Cotunneling into a Kondo lattice with odd hybridization

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Cotunneling into Kondo systems, where an electron enters an f-electron material via a cotunneling process through the local-moment orbital, has been proposed to explain the characteristic line shapes observed in scanning-tunneling-spectroscopy (STS) experiments. Here we extend the theory of electron cotunneling to Kondo-lattice systems in which the bulk hybridization between conduction and f electrons is odd under inversion, being particularly relevant to Kondo insulators. Compared to the case of even hybridization, we show that the interference between normal tunneling and cotunneling processes is fundamentally altered: it is entirely absent for layered, i.e., quasi-two-dimensional materials, while its energy dependence is strongly modified for three-dimensional materials. We discuss implications for STS experiments.

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I. INTRODUCTION

Scanning tunneling spectroscopy has developed into a powerful tool to investigate the surface electronic structure of both bulk and thin-film materials. It provides a spatially resolved map of the local single-particle density of states. Moreover, it has been used to derive information on the momentum-resolved band structure via so-called quasiparticle interference (QPI), i.e., energy-dependent Friedel oscillations caused by dilute impurities [1–3]. Recently, such QPI analysis has been employed [4–9] to confirm the spin-momentum locking of surface states of topological insulators [10–12].

In multiorbital systems, the proper interpretation of tunneling spectra requires knowledge about individual orbital tunneling matrix elements (or their ratios), which are determined by the wave-function overlaps between electronic states in the tip and Wannier states in the material. For Kondo systems [13], involving both weakly correlated conduction electrons and local-moment f electrons, it has been proposed [14,15] that both contribute to scanning-tunneling-spectroscopy (STS) spectra: In addition to direct tunneling into conduction states, cotunneling processes via localized states can occur. Such processes involve a magnetic interaction between the tunneling electron and the local moment. The quantum-mechanical interference between these two tunneling paths, together with the particle-hole (p-h) asymmetry of the conduction band, leads to a characteristic Fano-like line shape in the STS signal [16–23]. The interference term itself is determined by the effective coupling between f and conduction electrons.

Importantly, frequently used model Hamiltonians assume a spatially local Kondo interaction or hybridization between local moments and conduction electrons, such that, for Kondo-lattice systems with inversion symmetry, the effective momentum-space hybridization function is even under inversion.

In an alternative Anderson-model description, the f electrons to vanish, which implies that the interference between normal tunneling and cotunneling is absent in the simplest tunneling models. Complications arise from broken inversion symmetry near the surface, as well as from nonlocal tunneling processes, and we will discuss the consequences for STS spectra. We note that the role of odd hybridization for isolated Kondo impurities has been studied in a few papers in the past, e.g., in the context of graphene [28].

II. TUNNELING CONDUCTANCE FOR HEAVY-FERMION MATERIALS

To set the stage, we review the cotunneling theory of Refs. [14,15] (see Fig. 1). The bulk system is described by operators for conduction electrons and f states, c_{i\sigma} and f_{i\sigma}, respectively; explicit Hamiltonians follow below. A spatially local tunneling process between tip and surface is captured by a Hamiltonian, \[ \hat{H}_T = \sum_{\sigma} p_i \psi_{0\sigma} + \text{H.c.} \], where p is an electron operator for the tip, and \( \psi_0 \) involves both c and f electrons at site 0 below the tip. Importantly, Coulomb interactions on f orbitals are strong and suppress charge fluctuations, leading to cotunneling. In a Kondo-model description, f electrons form local moments \( \bar{S}_i \), and \( \psi_0 \) can be expressed as [14]

\[ \psi_{0\sigma} = v_c c_{i\sigma} + (1/2) \sum_i \bar{v}_f \bar{s}_{\sigma} \cdot \bar{S}_i c_{i\sigma}^\dagger. \]  

