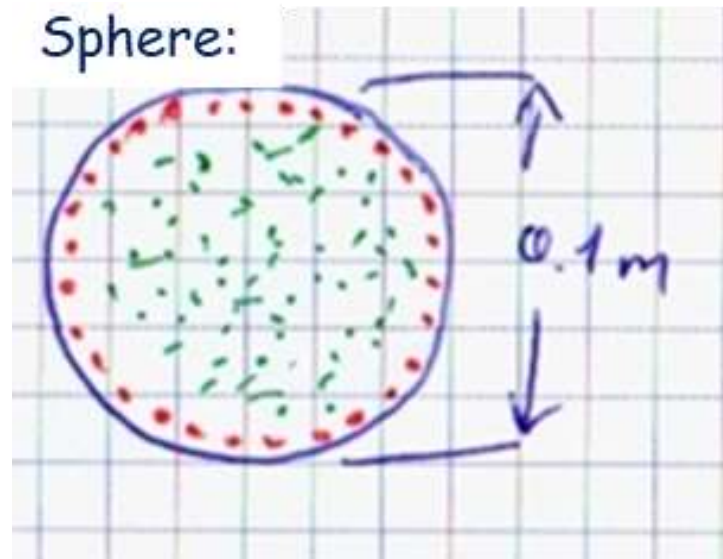
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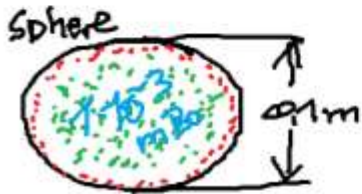
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We assume that the inner wall of a spherical vacuum chamber is covered by a monatomic (gas) layer. The pressure inside is  $1 \cdot 10^{-8}$  mBar.

Q: How many particles are within the volume and how many are attached to the wall?



$$V = \frac{1}{6} d^3 \pi = 5,2 \cdot 10^{-4} \text{ m}^3$$

$$A = \pi d^2 = 0,03 \text{ m}^2$$

$$\text{Monolayer} \hat{=} 1 \cdot 10^{19} \frac{1}{\text{m}^2}$$

$$N_{\text{surf}} = 0,03 \cdot 10^{19} = \underline{3 \cdot 10^{17} \text{ Particles}}$$

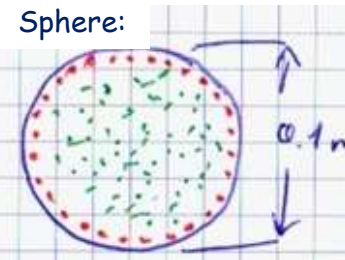
$$N_{\text{vol}} = n \cdot V = \frac{P}{kT} \cdot V = \underline{1,3 \cdot 10^{16} \text{ Particles}}$$

20 times more + sticks at the wall than inside the volume!!

