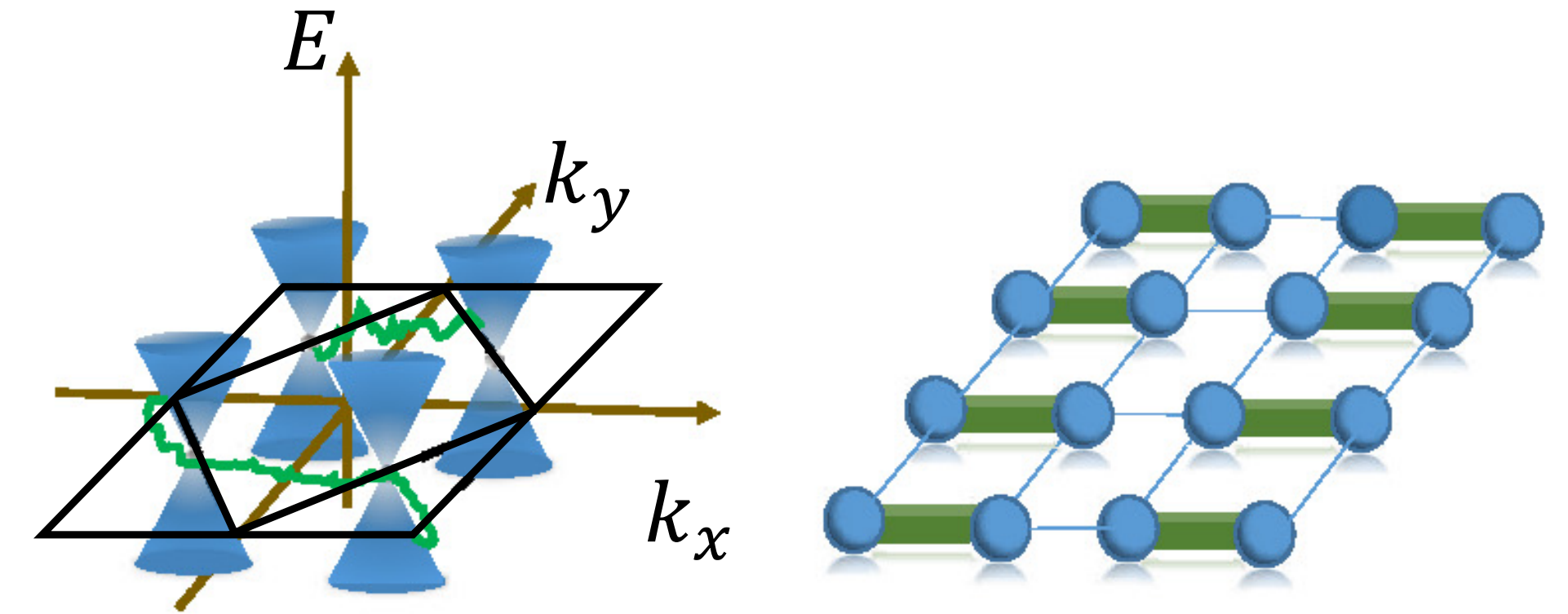
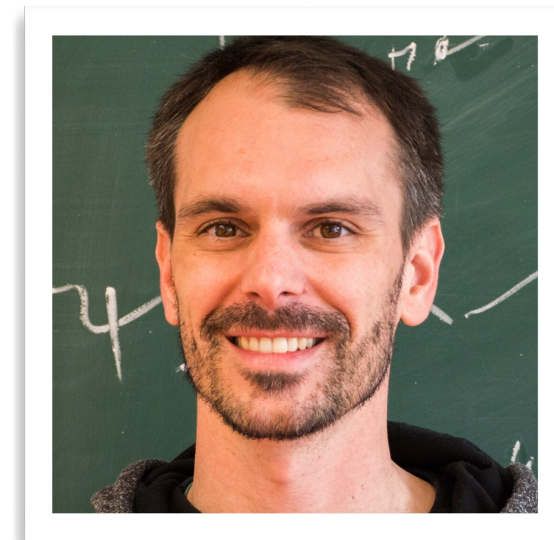


# Confinement transition in the QED<sub>3</sub>-Gross-Neveu-XY universality class

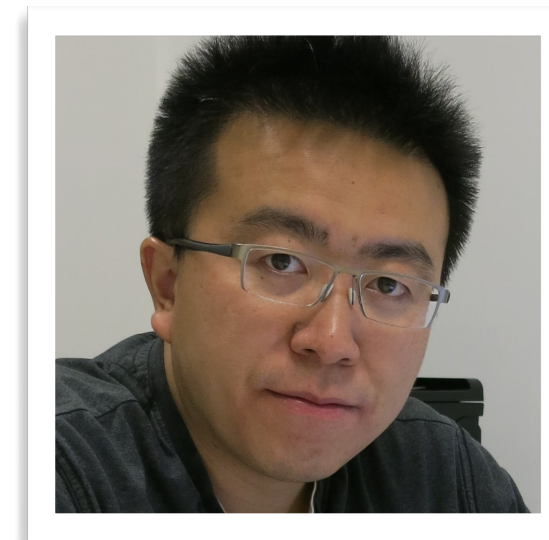
Lukas Janssen  
(TU Dresden)



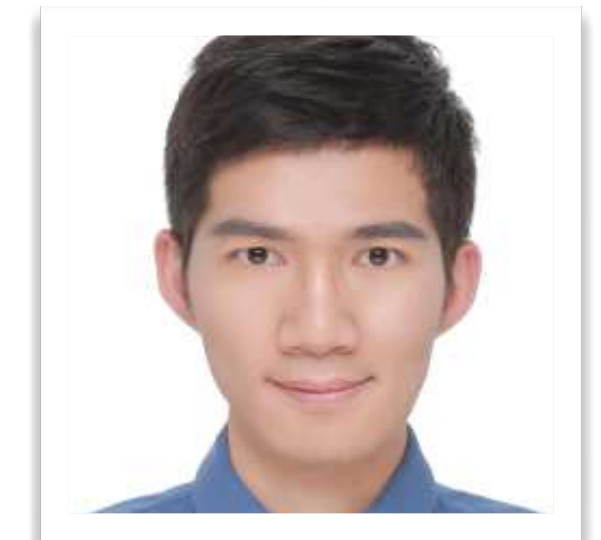
W. Wang  
(IOP Beijing)