Here, \( v_c \) and \( \bar{v}_f \) are the amplitudes for direct tunneling and cotunneling, respectively, \( \bar{s} \) is a Pauli matrix, and \( i \) represents the c electron site(s), which hybridize with the f orbital at 0. In an alternative Anderson-model description, the f electrons become renormalized by Coulomb interactions, which can be captured by a constant renormalization factor \( b \) at the mean-field level, \( f_{i\sigma} = b f_{i\sigma} \), with \( f_{i\sigma} \) being auxiliary fermion operators [13]. As a result, the operator \( \psi_0 \) takes the form [14]

\[ \psi_{0\sigma} = v_c c_{i\sigma} + v_f f_{i\sigma}. \]  

The same renormalized single-particle formulation can be obtained from the Kondo description, employing an SU(N) large-N limit and a mean-field decoupling of the Kondo interaction [13], leading to \( v_f = -\sum_i (f_{0\sigma} c_{i\sigma}) \bar{v}_f \).
FIG. 1. Schematic picture of cotunneling into a 3D heavy-fermion material. Each site (yellow) consists of a conduction $c$ (red) and a localized $f$ (blue) orbital. $\epsilon_c$ describes the on-site $c$ energy, $t_c$ is the NN $c$ hopping, $\epsilon_f$ is the on-site $f$ energy, $t_f$ is the NN $f$ hopping, and $V$ is the NN $c-f$ hybridization, which can be local (top right) or nonlocal (bottom left). The STM tip is described by its DOS $\rho_{\text{tip}}$. Electrons tunnel vertically from the tip into a $c$ orbital with amplitude $v_c$ or into a (renormalized) $f$ orbital with amplitude $v_f$.

Given $H_T$, the tunneling conductance at voltage $\Phi$ is

$$g(\Phi) = -\frac{4e^2}{h} \rho_{\text{tip}} \text{Im}[G_{\psi}(\Phi)],$$

where $e$ is the electron charge, $h$ is Planck’s constant, $\rho_{\text{tip}}$ is the density of states at the top of the tip, assumed energy-independent, and $G_{\psi}$ is the local energy-dependent Green’s function for the operator $\psi_0$. Using Eq. (2), we have

$$G_{\psi}(\omega) = v_c^2 G_c(\omega) + v_f^2 G_f(\omega) + v_c v_f [G_{cf}(\omega) + G_{fc}(\omega)],$$

where the propagators and tunneling amplitudes have been assumed spin-independent, and the spin degeneracy is taken into account in the prefactor of Eq. (3). Abbreviating $\rho(\omega) = -\text{Im}G(\omega)/\pi$, the conductance is then given by

$$g(\Phi) = \frac{4\pi e^2}{h} \rho_{\text{tip}} \left[ v_c^2 \rho_c + v_f^2 \rho_f + v_c v_f (\rho_{cf} + \rho_{fc}) + v_f^2 \rho_f \right].$$

The mixed terms $\rho_{cf}$ and $\rho_{fc}$, arising from the interference of normal tunneling and cotunneling, typically induce a distinct $p-h$ asymmetry at low energies, leading to a Fano-like line shape for a single Kondo impurity and to an asymmetric double-peak structure surrounding the hybridization gap for a Kondo lattice [14].

III. HYBRIDIZATION AND INTERFERENCE TERMS

Within the renormalized single-particle formulation [13], minimal bulk Hamiltonians for heavy-fermion metals as well as topological insulators involve four bands (i.e., two types of spin-degenerate orbitals), and they can be written in Bloch form,

$$\mathbf{\tau}(\mathbf{k}) = \begin{pmatrix} \epsilon_c(\mathbf{k}) & V_{cf}(\mathbf{k}) \\ V_{fc}(\mathbf{k}) & \epsilon_f(\mathbf{k}) \end{pmatrix},$$

where all individual entries are $2 \times 2$ matrices in spin (or pseudospin) space. Here, $\epsilon$ and $V$ denote kinetic-energy and hybridization terms, respectively, all of them representing interaction-renormalized quantities [13].

Assuming inversion symmetry, we have $\epsilon_c(\mathbf{k}) = \epsilon_c(-\mathbf{k})$ and $\epsilon_f(\mathbf{k}) = \epsilon_f(-\mathbf{k})$, while the hybridization can be even or odd, $V_{cf}(\mathbf{k}) = \pm V_{cf}(\mathbf{k})$. In particular, TKIs with inversion symmetry [24] are characterized by an odd hybridization function, typically arising from conduction-electron orbitals, which are even under inversion ($s$ or $d$), and localized-electron orbitals, which are odd ($f$).

