Resistive anisotropy due to spin-fluctuation scattering in the nematic phase of iron pnictides

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The large in-plane anisotropy of the resistivity is a hallmark of the nematic state of the iron pnictides. Solving the Boltzmann transport equation, we show that the prominent doping dependence as well as the large values of the anisotropy can be well explained by momentum-dependent spin-fluctuation scattering without assuming anisotropic impurity states. Due to the forward-scattering corrections, the hot spots contribute to the resistive anisotropy even in the case of strong spin fluctuations, which makes large values of the anisotropy possible. The ellipticity of the electron pockets plays an important role in explaining the dominance of positive values of the anisotropy, i.e., larger resistivity in the direction with weaker spin fluctuations, throughout the doping range.

Introduction. Currently, one of the most intensively discussed topics in the field of high-$T_c$ superconductivity is the origin of the nematic phase of the iron pnictides [1,2]. The nematic phase transition occurs at temperatures $T_n$ above or coinciding with the magnetic ordering temperature $T_N$, at which a stripe antiferromagnetic state with ordering vector $Q=(\pi,0)$ (defining the $x$ direction in this work) is established. The nematic phase found for $T_N < T < T_c$ is characterized by a broken rotational symmetry between the $x$ and $y$ directions in the absence of magnetic order. Although one of its most obvious manifestations is the orthorhombic distortion of the lattice, it is generally considered that the nematic state arises from electronic correlations [3]. However, the precise mechanism is still under debate [4–8].

Another key experimental signature of the nematic phase is the pronounced difference between the resistivities along the $x$ and $y$ directions, $\Delta\rho \equiv (\rho_y - \rho_x)/\rho_x$ [3,9–12]. Understanding the origin of the resistive anisotropy should offer crucial insights into the origin of the nematicity. Two scenarios are debated: (i) the scattering off anisotropic impurity states [9,13–16] and (ii) the scattering off fluctuating collective excitations with spectrum reflecting the underlying nematicity [11,17].

The existing description of the resistive anisotropy due to spin fluctuations [17], i.e., within scenario (ii), is restricted to the limit of weak spin-fluctuation scattering compared to isotropic impurity scattering, although the former is likely stronger than the latter, except at very low temperatures when the spin fluctuations are frozen out [18–22]. Naturally, this limit is only compatible with small values of $\Delta\rho$, since the dominant impurity part leads to isotropic resistivity. Though in disagreement with the huge positive anisotropy up to $\Delta\rho \approx 0.5$ observed in experiments on electron-doped samples [3,9], the theory correctly predicts negative $\Delta\rho$ for hole-doped samples [11].

Within scenario (i), the much larger $\Delta\rho$ in electron-doped Ba(Fe$_{1-x}$Co$_x$)$_2$As$_2$ [3] compared to hole-doped Ba$_{1-x}$K$_x$Fe$_2$As$_2$ [11,12] is explained as a consequence of the stronger scattering off Co dopants placed within the iron plane [9,13,16]. The observed anisotropic impurity states are all elongated in the $x$ direction, hence giving a larger scattering cross section in the $y$ direction [13]. The negative $\Delta\rho$ measured for hole-doped samples then arises due to details of the band structure [16]. The dependence of $\Delta\rho$ on the degree of disorder is controversial: some experiments show, in agreement with scenario (i), a reduction of $\Delta\rho$ upon sample annealing, which is supposed to lower the degree of disorder [9], while others report a much weaker disorder dependence [10].

In this work, we consider scenario (ii) with spin-fluctuation scattering of arbitrary strength. For spin-fluctuation and isotropic impurity scattering of comparable strength, we reproduce both the small negative $\Delta\rho$ for hole-doped samples and the large positive $\Delta\rho$ in electron-doped samples. We also show that the reduction of $\Delta\rho$ in electron-doped samples upon annealing is consistent with the spin-fluctuation scenario. In a nutshell, our results follow from the role of the spin-fluctuation scattering strength in controlling the size of the Fermi-surface segments that contribute to the resistive anisotropy.

Model and method. We describe the band structure by an effective two-dimensional model [5,11,17,22,23] with a nearly circular hole Fermi pocket at the center of the Brillouin zone and two elliptical electron pockets $eX$ and $eY$ displaced by $Q_X = (\pi,0)$ and $Q_Y = (0,\pi)$, respectively, where length is measured in units of the iron-iron separation. We use the same dispersions as in Ref. [23] and fix the ellipticity of the electron pockets by choosing $\xi_e = 2$. The Fermi pockets are sketched in Fig. 1. The sizes of the pockets depend on the doping level, which is controlled by the electron filling $n$ [22]. The validity of the minimal model for the case of 122 pnictides has been discussed in the supplementary information for Ref. [11].