M. M. Scherer  
(U Cologne)



Z. Y. Meng  
(U Hong Kong)

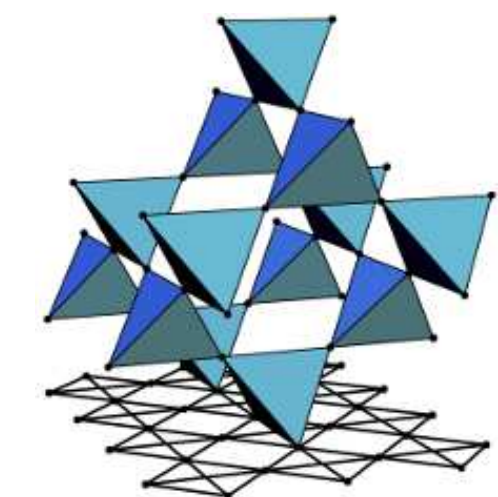


X. Y. Xu  
(UC San Diego)



**ct.qmat**  
Complexity and Topology  
in Quantum Matter

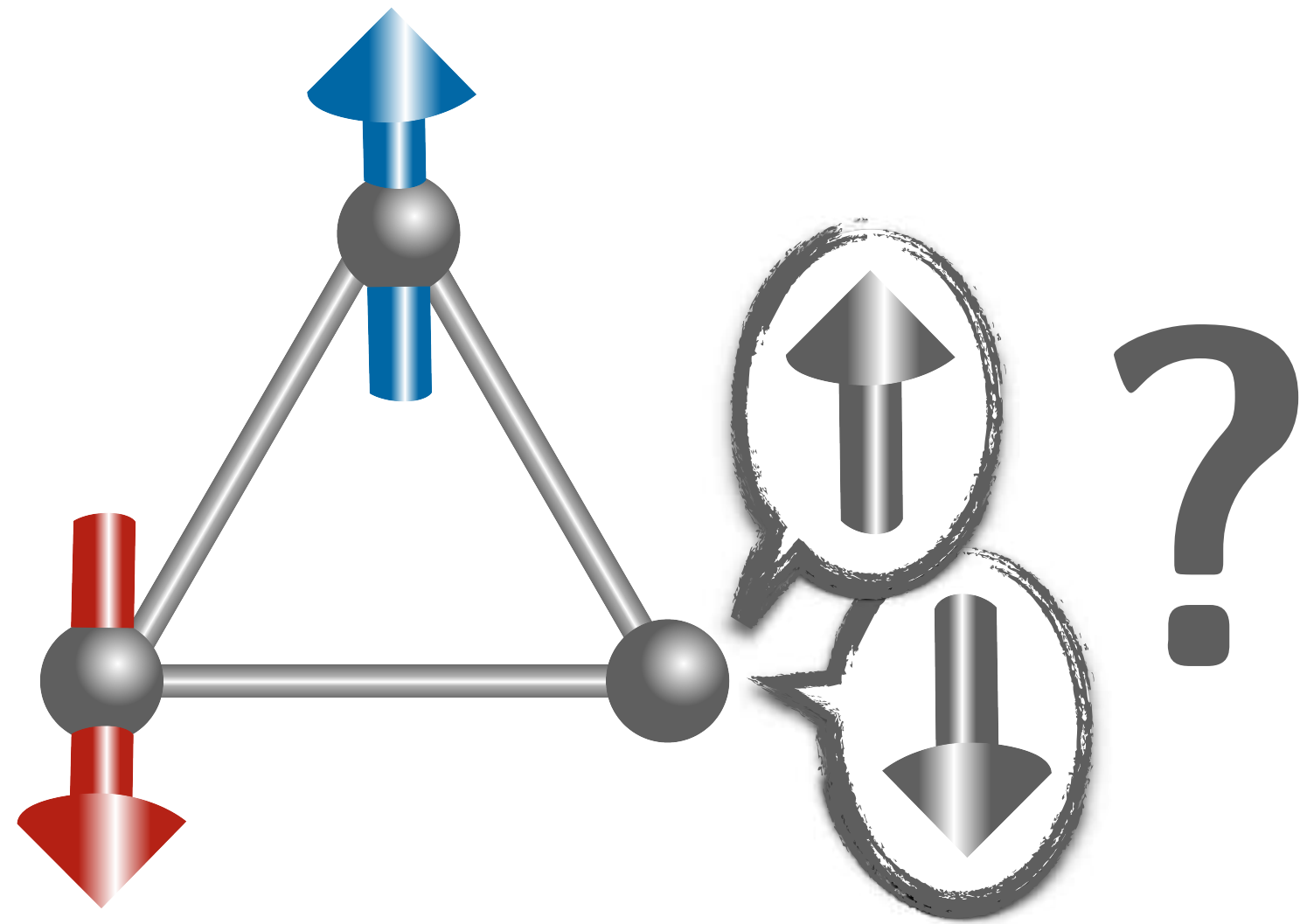
Würzburg-Dresden Cluster of Excellence



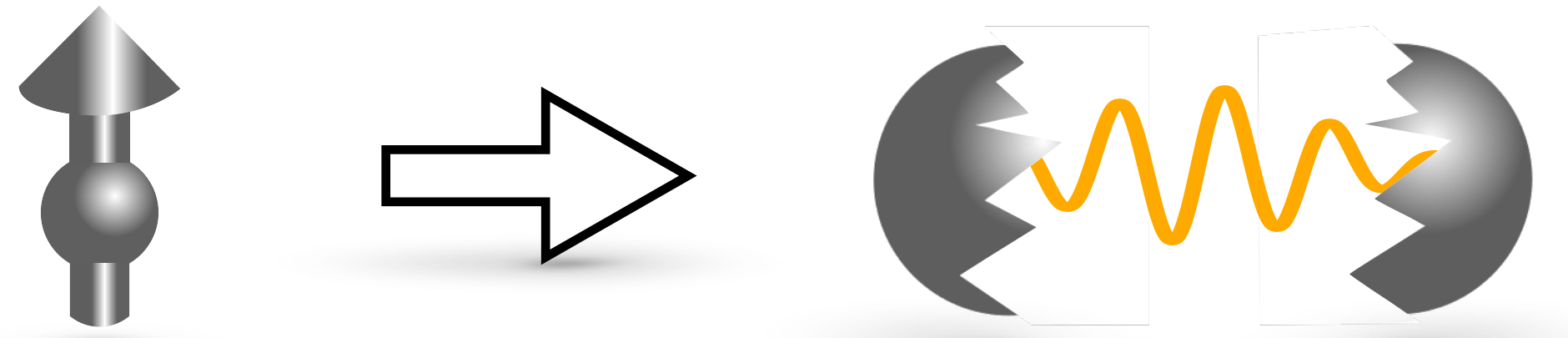
SFB 1143

# Introduction: Quantum spin liquids

Frustration:

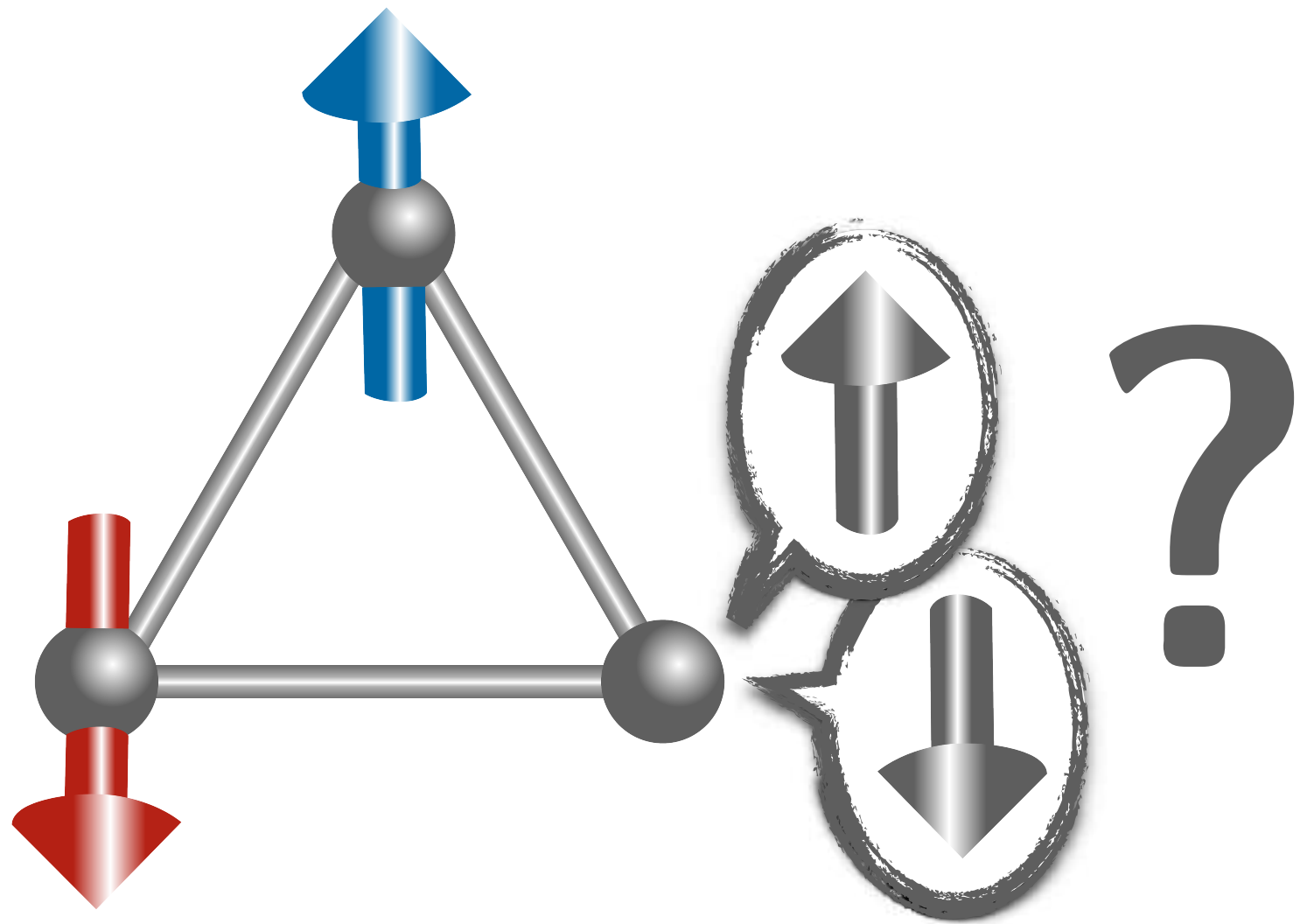


Fractionalization:

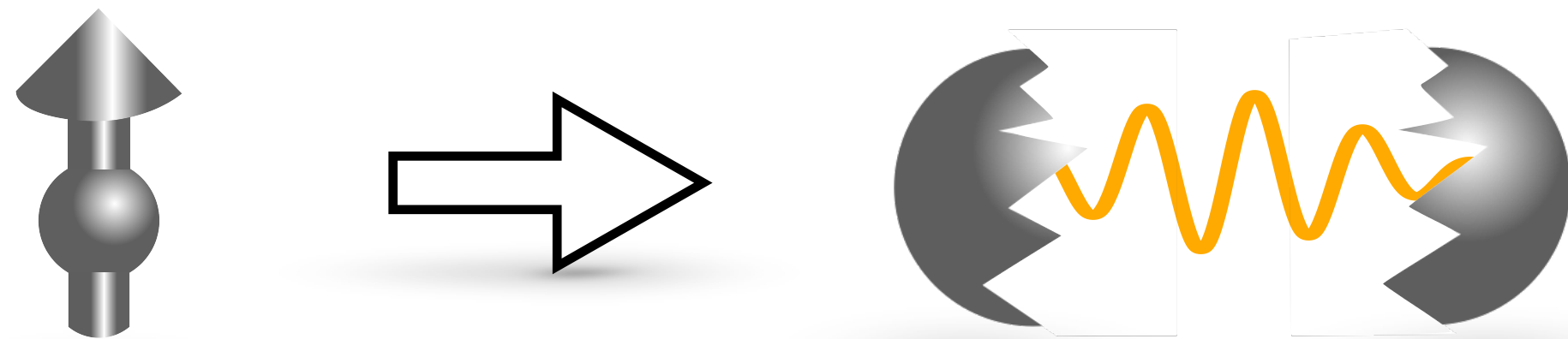


# Introduction: Quantum spin liquids

Frustration:



Fractionalization:



$\mathbb{Z}_2$  spin liquid:

Kitaev honeycomb model  
Toric code  
...

[Kitaev, Ann. Phys. '06]  
[Kitaev, Ann. Phys. '03]

→ Talk by Shouryya Ray (X44.00004)

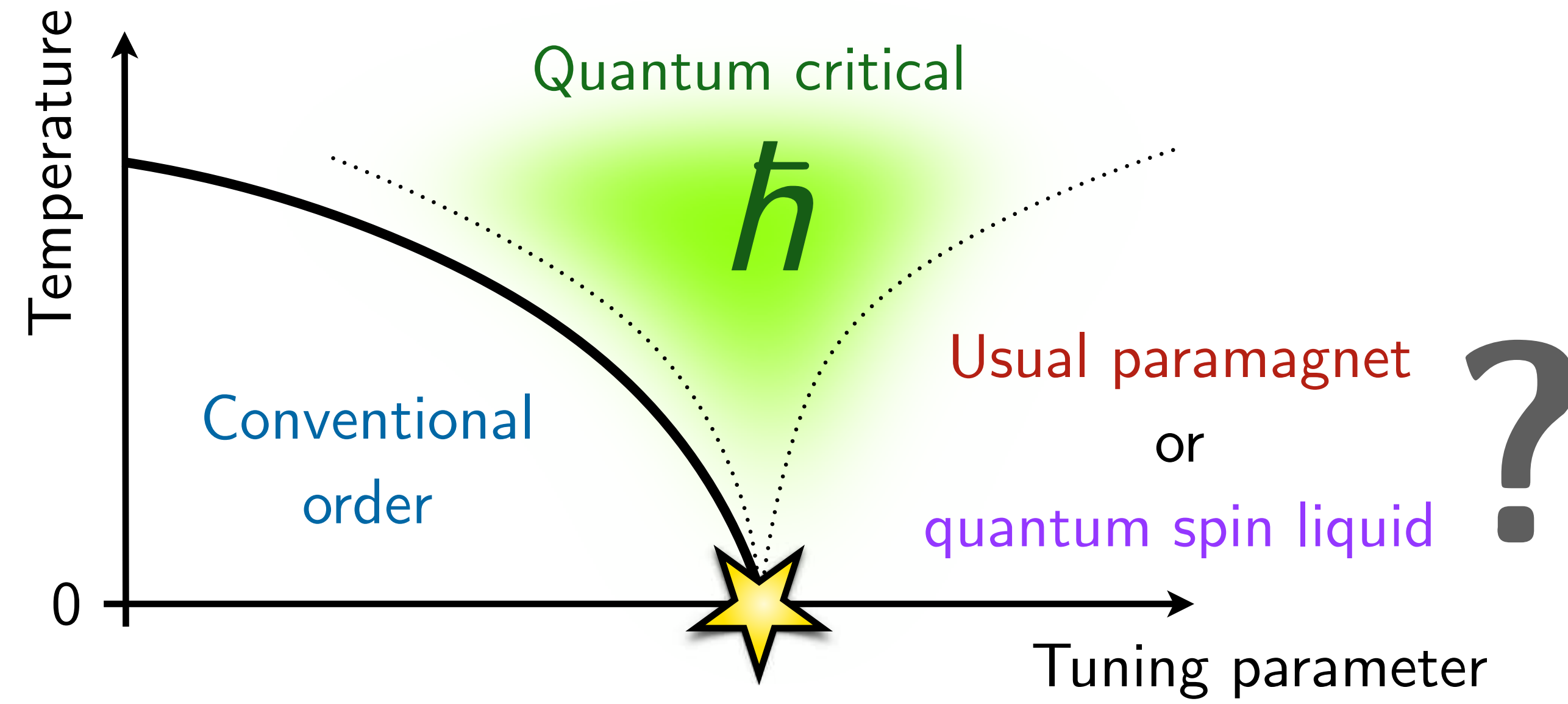
U(1) spin liquid:

Kagome model?  
Triangular model?  
...