In all cases, the orbital-off-diagonal propagators obey

$$G_{cf}(\mathbf{k}) = G_{cf}^0(\mathbf{k}) V_{cf}(\mathbf{k}) G_f(\mathbf{k}),$$

$$G_{fc}(\mathbf{k}) = G_{fc}^0(\mathbf{k}) V_{fc}(\mathbf{k}) G_c(\mathbf{k}),$$

where $G_{cf}^0(\mathbf{k})$ is the Green’s function for $c$ electrons when $V = 0$, and all propagators are taken at the same fixed frequency $\omega$. Given that $G_{cf}^0$ and $G_f$ are even under inversion, $G_{cf}$ and $G_{fc}$ inherit the inversion eigenvalues of $V_{cf}$ and $V_{fc}$, i.e., odd (even) hybridization implies odd (even) off-diagonal propagators.

The interference term in the tunneling conductance (5) is determined by the local off-diagonal propagator $G_{cf} = k \int G_{cf}(\mathbf{r} = \mathbf{r}')$ where translation invariance has been assumed. For an inversion-symmetric system with odd hybridization, this vanishes:

$$G_{cf} = \int G_{cf}(\mathbf{k})d\mathbf{k} = 0,$$

as a consequence of the integrand being odd in $\mathbf{k}$—this observation is central for the rest of the paper. Obviously $G_{cf} = 0$ implies the absence of the interference term in Eq. (5), and the tunneling line shape needs to be reconsidered. While this analysis strictly applies to a layered, i.e., effectively two-dimensional (2D), system in which the surface layer probed by STS displays bulk properties, it must be modified for three-dimensional (3D) systems: Here, translation and inversion symmetries are broken by the surface, and an effective local $G_{cf} \neq 0$ is created as a consequence, such that the interference term of Eq. (5) reappears. However, its energy dependence is distinct from that in the case of even hybridization.

IV. NUMERICAL EXAMPLES

To confirm and illustrate this reasoning, we have numerically studied a number of 2D and 3D Kondo-lattice models, the latter in a (001) slab configuration, to study the surface tunneling spectrum. In all cases, we work in a single-particle formulation with fixed renormalized parameters (i.e., ignoring self-consistency [13]). This implies that we neglect material-dependent surface effects, i.e., reduced Kondo temperature or Kondo breakdown [29], as well as surface reconstruction [30] and dangling bonds, polar charges, passivation, etc.

The examples include topologically trivial and nontrivial band structures, the latter corresponding to TKIs. Given the noninteracting character of the effective models, different electron concentrations can simply be achieved by tuning the overall chemical potential, and we will explicitly display figures for the Kondo-insulating cases. For simplicity, we work
on square (2D) or cubic (3D) lattices, with kinetic-energy matrices of the form

$$
\epsilon_{c,f}(k) = \left( \begin{array}{c}
\epsilon_{c,f} - 2t_{c,f} \sum_j \cos k_j \end{array} \right) \mathbb{I},
$$

(10)

where \( j = x,y \) in two dimensions and \( j = x,y,z \) in three dimensions. The nearest-neighbor (NN) hopping is taken as \( t_c > 0, t_f < 0 \); in the examples we will use \( t_f/t_c = -0.1 \). Numerical values for \( \epsilon_{c,f} \) and \( V \) are chosen to ensure comparable bandwidths and hybridization gaps in all cases.