To focus on the impact of the spin-fluctuation scattering, in the following we neglect the distortion of the Fermi pockets due to the splitting of the iron $d_{xy}$ and $d_{xz}$ orbital levels [24,25]. In the Supplemental Material [26] we show that this splitting gives rise to an additional resistive anisotropy. By itself, this shows poor agreement with experiment, however, and the effect of nematicity in the spin-fluctuation scattering is the dominant mechanism over a large parameter range.

We assume transport to be dominated by scattering off spin fluctuations and isotropic impurities. The spin-fluctuation scattering amplitude is determined by the imaginary part of the spin susceptibility. We use a phenomenological model for the susceptibility in the nematic phase that has been employed

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Following Ref. [22], we introduce a total elastic scattering rate on each Fermi surface are parametrized by the angle anisotropy, depending on the direction of the Fermi velocity. States discussed in the main text, the electron pockets can be divided into pocket index \( p \), leading to stronger scattering between the hole pocket and the electron pocket \( (s, \theta) \) of the hot spots depends on the doping level [22,23]. In the nematic phase, scattering between the hole pockets of the two-band model. In the nematic phase, scattering is peaked at the nesting vector \( Q \) and \( \mathbf{Q} \) for all dopings, consistent with the observed stability of commensurate antiferromagnetic order against doping. The resulting scattering rate is therefore large for scattering wave vectors close to \( \mathbf{Q}_X \) or \( \mathbf{Q}_Y \). The strongest scattering is found at the “hot spots,” i.e., the points on the Fermi pockets connected by the nesting vectors. The position of the hot spots depends on the doping level [22,23]. In the nematic phase a finite order parameter \( \phi > 0 \) breaks the \( C_4 \) symmetry. This enhances the peak at \( \mathbf{Q}_X \) in the susceptibility, leading to stronger scattering between the hole pocket \( h \) and the electron pocket \( eX \) than between the pockets \( h \) and \( eY \), as indicated in Fig. 1.

We focus on the dependence of the resistive anisotropy on doping (electron filling \( n \)) and on the relative strengths of spin-fluctuation and impurity scattering (controlled by \( W_{sf}/W_{imp} \)). The explicit temperature \( T \) in Eq. (1) controls the energy available for spin excitations and thus additionally affects the strength of spin-fluctuation scattering. In the relevant limit \( k_B T \ll \omega_q \), this leads to the familiar \( T^2 \) dependence. Since the nematic phase appears in a narrow temperature interval above the Néel temperature \( T_N(n) \), we choose the temperature \( T(n) = T_N(n) = T_0(1 - (n - 2.09)/0.21)^2 \) with \( T_0 = \max[T_N(n)] = 137 \) K. This mimics the situation in 122 pnictides, where the magnetic order is suppressed upon doping the parent compound, here taken to correspond to \( n = 2.09 \) [23]. Our results are qualitatively insensitive to the specific form of \( T(n) \). Since the temperature tracks \( T_N(n) \), it is reasonable to keep the parameters \( \xi, \phi \), and \( \Gamma \) fixed; we have checked that the qualitative behavior does not depend on their precise values.

We employ the nonequilibrium Green’s function formalism [29] in the Boltzmann approximation, where the linear-response distribution function at the Fermi energy is determined by the vector mean free paths \( \Lambda_i \) [30,31] of the states \( |s, \theta\rangle \). The vector mean free path obeys the kinetic equation [22]

\[
\Lambda_{s\theta} = \tau_{s\theta} \mathbf{v}_{s\theta} + \tau_{s\theta} \sum_x \int \frac{d\theta'}{2\pi} N_{x\theta'} W_{s\theta'}^{x\theta'} \Lambda_{x\theta'},
\]

where \( \mathbf{v}_{s\theta} \equiv \hbar^{-1} \mathbf{v}_{k_{s\theta}(k)} \) is the velocity, \( N_{s\theta} = |d\mathbf{k}_{s\theta}/d\theta|/\pi \hbar |\mathbf{v}_{s\theta}| \) is the density of states, and

\[
\tau_{s\theta} = \left( \frac{1}{2\pi} \sum_x \int d\theta' N_{x\theta'} W_{s\theta'}^{x\theta'} \right)^{-1}
\]

is the lifetime of the state \( |s, \theta\rangle \). The first term on the right-hand side of Eq. (2) represents the relaxation-time approximation, while the second incorporates the forward-scattering corrections.