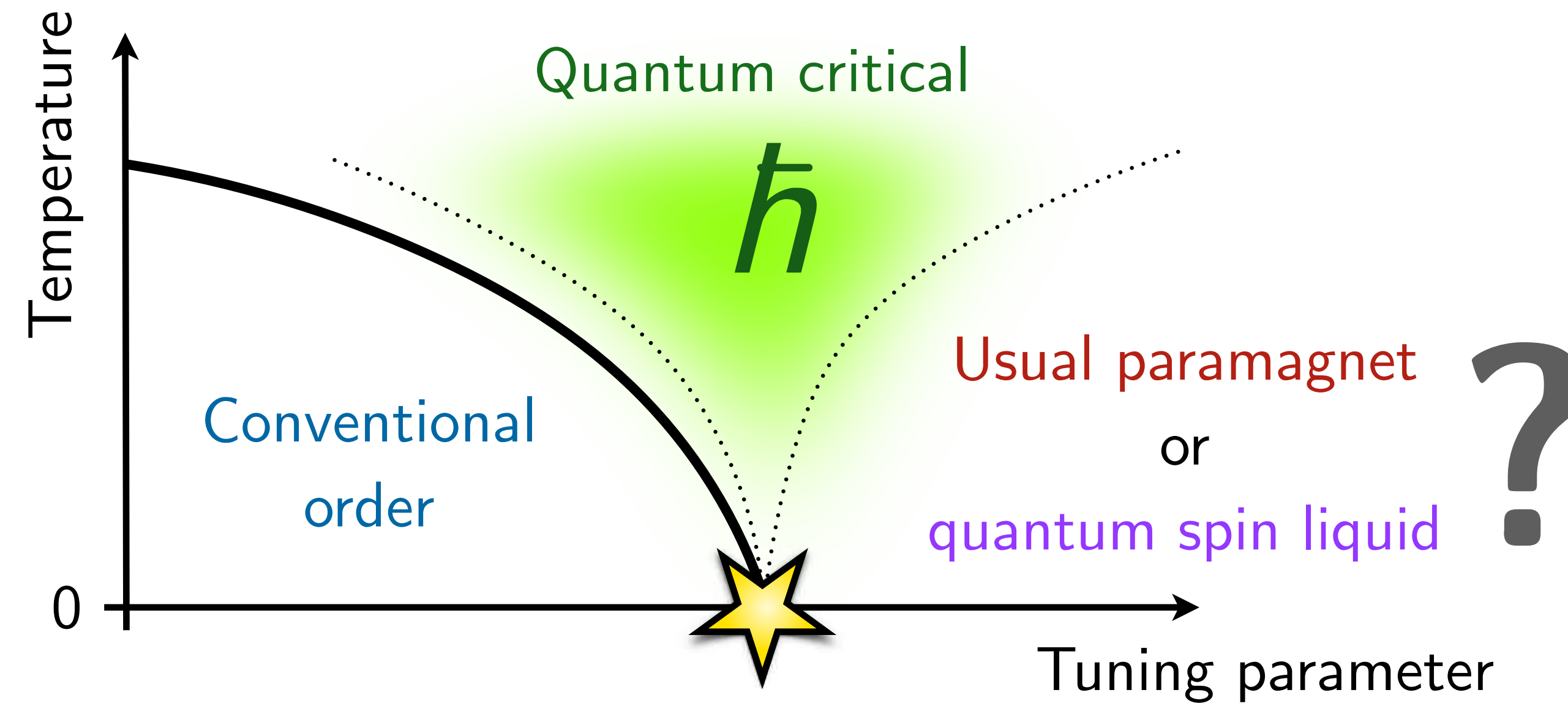
[He *et al*, PRX '17]  
[Hu *et al.*, PRL '19]