### A. 2D model, even hybridization

We start with simple 2D models representative of layered heavy-fermion materials. For the case of even hybridization, we choose a local, spin-independent version,

$$
V_{cf}(k) = V \mathbb{I}
$$

(11)

with \( V < 0 \); we similarly take spin-independent tunneling amplitudes, \( v_c \equiv v_c^\dagger = v_f, v_f^\dagger \equiv v_f \). If the chemical potential is placed inside the hybridization gap, this yields a topologically trivial (or normal) Kondo insulator (NKI). In this case, \( \rho_{cf} = \rho_{f} \) is in general nonzero, peaked where most of the \( f \) states live, i.e., just above and below the gap, and zero in the gap. The sign of \( \rho_{f} \) is related to the fact that below (above) the gap, the (anti)bonding linear combination of \( c \) and \( f \) states is created; in particular, at \( p-h \) symmetry, \( \rho_{cf} \) is odd in \( \omega \): \( \rho_{cf}(-\omega) = -\rho_{cf}(\omega) \). Concrete results are shown in Fig. 2, which illustrates an asymmetric tunneling signal arising from the interference term \( \rho_{cf} \).

### B. 2D model, odd hybridization

To demonstrate the effect of odd hybridization in a planar geometry, we choose a nonlocal, spin-dependent hybridization of the form

$$
V_{cf}(k) = -2i V (\sigma_x k_x + \sigma_y k_y),
$$

(12)

and \( V_{cf}(k) \equiv \{V_{cf}(k)\}^{\dagger} = -V_{cf}(k) \) is anti-Hermitian. This model realizes a 2D TKI. Our specific choice of the relative phase between conduction and localized states (easily generalizable to three dimensions; see below) implies a factor of \( i \) occurring in \( V_{cf} \) (12). This choice also leads to the tunneling between \( f \) orbitals and the tip along \( z \) occurring with amplitudes \( v_f \equiv v_f^\dagger = v_f \), with \( v_f \) being real, while \( v_c \equiv v_c^\dagger = v_c \). The Green’s functions remain diagonal in (pseudo-)spin space, \( \rho^{\uparrow\downarrow} = \rho^{\downarrow\uparrow} = 0 \), and Eq. (5) for the tunneling conductance continues to apply, with \( \rho_c \equiv \rho_c^{\uparrow\downarrow} = \rho_c^{\downarrow\uparrow} = \rho_c \), \( \rho_f \equiv \rho_f^{\uparrow\downarrow} = \rho_f^{\downarrow\uparrow} \), and \( \rho_{cf,f,c} = \rho_{cf,f,c} = -\rho_{cf,f,c} \).

As emphasized above, \( \rho_{cf} \) is strictly zero here, as demonstrated in Eq. (9), while \( \rho_c \) and \( \rho_f \) are not qualitatively different from the even-hybridization case; compare Figs. 2(a) and 3(a). In the case of strong \( p-h \) symmetry, Fig. 3(a), the two peaks below and above the gap are strongly asymmetric. For weakly coupled layers, \( \rho_{cf} \) will be nonzero but very small, such that the main conclusions remain unchanged.

FIG. 2. Numerical results for a 2D NKI with even hybridization (11) at \( p-h \) symmetry, \( \epsilon_c = \epsilon_f \). (a) Imaginary parts of the Green’s functions, \( \rho_c, \rho_f, \) and \( \rho_{cf} = \rho_{f} \). (b) Conductance \( g \) (in arbitrary units) for both signs of \( v_f/v_c \). The hybridization is \( V = 0.011 D_c \), where \( D_c = 8t_c \) is the \( c \)-bandwidth. The vertical dashed lines denote the bulk gap \( \Delta/D_c = 0.012 \), and the small weight inside it is due to finite broadening, \( \delta/D_c = 2.5 \times 10^{-4} \), used in the calculation.

FIG. 3. Same as Fig. 2, but for a 2D TKI with odd hybridization (12) close to \( p-h \) symmetry (exactly at \( p-h \) symmetry the system is metallic). Since \( \rho_{cf} \) is always zero, the line shape here is independent of the sign of \( v_f/v_c \). Parameters are \( \epsilon_c = -\epsilon_f = -0.125 D_c \) and \( V = 0.026 D_c \).
layers. (a) Imaginary part of the Green’s functions, \( \rho_{cf}(z=0) \) and \( \rho_{cf}(z=1) \), and \( \rho_{cf} \) bulk, for different \( \omega/D_c \) when \( \epsilon_c - \epsilon_f = -0.5D_c \).