The resistivity \( \rho_i \) in the direction \( i = x, y \) is determined by the vector mean free path,

\[
\rho_i = \sum_s \int \frac{d\theta}{2\pi} \sigma_i^{s\theta} \Lambda_{s\theta}^{-1} \equiv \left( \sum_s \int \frac{d\theta}{2\pi} \sigma_i^{s\theta} \right)^{-1},
\]

where \( \sigma_i^{s\theta} \) is the contribution of the state \( |s, \theta\rangle \) to the total conductivity \( \sigma^i = \sum_s \int \frac{d\theta}{2\pi} \sigma_i^{s\theta} \). It is useful to resolve the resistive anisotropy in terms of band and angular contributions,

\[
\Delta \rho = \int \frac{d\theta}{2\pi} (\Delta \rho_{\theta\theta} + \Delta \rho_{\phi\phi}),
\]

where the contributions from hole and electron pockets read, respectively,

\[
\Delta \rho_{\theta\theta} = \frac{1}{2\sigma^y} \left( \sigma_{h,\theta}^y - \sigma_{h,\phi}^y + \sigma_{h,\theta+\pi/2}^y - \sigma_{h,\phi+\pi/2}^y \right),
\]

\[
\Delta \rho_{\phi\phi} = \frac{1}{\sigma^x} \left( \sigma_{eX,\theta}^x - \sigma_{eY,\phi}^x + \sigma_{eX,\theta+\pi/2}^x - \sigma_{eY,\phi+\pi/2}^x \right).
\]
In Eq. (6), we consider the contributions from the hole-pocket states \(|h, \theta\rangle\) and \(|h, \theta + \pi/2\rangle\) together, since only the joint contribution vanishes in the normal, \(C_4\)-symmetric phase. For the same reason, the states \(|eY, \theta\rangle\) and \(|eX, \theta + \pi/2\rangle\) are considered together in Eq. (7). According to the definition of \(\Delta \rho_{\theta \phi}\), the contributions from states close to the minor axis of the elliptical electron pockets are found at \(\theta \approx 0\), while the contributions from states close to the major axis are found at \(\theta \approx \pi/2\).

**Results.** Figure 2 summarizes the results for the resistive anisotropy obtained by solving Eq. (2) numerically \([22]\). In Fig. 2(a) the resistive anisotropy is plotted as a function of doping and the ratio \(W_{sf}/W_{imp}\), while in Fig. 2(b) the doping dependence is illustrated for three characteristic values of \(W_{sf}/W_{imp}\). The contributions \(\Delta \rho_{\theta \phi}\) from the electron pockets are found to dominate the anisotropy, for which reason only these contributions are shown in Fig. 2(c). As evident from Fig. 2(c) and illustrated in Fig. 1, the electron pockets can be divided into positively and negatively contributing parts, with the crossover located roughly where the Fermi velocity points in the diagonal direction; the parts close to the minor axis of the electron pockets contribute with positive sign, while the parts close to the major axis contribute with negative sign. This is because the conductivity of the electron pocket \(eY\) is larger than that of \(eX\) due to the stronger scattering for the latter.

The total resistive anisotropy in Figs. 2(a) and 2(b) shows a strong doping dependence, which changes qualitatively with \(W_{sf}/W_{imp}\). The angle-resolved plots in Fig. 2(c) show that for increasing \(W_{sf}/W_{imp}\) the contributing regions of the electron pockets expand. This is schematically illustrated in Fig. 3. For small \(W_{sf}/W_{imp}\), the resistive anisotropy is dominated by regions close to the hot spots, whereas the “cold” regions, where spin-fluctuation scattering is weaker, give small contributions. Since the electron pockets have negatively and positively contributing parts, the position of the hot spots determines the sign of the resistive anisotropy. The negative (positive) extremum is found for the filling \(n \approx 2.02\) \((n \approx 2.17)\), for which the hot spots lie on the major (minor) axis of the electron pockets. The difference between the positive and negative extrema is due to different velocities and densities of states at the major and minor axes.

In the impurity-dominated limit, \(W_{sf}/W_{imp} \ll 1\), the anisotropy is very small as impurity scattering is isotropic. With increasing \(W_{sf}/W_{imp}\), the contributing regions of the electron pockets expand and the extrema of \(\Delta \rho\) grow, until the active region starts to include parts contributing with

**FIG. 2.** (Color online) (a) Resistive anisotropy as a function of doping (parametrized by \(n\)) and the relative strengths of spin-fluctuation and impurity scattering. (b) Resistive anisotropy as a function of doping for \(W_{sf}/W_{imp} = 0.1, 1, \) and 10. (c) Angle-resolved contributions of the electron pockets to the resistive anisotropy as defined in Eq. (7). While for \(W_{sf}/W_{imp} = 0.1\) only regions close to the hot spots (indicated by arrows) contribute, for increasing \(W_{sf}/W_{imp}\) the contributing regions grow. (d) Ratio of averaged resistivities at the temperatures \(T(n)\) considered in (a)–(c) and at \(T = 0\) K. We choose the parameters \(\eta = 0.5, \Gamma = 350\) meV, \(\xi^{-2} = 0.027\), and \(\phi = 0.017\).