→ This talk

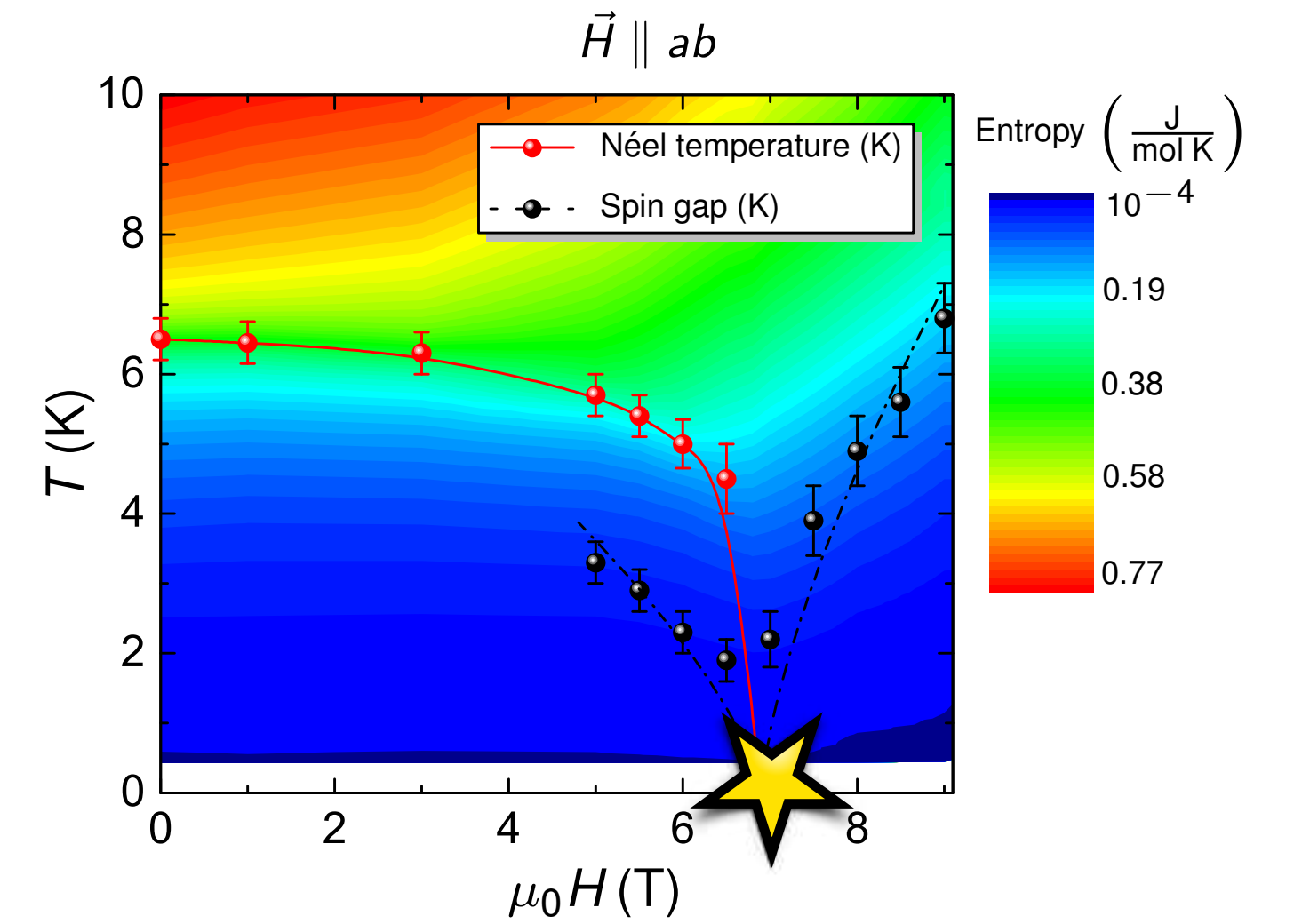
# Motivation: Spin-liquid criticality



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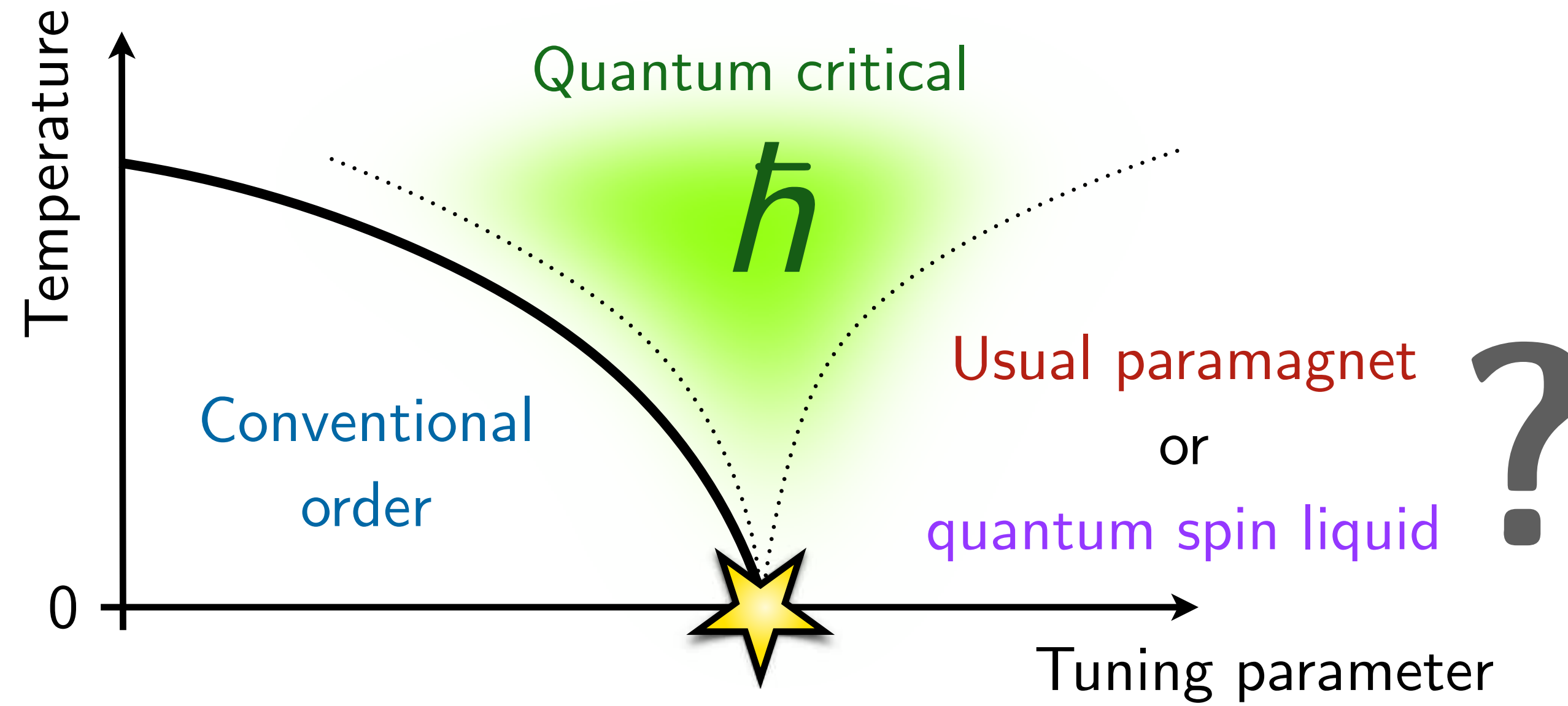


## Example: $\alpha$ -RuCl<sub>3</sub> in field

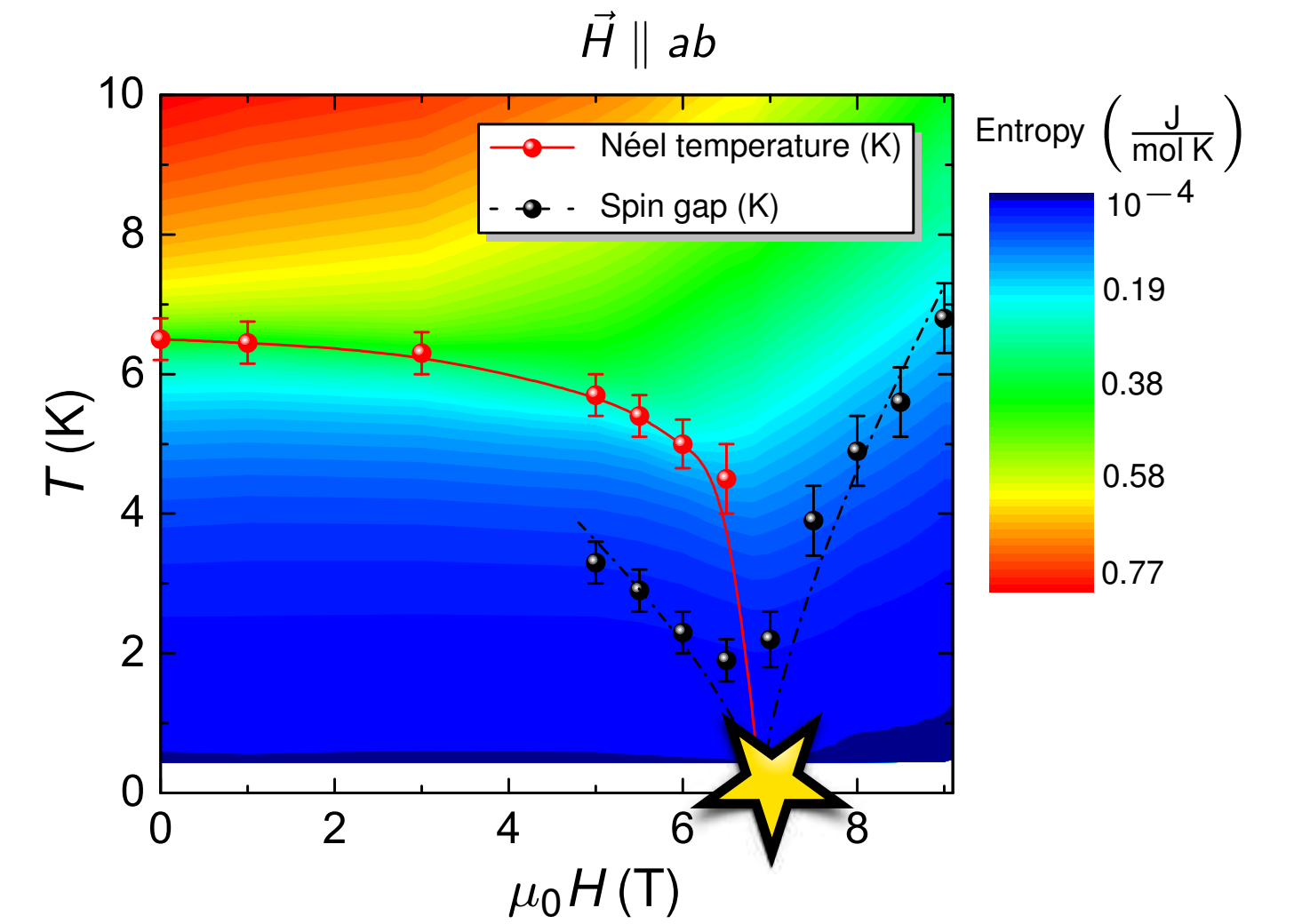


[Wolter, Corredor, LJ, *et al.*, PRB '17]

# Motivation: Spin-liquid criticality



## Example: $\alpha$ -RuCl<sub>3</sub> in field



[Wolter, Corredor, LJ, et al., PRB '17]

## Main question:

How do fractionalized excitations affect quantum criticality?

# Model: Lattice compact QED<sub>3</sub>

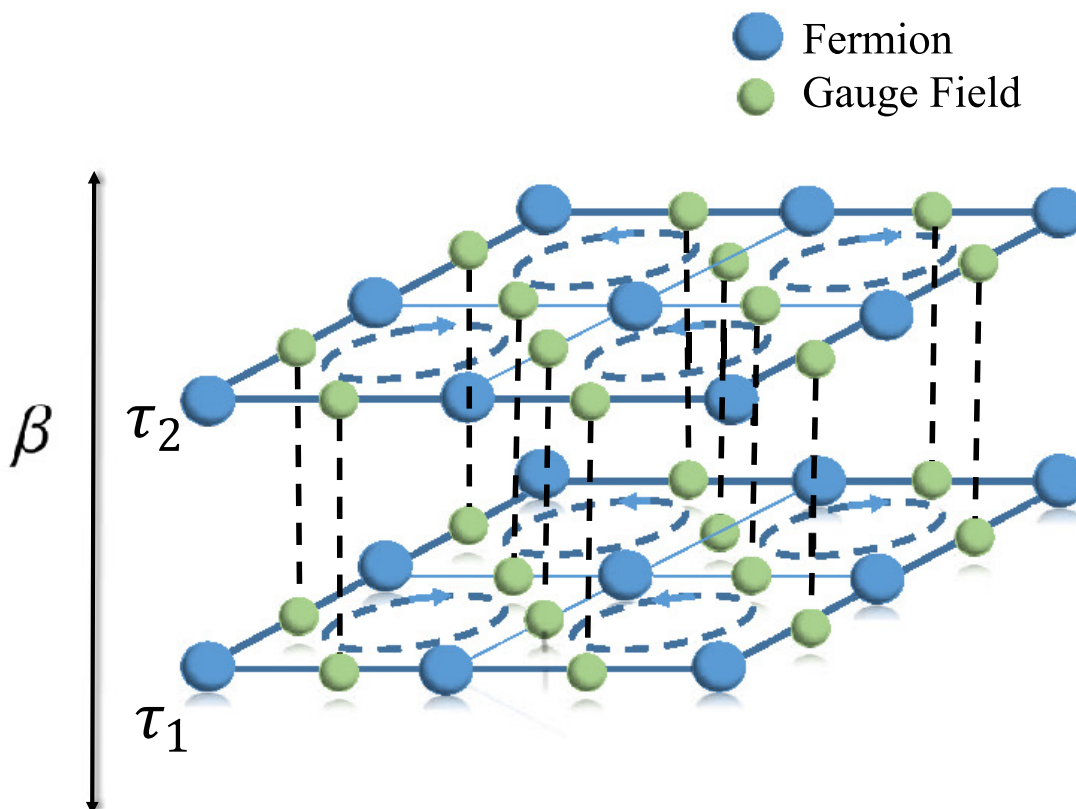
Action (square lattice):

$$S = \int_0^\beta d\tau \left[ \sum_{\langle ij \rangle, \alpha} \psi_{i\alpha}^\dagger (\partial_\tau \delta_{ij} - t e^{i\varphi_{ij}}) \psi_{j\alpha} + \text{H.c.} \right. \\
 \left. + \frac{4}{JN_f} \sum_{\langle ij \rangle} \frac{1 - \cos[\varphi_{ij}(\tau + 1) - \varphi_{ij}(\tau)]}{\Delta\tau^2} + \frac{KN_f}{2} \sum_{\square} \cos(\text{curl } \varphi) \right]$$

