Uniform Mean Ergodicity, Quasi-Compactness and Compactness of Koopman Operators

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Abstract

Each continuous mapping $\varphi:X\to X$ on a compact Hausdorff space X induces a lattice homomorphism

$$T_{\varphi}: C(X) \to C(X), \quad f \mapsto f \circ \varphi,$$

on the Banach lattice C(X) of continuous functions $f: X \to \mathbb{C}$, called the *Koopman operator*. The operator theoretic properties that we examine are *uniform mean ergodicity, quasi-compactness* and *compactness* and relate those to more classical properties of dynamical systems.