**FIG. 3.** (Color online) Increasing strength of spin-fluctuation scattering extends the contributing regions of the electron pockets. Two characteristic filling levels are considered, \(n \approx 2.02\) and \(n \approx 2.17\), with hot spots at the major and the minor axis of the electron pockets, respectively.
the opposite sign. Upon further expansion, the positive and negative contributions begin to partially compensate each other. Since the negatively contributing regions are smaller, the negative extremum of $\Delta \rho$ is suppressed at a smaller ratio $W_{sf}/W_{imp}$ than the positive extremum. At $W_{sf}/W_{imp} \approx 1$ this results in a strong doping asymmetry with small negative values on the hole-doped side and large positive values on the electron-doped side.

We emphasize that the result that the hot spots contribute to $\Delta \rho$ even for dominant spin-fluctuation scattering, as sketched in Fig. 3, is not obvious. Since in this limit the scattering at the hot spots is much stronger than in the cold regions, one would naively expect the hot spots to be short circuited by the cold regions [32], i.e., to be irrelevant for the transport, in which case $\Delta \rho$ would be significantly small [11,17]. However, as we have shown for the $C_4$-symmetric state of the pnictides [22], the short-circuiting is compensated by enhanced forward-scattering corrections.

To compare the results to measurements, we have to identify the relevant range of $W_{sf}/W_{imp}$. In Fig. 2(d), we plot the calculated ratio of the averaged resistivity $\rho(T) = (\rho_{+} + \rho_{-})/2$ at $T = T(n)$ and at $T = 0$ K, where the spin excitations are frozen out and the resistivity is due to impurity scattering alone, which we assume to be temperature independent. Ignoring for the moment that the system is antiferromagnetic at $T = 0$ K, we observe that for $W_{sf}/W_{imp} = 1$ and $W_{sf}/W_{imp} = 10$ the resistivity ratios are comparable to those measured for as-grown and annealed samples, respectively [9]. The reduction of the density of states in the antiferromagnetic phase should increase the $T = 0$ K resistivity, however, and so our argument likely underestimates $W_{sf}/W_{imp}$.

For $W_{sf}/W_{imp} = 1$, Figs. 2(a) and 2(b) show a large positive peak with $\Delta \rho \approx 0.4$ in electron-doped samples and a small negative peak with $\Delta \rho \approx -0.01$ in hole-doped samples. This is in good agreement with experimental observations [3,9,11]. The results also show that in electron-doped samples an increase of $W_{sf}/W_{imp}$ beyond about 1 leads to a reduction of the peak value of $\Delta \rho$. A reduction of $\Delta \rho$ upon annealing was indeed observed in electron-doped Ba(Fe$_{1-x}$Co$_x$)$_2$As$_2$ [9], where this effect has been taken as strong evidence that the resistive anisotropy mainly stems from scattering at anisotropic impurity states. Our results show, however, that such a reduction is also consistent with anisotropic spin-fluctuation scattering. For the hole-doped samples, we predict an increase in $\Delta \rho$ with annealing if $W_{sf}/W_{imp} \gtrsim 1$, see Figs. 2(a) and 2(b), which to our knowledge has not been measured so far.

In the Supplemental Material [26], we show that anisotropy due to orbital splitting adds nearly additively to $\Delta \rho$, indicating the robustness of the results against band details. This is in line with the fact that the main features of $\Delta \rho$ are explained by a mechanism that does not rely on the details of the model.

Summary. We have studied the resistive anisotropy in the nematic state of iron pnictides. We have considered a two-band model and assumed scattering to be dominated by spin fluctuations and isotropic impurities. The inclusion of forward-scattering corrections is crucial for the correct description [22]. The obtained resistive anisotropy $\Delta \rho$ shows good agreement with experimental results for annealed and as-grown samples. In particular, we have shown that the twin puzzles of the doping asymmetry of $\Delta \rho$ and the reduction of $\Delta \rho$ upon annealing can be explained within the spin-fluctuation scenario. The qualitative behavior is governed by the contributing regions on the elliptical electron pockets, in particular their growth with increasing spin-fluctuation strength. Importantly, the hot spots contribute to $\Delta \rho$ even for strong spin-fluctuation scattering, contrary to what was thought previously. Since spin fluctuations are particularly strong at the hot spots, this naturally leads to large anisotropies.

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