Compact U(1) gauge field

Fermions

... favors  $\pi$  flux for  $K > 0$



# Model: Lattice compact QED<sub>3</sub>

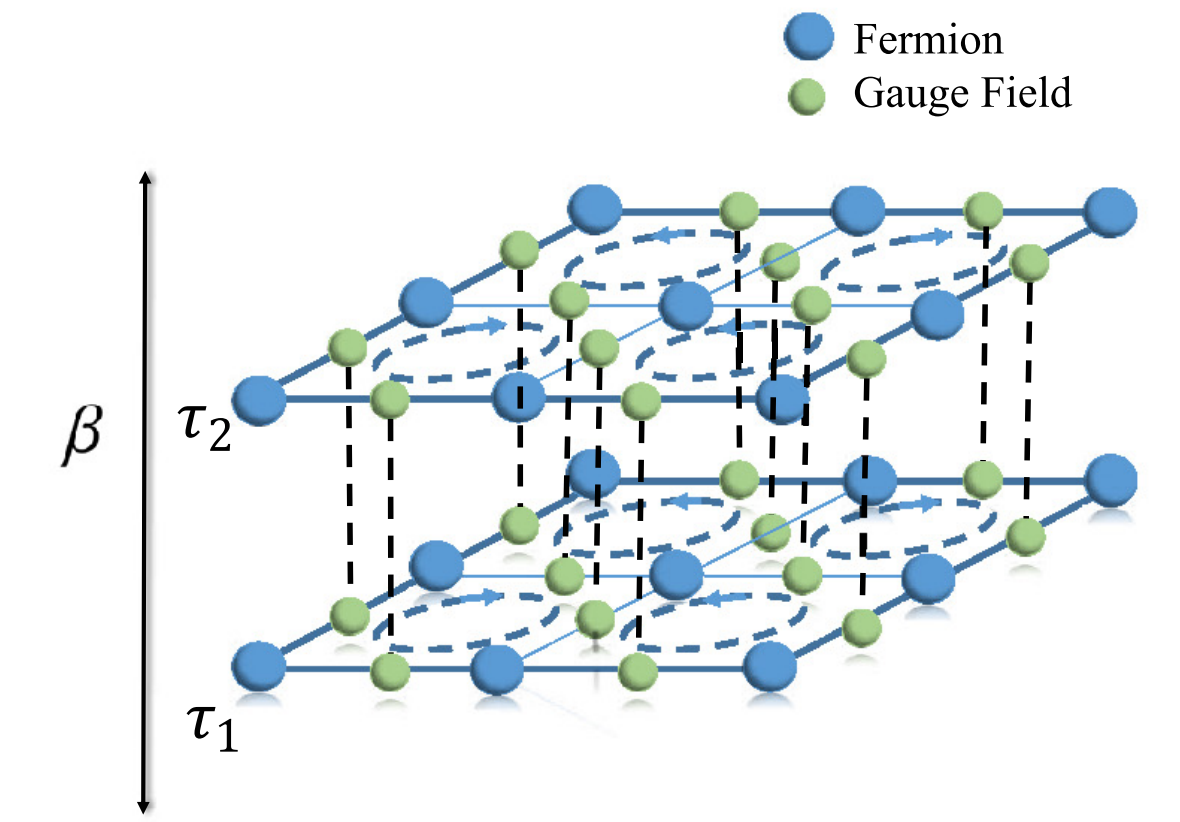
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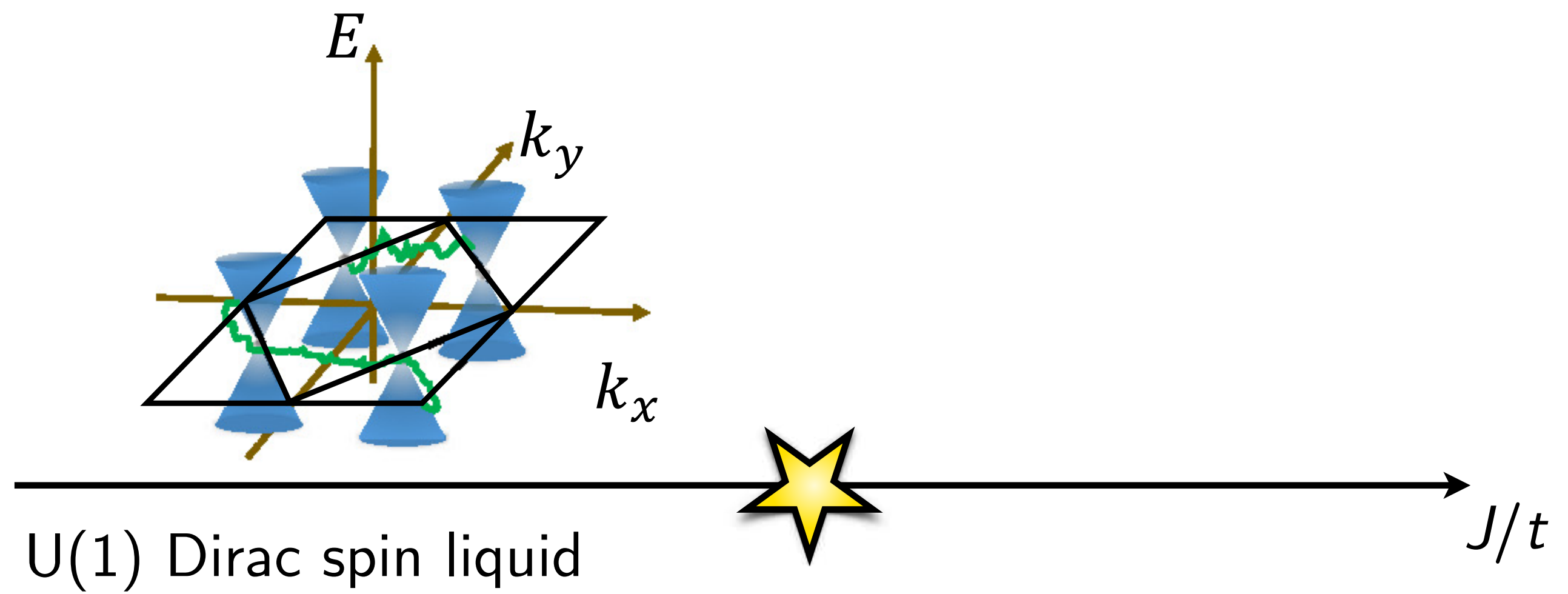
Compact U(1)  
gauge field

Fermions

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Phase diagram ( $K > 0$ ):





# Model: Lattice compact QED<sub>3</sub>

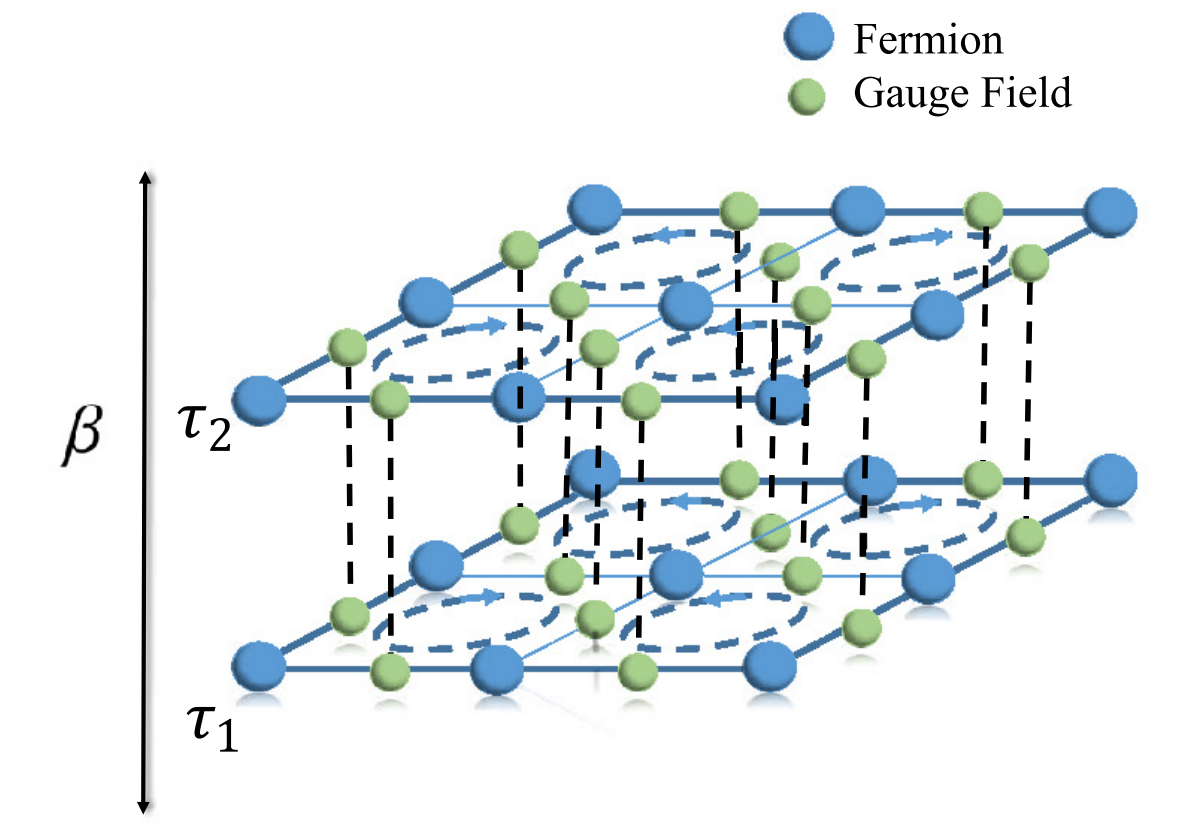
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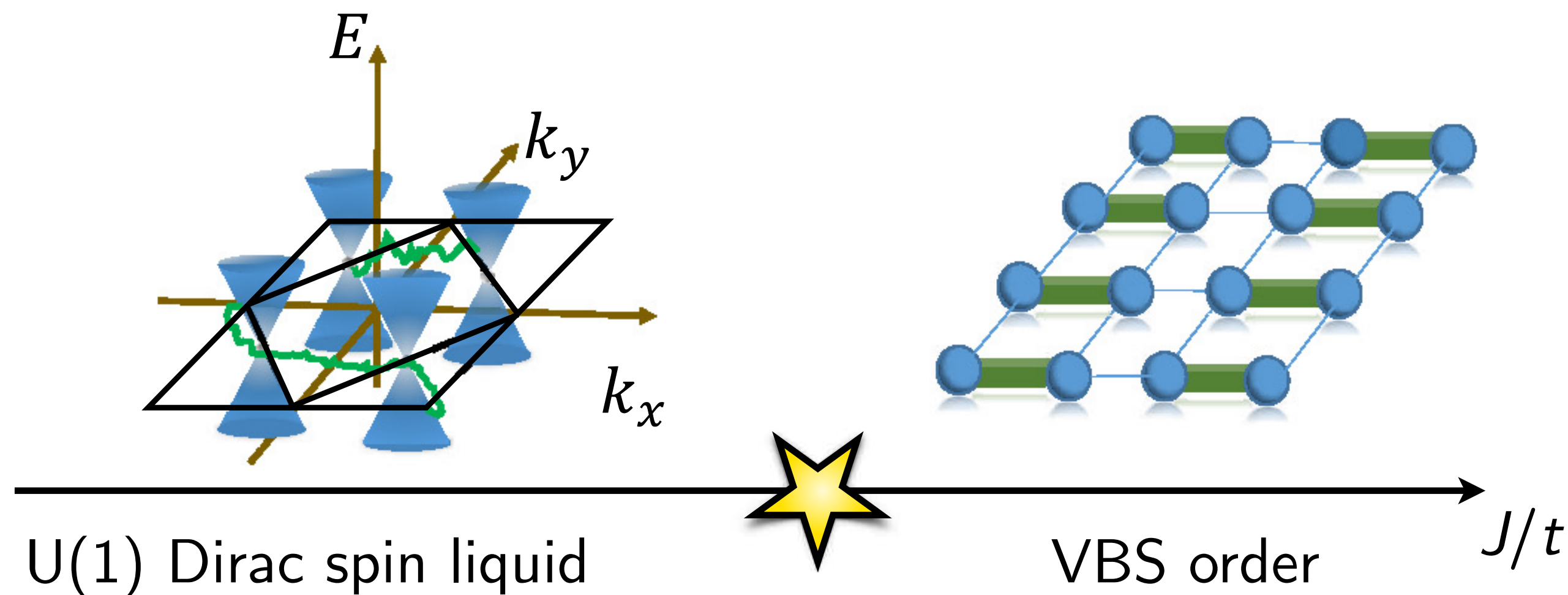
Compact U(1)  
gauge field