C. 3D model, even hybridization

For the 3D case, in which STS can probe the surface but not the bulk, we start again with the case of even hybridization,

\[
V_{cf}(\mathbf{k}) = V \mathbf{I} \tag{13}
\]

We assume that the tip only probes the topmost layer, i.e., in a slab calculation that yields \( \rho(z) \) we take \( \rho(z=0) \) when evaluating the tunneling signal according to Eq. (5). As in the 2D case, we have \( v_f = v_f^\uparrow = v_f^\downarrow \) and \( v_c = v_c^\uparrow = v_c^\downarrow \).

The results from the slab calculation with even hybridization, Fig. 4, show that the relevant quantities \( \rho_c, \rho_f, \) and \( \rho_{cf} \) display a very weak dependence on the layer index \( z \); moreover, they are similar to the 2D case, Fig. 2. As a consequence, neglect of surface effects is a reasonable approximation in this case, and a bulk theory is still appropriate to approximately describe the surface. We recall that self-consistency has been neglected: this would take into account that Kondo screening is modified near the surface compared to the bulk, but it would not change our conclusions concerning \( p-h \) asymmetries.

D. 3D model, odd hybridization

We now turn to the case of odd hybridization in three dimensions. The simplest model \([24,31]\) for a TKI in three dimensions is obtained using a hybridization matrix,

\[
V_{cf}(\mathbf{k}) = -2iV(\sigma_z \sin k_x + \sigma_y \sin k_y + \sigma_z \sin k_z), \tag{14}
\]

and \( V_{cf} \equiv [V_{cf}(\mathbf{k})]_0^\downarrow = -V_{cf}(\mathbf{k}) \); we will take \( V < 0 \). The choice of relative phases of Wannier states yields real hybridization terms in real space along the \( z \) direction. As in the 2D case, the tunneling matrix elements involving the STM tip obey \( v_f = v_f^\downarrow = -v_f^\uparrow \) and \( v_c = v_c^\downarrow = v_c^\uparrow \); we stress that our choice of the relative sign of \( v_f^\downarrow \) and \( v_c^\downarrow \) is linked to the form of the hybridization along \( z \) that is proportional to \( \sigma_z \); qualitatively, the tip state resembles a conduction orbital in that it features weak spin-orbit coupling and weak correlations. Upon modeling STS, we restrict our attention to a (001) surface.

The model described by Eqs. (6), (10), and (14) admits different phases depending on the energy difference \( \epsilon_c - \epsilon_f \) \([24,31]\): when \( |\epsilon_c - \epsilon_f| > \delta(|\epsilon_c| + |\epsilon_f|) \), it realizes a
FIG. 6. Same as Fig. 5, but for a weak TKI with odd hybridization (14) and two identical surface Dirac cones at $p\text{-}h$ symmetry, $\epsilon_c = \epsilon_f$; $V = 0.021D_c$. We note that here $\rho_{cf}(z,\omega) = \rho_{cf}(z,-\omega)$, and $\rho_{cf}$ depends strongly on the layer index, being zero in the bulk, showing that a bulk description of the surface is inadequate.

topologically trivial insulator, when $|\epsilon_c - \epsilon_f| < 2(|t_c| + t_f)$, it realizes a weak topological insulator, and otherwise, it realizes a strong topological insulator.

In Fig. 6 we present results in the weak topological phase with two surface Dirac cones at the $p\text{-}h$–symmetric point ($\epsilon_c = \epsilon_f$), and in Fig. 7 we present results in the strong topological phase with one surface Dirac cone away from $p\text{-}h$ symmetry. In both cases, in-gap spectral weight appears due to the presence of topological surface states. We find in general $\rho_{cf}(z,\omega) = \rho_{cf}(z,-\omega) \neq 0$ unless $\rho_{cf}$ is measured deep in the bulk, Figs. 6(c) and 7(c). This may be interpreted as an effective local even-hybridization term that is generated by the presence of the surface. Consequently, an interference term now appears in the tunneling conductance. However, its energy dependence is found to be completely different from the even-hybridization case in Fig. 5. First, it has an appreciable weight in the gap arising from the topological surface states; secondly, it changes sign not in the gap, but for energies corresponding to bulk $f$ states: this happens twice for $\rho_{cf}(z = 0,\omega)$, while $\rho_{cf}(z > 0,\omega)$ has in general more nodes.

