

GRUNDABLEITUNGEN

$f$	$f'$	$f$	$f'$
$x^n$	$nx^{n-1}$	$\arccos x$	$\frac{-1}{\sqrt{1-x^2}}$
$\frac{1}{x^n}$	$\frac{-n}{x^{n+1}}$	$\arctan x$	$\frac{1}{1+x^2}$
$\sqrt{x}$	$\frac{1}{2\sqrt{x}}$	$\operatorname{arccot} x$	$\frac{-1}{1+x^2}$
$\sqrt[n]{x}$	$\frac{1}{n\sqrt[n]{x^{n-1}}}$	$\sinh x$	$\cosh x$
$e^x$	$e^x$	$\cosh x$	$\sinh x$
$\ln x$	$\frac{1}{x}$	$\tanh x$	$\frac{1}{\cosh^2 x}$
$a^x$	$a^x \ln a$	$\operatorname{coth} x$	$\frac{-1}{\sinh^2 x}$
$x^x$	$x^x(1+\ln x)$	$\operatorname{arsinh} x$	$\frac{1}{\sqrt{x^2+1}}$
$\sin x$	$\cos x$	$\operatorname{arcosh} x$	$\frac{1}{\sqrt{x^2-1}}, \quad x > 1$
$\cos x$	$-\sin x$	$\operatorname{artanh} x$	$\frac{1}{1-x^2}, \quad  x  < 1$
$\tan x$	$\frac{1}{\cos^2 x}$	$\operatorname{arcoth} x$	$\frac{1}{1-x^2}, \quad  x  > 1$
$\cot x$	$\frac{-1}{\sin^2 x}$		
$\arcsin x$	$\frac{1}{\sqrt{1-x^2}}$		
$\int g dx$	$g$	$\int g dx$	$g$

Aus: Merziger et al., Formeln und Hilfen zur höheren Mathematik, ISBN:978-3-9239-2336-6, Binomi Verlag 2010

# GRUNDINTEGRALE ZUR VORLESUNG MATHEMATIK I/1

Es sei  $a \in \mathbb{R}$  ein beliebiger, konstanter Parameter.

$$1. \int x^a dx = \frac{x^{a+1}}{a+1} + C \quad (a \neq -1)$$

$$2. \int e^x dx = e^x + C$$

$$3. \int a^x dx = \frac{1}{\ln a} a^x + C$$

$$4. \int \frac{1}{x+a} dx = \ln|x+a| + C$$

$$5. \int \frac{1}{x^2+a^2} dx = \frac{1}{a} \arctan\left(\frac{x}{a}\right) + C$$

$$6. \int \sqrt{x^2+a^2} dx = \begin{cases} \frac{1}{2} (x\sqrt{x^2+a^2} + a^2 \operatorname{arsinh}(\frac{x}{a})) + C \\ \frac{1}{2} (x\sqrt{x^2+a^2} + a^2 \ln|x+\sqrt{x^2+a^2}|) + C \end{cases}$$

$$7. \int \frac{1}{\sqrt{x^2+a^2}} dx = \operatorname{arsinh}\left(\frac{x}{a}\right) + C$$

$$8. \int \frac{1}{\sqrt{x^2-a^2}} dx = \operatorname{arcosh}\left(\frac{x}{a}\right) + C$$

$$9. \int \frac{1}{\sqrt{a^2-x^2}} dx = \arcsin\left(\frac{x}{a}\right) + C$$

$$10. \int \frac{Bx+C}{x^2+px+q} dx = \frac{B}{2} \ln|x^2+px+q| + (C - \frac{Bp}{2}) \int \frac{1}{x^2+px+q} dx$$

$$11. \int \frac{1}{x^2+px+q} dx = \frac{2}{\sqrt{4q-p^2}} \arctan \frac{2x+p}{\sqrt{4q-p^2}} + C \quad \boxed{\text{nur für } 4q - p^2 > 0}$$

$$12. \int \frac{Bx+C}{(x^2+px+q)^\beta} dx = -\frac{B}{2(\beta-1)} \frac{1}{(x^2+px+q)^{\beta-1}} + (C - \frac{Bp}{2}) \int \frac{1}{(x^2+px+q)^\beta} dx$$

$$13. \int \frac{1}{(x^2+px+q)^\beta} dx = \frac{1}{(\beta-1)(4q-p^2)} \frac{2x+p}{(x^2+px+q)^{\beta-1}} + \frac{4\beta-6}{(\beta-1)(4q-p^2)} \int \frac{1}{(x^2+px+q)^{\beta-1}} dx$$

$$14. \int \sin(x) dx = -\cos(x) + C$$

$$15. \int \cos(x) dx = \sin(x) + C$$

$$16. \int \frac{1}{\cos^2(x)} dx = \int (1 + \tan^2(x)) dx = \tan(x) + C$$

$$17. \int \sinh(x) dx = \cosh(x) + C$$

$$18. \int \cosh(x) dx = \sinh(x) + C$$

$$19. \int \frac{1}{\cosh^2(x)} dx = \tanh(x) + C$$

$$20. \int \frac{1}{\sin^2(x)} dx = \int (1 + \cot^2(x)) dx = -\cot(x) + C$$

$$21. \int f'(x)f(x) dx = \frac{1}{2}f^2(x) + C$$

$$22. \int \frac{f'(x)}{f(x)} dx = \ln|f(x)| + C$$