Fermions

... favors  $\pi$  flux for  $K > 0$



Phase diagram ( $K > 0$ ):



[Xu et al., PRX '19]

# Field theory: QED<sub>3</sub>-Gross-Neveu-XY

Action (continuum):

$$S = \int d\tau \int d^2\vec{x} \left[ \bar{\psi} \gamma_\mu (\partial_\mu - iA_\mu) \psi + \phi^a \bar{\psi} \mu^a \psi + \frac{r}{2} \phi^a \phi^a + \frac{1}{2e^2} (\epsilon_{\mu\nu\rho} \partial_\nu A_\rho)^2 \right]$$

$a = x, y$

Noncompact U(1)  
gauge field

Dirac fermions

XY order parameter

# Field theory: QED<sub>3</sub>-Gross-Neveu-XY

Action (continuum):

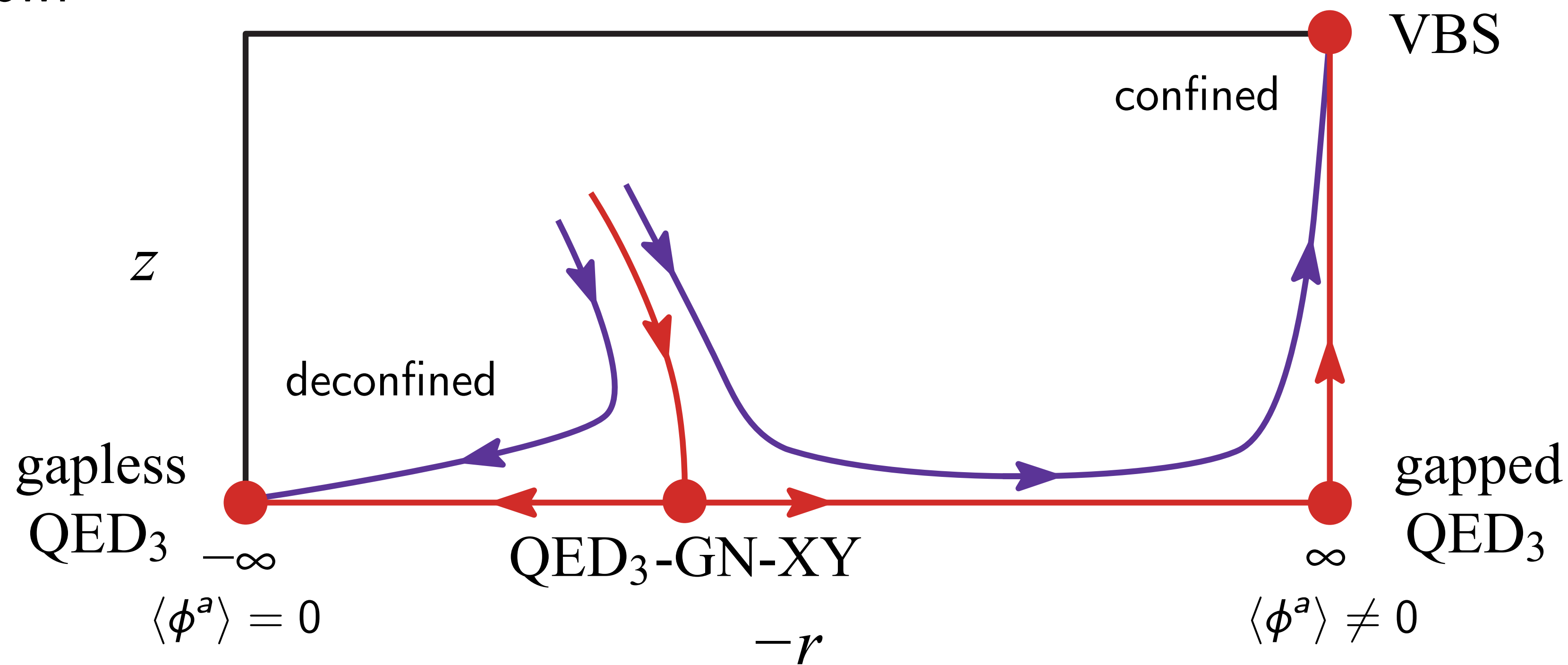
$$S = \int d\tau \int d^2\vec{x} \left[ \bar{\psi} \gamma_\mu (\partial_\mu - iA_\mu) \psi + \phi^a \bar{\psi} \mu^a \psi + \frac{r}{2} \phi^a \phi^a + \frac{1}{2e^2} (\epsilon_{\mu\nu\rho} \partial_\nu A_\rho)^2 \right] \quad a = x, y$$

Noncompact U(1)  
gauge field

Dirac fermions

XY order parameter

RG flow:



QED<sub>3</sub>-GN-XY criticality:

$$\nu^{-1} = 1 - \frac{80}{3\pi^2 N_f} + \mathcal{O}(1/N_f^2)$$

$$\eta_\phi = 1 + \frac{56}{3\pi^2 N_f} + \mathcal{O}(1/N_f^2)$$

$$\Delta_{\text{VBS}} = 1 + \frac{28}{3\pi^2 N_f} + \mathcal{O}(1/N_f^2)$$

$$\Delta_{\text{AFM}} = 2 - \frac{40}{3\pi^2 N_f} + \mathcal{O}(1/N_f^2)$$

[LJ, Wang, Scherer, Meng, Xu, PRB '20]  
Extension to  $\mathcal{O}(1/N_f^2)$ : [Zerf et al., PRD '20]

See also: [Dupuis et al., PRB '19]

# Evidence for QED<sub>3</sub>-Gross-Neveu-XY criticality

## Scenario 1: Conventional paramagnet

$$\begin{aligned} \text{XY:} \quad \nu &\simeq 0.672 \\ \eta_\phi &\simeq 0.039 \end{aligned}$$

## Scenario 2: Dirac fermions

$$\begin{aligned} \text{Gross-Neveu-XY:} \quad \nu &\simeq 1.07 \\ \eta_\phi &\simeq 0.97 \end{aligned}$$

... for  $N_f = 8$

## Scenario 3: Dirac fermions + U(1) gauge field

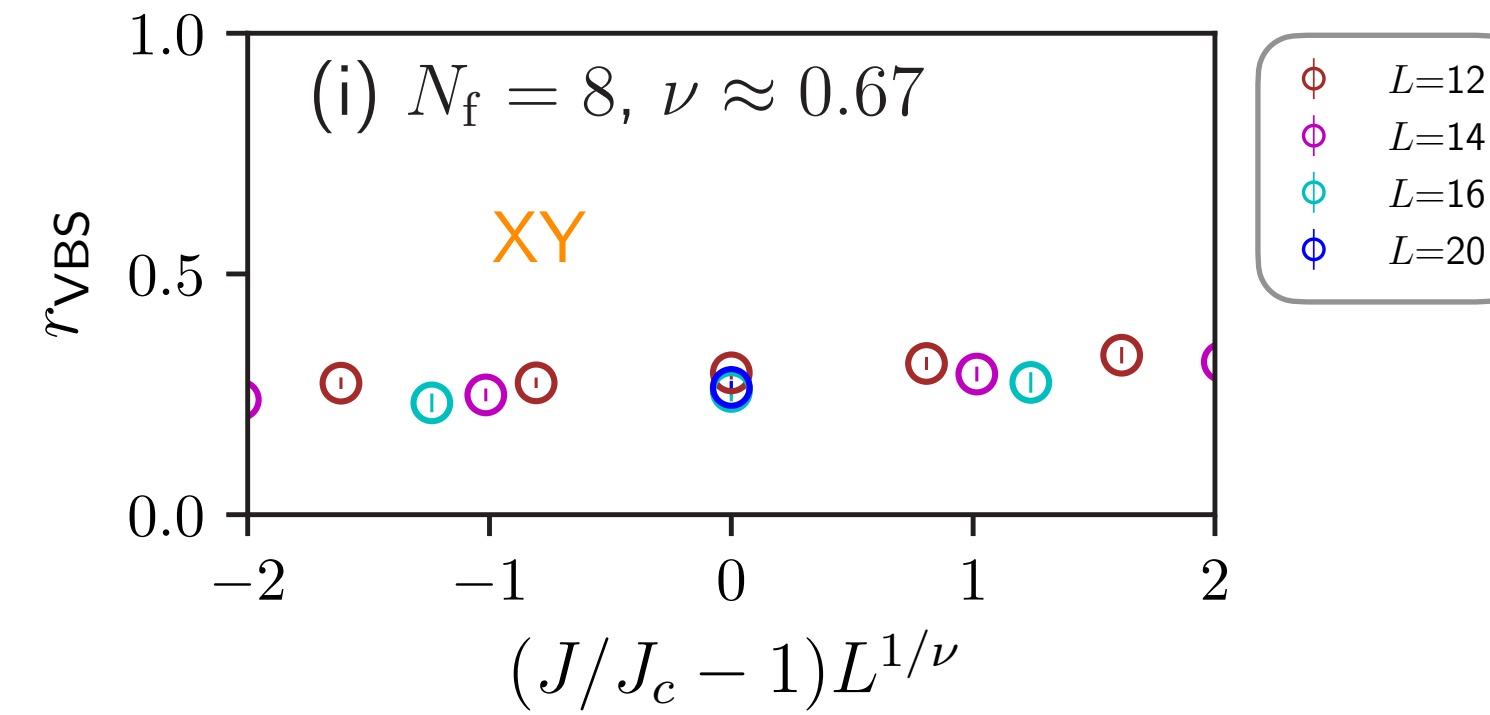
$$\begin{aligned} \text{QED}_3\text{-Gross-Neveu-XY:} \quad \nu &\simeq 1.51 \\ \eta_\phi &\simeq 1.24 \end{aligned}$$