FIG. 7. Same as Fig. 5, but for a strong TKI with a single cone whose Dirac energy is in the bulk gap. Parameters are $V = 0.021D_c$ and $\epsilon_c - \epsilon_f = 0.33D_c$; the small wiggles in the energy dependence arise from the finite thickness of the slab ($N = 30$).
FIG. 8. Same as Fig. 5, but for the odd-hybridization model (14) in the topologically trivial phase corresponding to a 3D NKI. In this case, $\rho_{cf}$ is nonzero on the surface, but extremely small when compared to Figs. 6 and 7. Moreover, in-gap surface states are absent. Parameters are $V = 0.021 D_c$ and $\epsilon_c - \epsilon_f = 0.56 D_c$. We note that the apparent steps in panels (a) and (b) arise from the finite size of the slab along $z$, i.e., they represent 2D band edges.

In particular, in the $p$-$h$-symmetric case of Fig. 6, $\rho_{cf}(z, \omega)$ is an even function of energy here, $\rho_{cf}(z, -\omega) = \rho_{cf}(z, \omega)$, while with even hybridization, as remarked, it is odd. Even in the absence of $p$-$h$ symmetry, Fig. 7, the overall behavior of $\rho_{cf}(z, \omega)$ does not change.

We have repeated the calculation in the topologically trivial phase of the model [24]; note that in this case, an insulator would be obtained even for zero hybridization, since the $c$ and $f$ bands do not intersect when $V = 0$. As shown in Fig. 8, we see that, given the same hybridization as in Fig. 7, $\rho_{cf}(z, \omega)$ is much smaller here, and it is zero in the gap due to the absence of surface states. However, $\rho_{cf}(z = 0, \omega)$ changes sign in the $f$ band and not in the gap, in analogy to what happens in the topologically nontrivial phase, and in contrast to the case with even hybridization.

Taking the information from Figs. 6, 7, and 8 together, we can therefore attribute the occurrence of nonzero in-gap weight of $\rho_{cf}(z, \omega)$ to topological surface states, and we speculate that its change of sign in the gap or in the $f$ band is due to even versus odd hybridization.

FIG. 9. Same as Fig. 5, but for a strong TKI with three Dirac cones and parameters $V = 0.031 D_c$, $\epsilon_c - \epsilon_f = 0.167 D_c$, $t'_f/t_f = -0.4$, and $t'_c/t_c = -0.5$. 

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As a final example, we provide results for a system with three Dirac cones, which should mimic SmB₆ [32]. To do this, we modify the kinetic energy by introducing second NN hopping:

\[ \epsilon'_{c,f}(k) = -4t'_{c,f} \sum_{j \neq l} \cos k_j \cos k_l \hat{1}, \]

(15)
in such a way as to have a band inversion at the three X points [32]. Parenthetically, we note that this simplified model has a surface spin structure, in disagreement with experiment [33] due to incorrect mirror Chern numbers [34,35], but this is largely irrelevant for the spin- and momentum-integrated STS spectrum considered here. For this model, results are shown in Fig. 9, where we can observe the same general features that we described for a TKI with one or two cones. However, here one of the cones is inequivalent to the other two, with a different Dirac energy, hence we do not clearly observe \( \rho_{c,f}(z,\omega) \) going to zero at the center of the cones.

V. STS LINE SHAPE

The above discussion has consequences for the energy dependence of the STS spectrum, i.e., the line shape, and the role of the tunneling paths in Kondo systems. In standard models for heavy-fermion materials, the phenomenological parameters \( v_c \) and \( v_f \) affect this line shape: their relative magnitude weights the contributions from \( \rho_{c}, \rho_{f}, \) and \( \rho_{c,f}, \) and their relative sign tells if \( \rho_{c,f} \) enters with a plus or a minus sign [see Eq. (5)], which in turn increases the strength of the peak either at positive or negative energies; see Figs. 2(b) and 5(b). In a TKI, instead, the relative sign enhances or depresses all features related to surface states; see Figs. 6(b) and 7(b).