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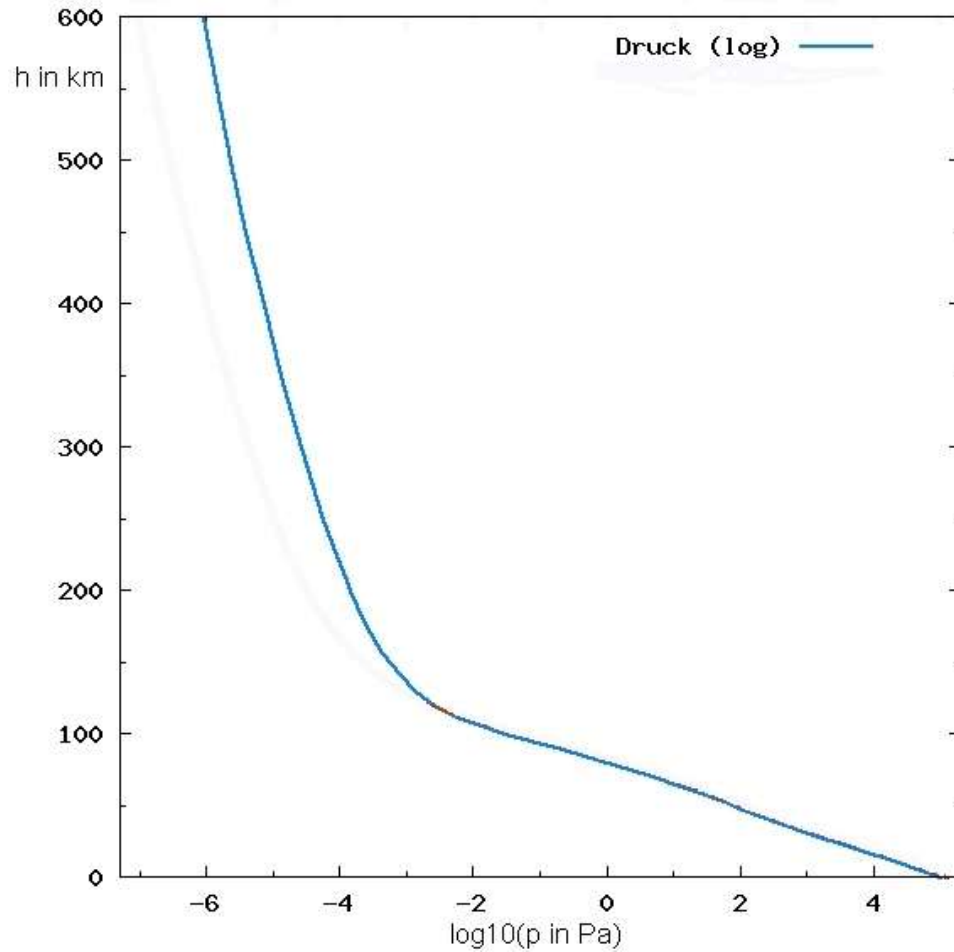
Sphere:



$V = \frac{1}{6} d^3 \pi = 5,2 \cdot 10^{-4} \text{ m}^3$   
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 $N_{\text{obeff.}} = 0,03 \cdot 10^{19} = 3 \cdot 10^{17} \text{ Particles}$   
 $N_{\text{Vol}} = 12 \cdot V = \frac{P}{kT} \cdot V = 1,3 \cdot 10^{16} \text{ Particles}$

At this pressure, there are 20 times more particles at the wall than inside the "vacuum"!

# Vacuum in space

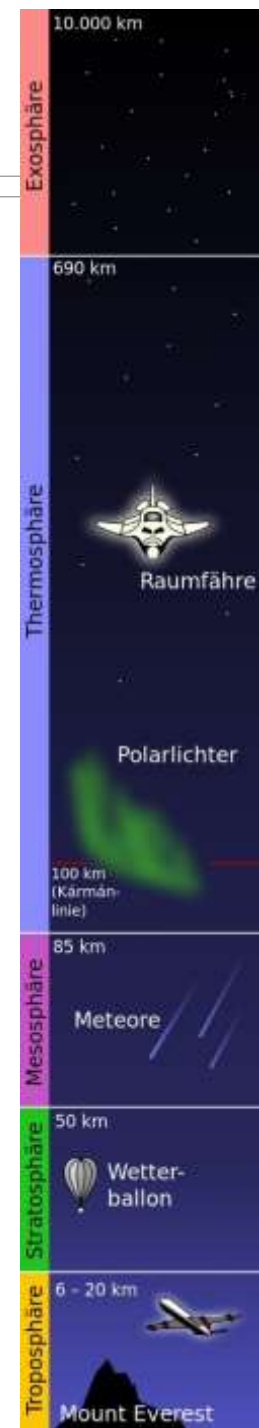


Ultrahoch-

Hoch-

Fein-

Grob- Vakuum





**»Wissen schafft Brücken.«**