... for  $N_f = 8$

# Evidence for QED<sub>3</sub>-Gross-Neveu-XY criticality

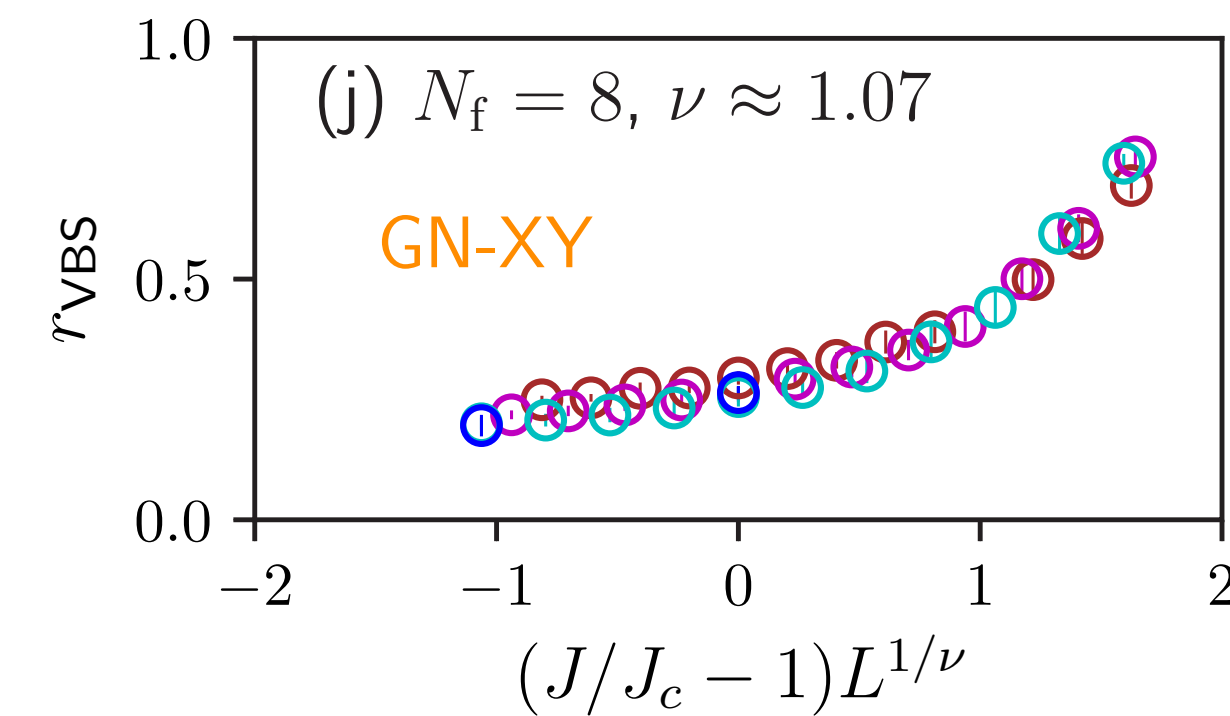
## Scenario 1: Conventional paramagnet

XY:  $\nu \simeq 0.672$   
 $\eta_\phi \simeq 0.039$



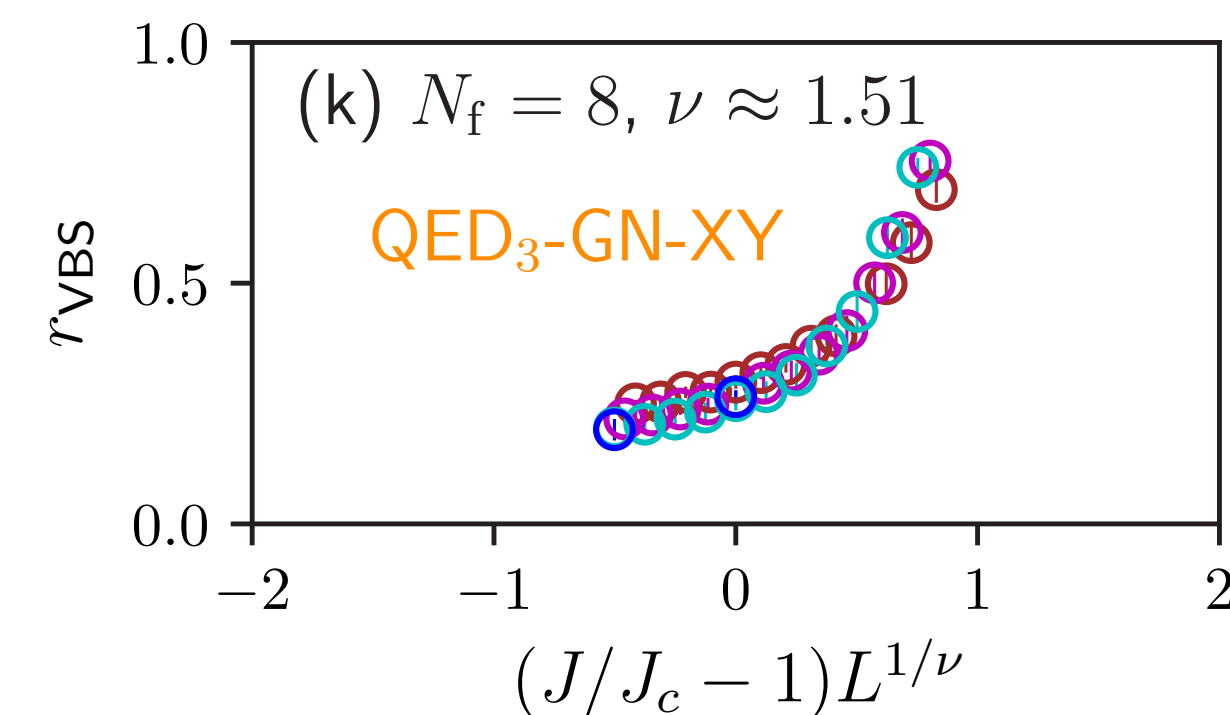
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## Scenario 3: Dirac fermions + U(1) gauge field