We note that, if the STM apex atom behaves like a c orbital in the material, we can approximate \( v_f \approx V < v_c \approx -t_c < 0, \) leading to \( \text{sgn}(v_f,v_c) = \text{sgn}(-t_c,V) > 0 \). In the STS signal, this situation enhances both features below the gap in a NKI [Figs. 2(b) and 5(b)], and features from surface states in a TKI [Figs. 6(b) and 7(b)].

When \( \rho_{c,f} \) is small, for example in the case of the NKI with odd hybridization [Fig. 8(b)], or for a TKI in two dimensions [Figs. 3(b) and 4(b)], the STS signal is mostly independent of the sign of \( v_f/v_c, \) and it is simply proportional to the sum \( v_c^2 \rho_c + v_f^2 \rho_f, \) i.e., the interference term can be neglected. We stress that \( \rho_{c,f} = 0 \) does not always imply a symmetric line shape, i.e., strongly \( p-h \)-asymmetric bands can lead alone to an asymmetric line shape [Fig. 4(b)]. Conversely, in the 2D case with odd hybridization, \( p-h \) asymmetry is the only source of an asymmetric line shape (assuming point tunneling).

VI. EXTENSION TO MORE REALISTIC MODELS

In this paper we have employed simple four-band models, while real materials, such as SmB₆, are described by more complicated models [27,36]. We expect, however, that the main results of this paper will remain valid as long as cubic (or tetragonal) symmetry is preserved.

Concerning SmB₆, we remark that existing STS measurements [37,38] find quite generally a Fano line shape close to the Fermi energy. This appears well described [37,38] by existing simplified bulk theories [14,21]—where the asymmetry mainly arises from band-structure effects—except for the residual conductance in the (pseudo)gap, which is due to some other conduction channel. A topological band-structure model, such as ours, naturally assigns this residual conductance to topological surface states (but details are beyond our simplified description).

The tunneling theory used in this paper assumed pointlike tunneling between tip and surface. If the tip is larger, we have to consider the nonlocal Green’s function \( G(r,r') \), which can be nonzero even when \( G(r,r) = 0; \) hence, our approach is only a starting approximation of the phenomenon. As a general rule, in the presence of translational symmetry, \( G_{r'}(r-r') \) will have a node when \( (r-r') = 0 \), in contrast to the even-hybridization case. In Fig. 10 we show how \( \rho_{c,f} \) depends on \( (r-r') \) in two dimensions, with either even or odd hybridization.

Finally, we note that a fully accurate description of the tunneling signal requires the explicit use of the spatial shape of the Wannier functions [39]. However, this implies more complicated numerical work, which is beyond the scope of this paper.

VII. CONCLUSIONS

For heavy-fermion systems with bulk inversion symmetry, we have argued that a hybridization term that is odd under...
inversion leads to the vanishing of the local nondiagonal term $G_{ef}$ of the Green’s function. We have shown that this strongly modifies considerations concerning the spectral line shape as measured in STS experiments, because the cotunneling interference term usually made responsible for the appearance of a Fano-like line shape is either absent or very different from that in the even-hybridization case. Sharp conclusions can be drawn for $p$–$h$–symmetric bands, where even hybridization generically leads to a $p$–$h$–asymmetric STS signal, its asymmetry being entirely due to $G_{ef}$, and odd hybridization to a strictly $p$–$h$–symmetric line shape. In a general $p$–$h$–asymmetric situation, an asymmetric STS line shape can arise from both band asymmetries and tunneling interference, and additional information (e.g., from angle-resolved photoemission spectroscopy or band-structure calculations) is required to deduce the properties of tunneling paths or hybridizations from STS data.

We have provided concrete examples for tunneling spectra in simple models of topological and nontopological Kondo insulators, which we hope will be useful for the interpretation of future tunneling experiments. We recall, however, that a measurement of the local DOS alone cannot distinguish topological from nontopological states, whereas a QHE experiment can do so by detecting the spin-momentum locking of surface states.

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