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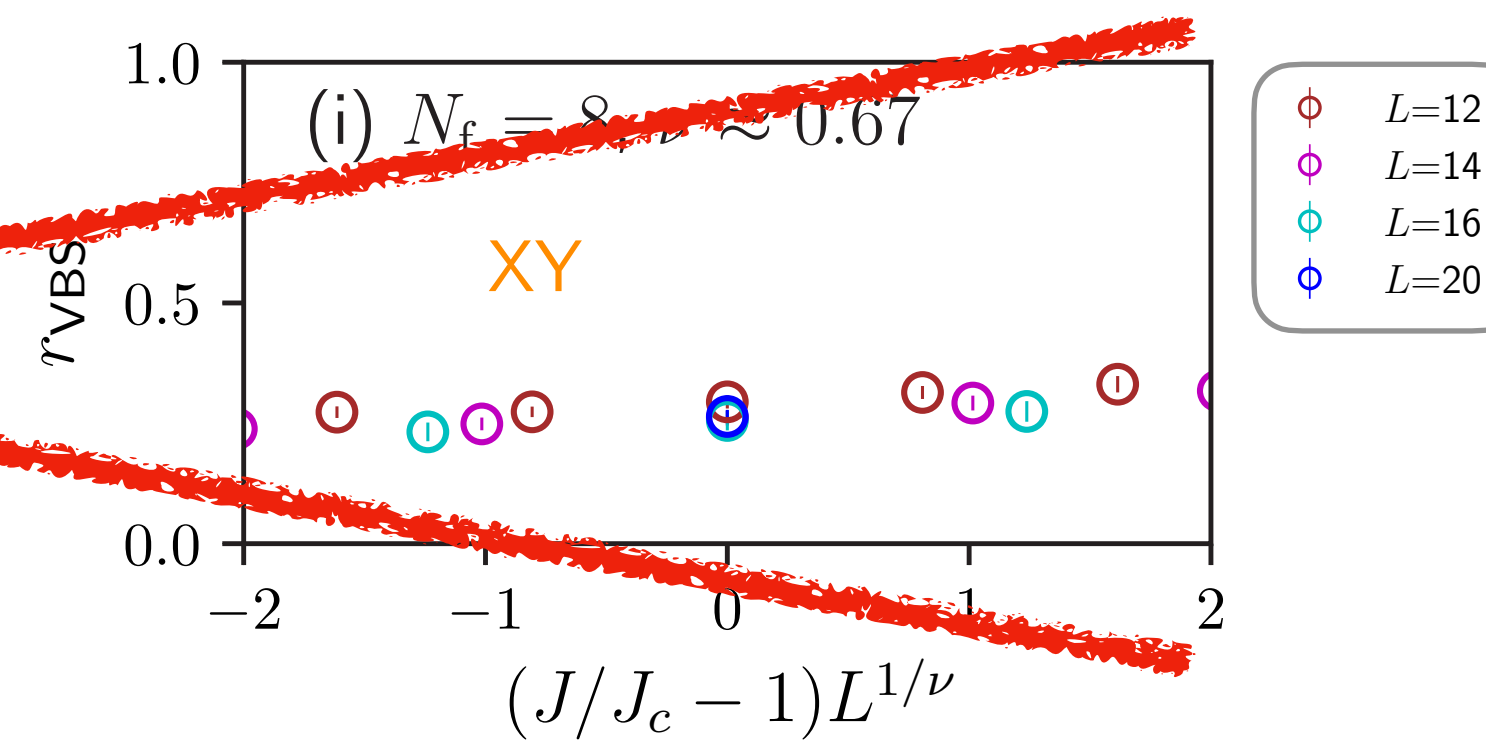
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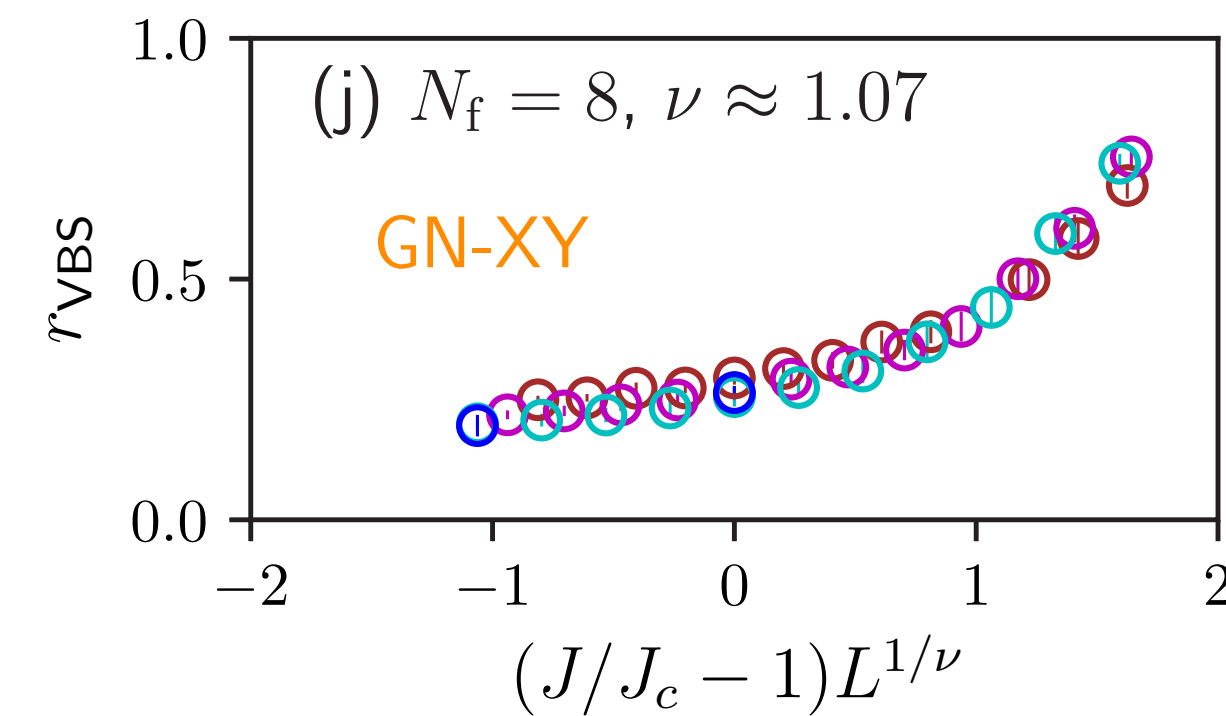
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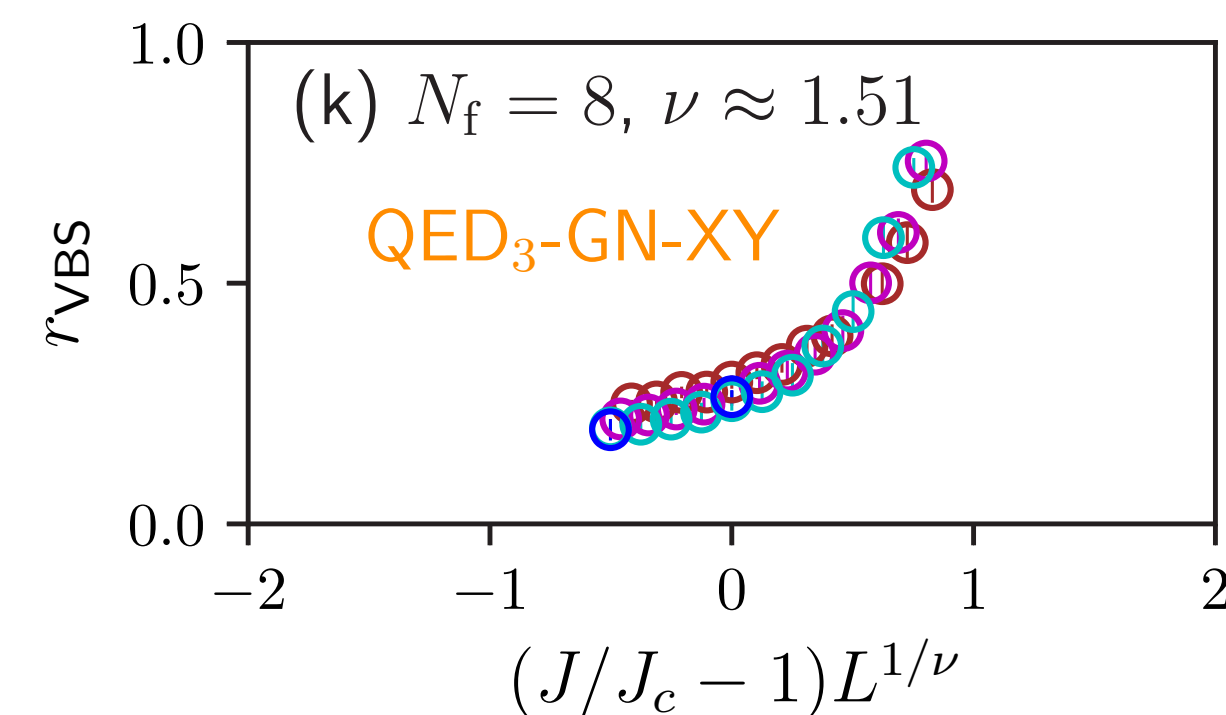


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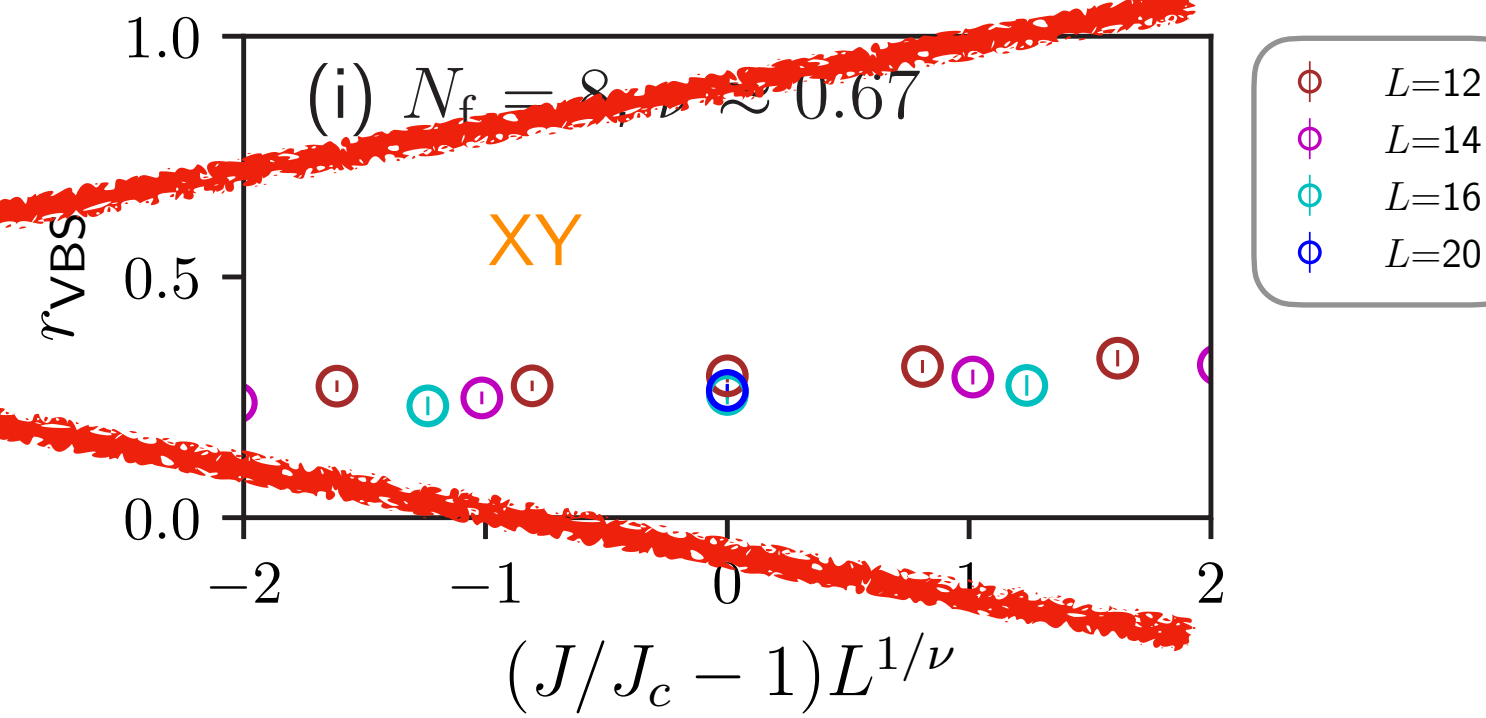
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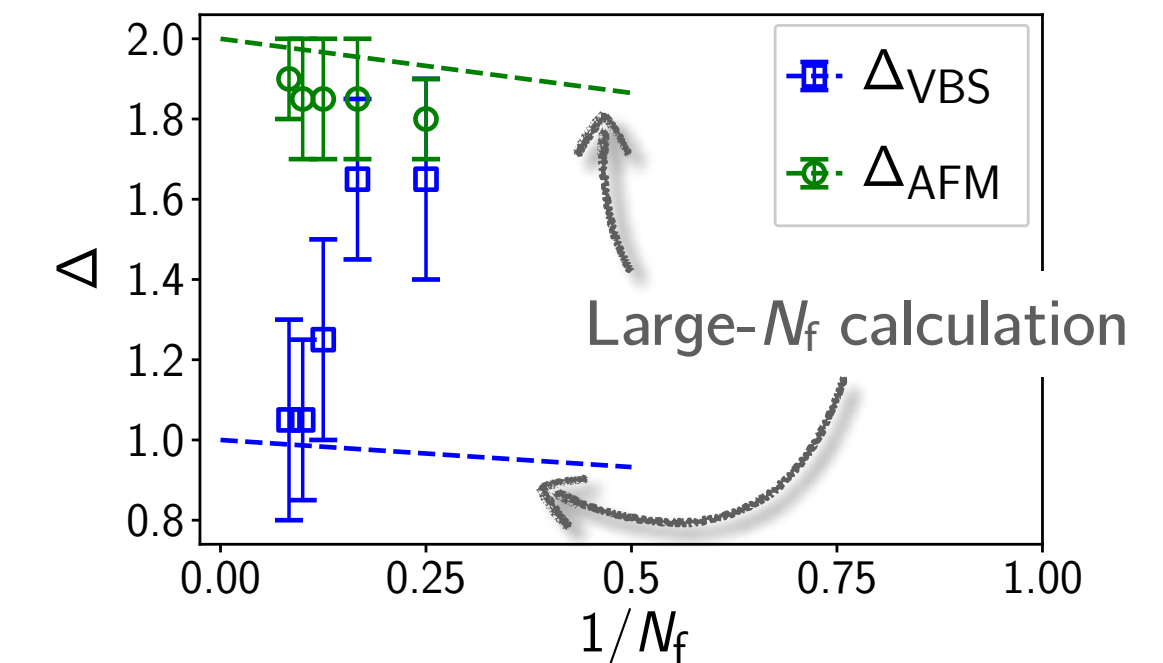
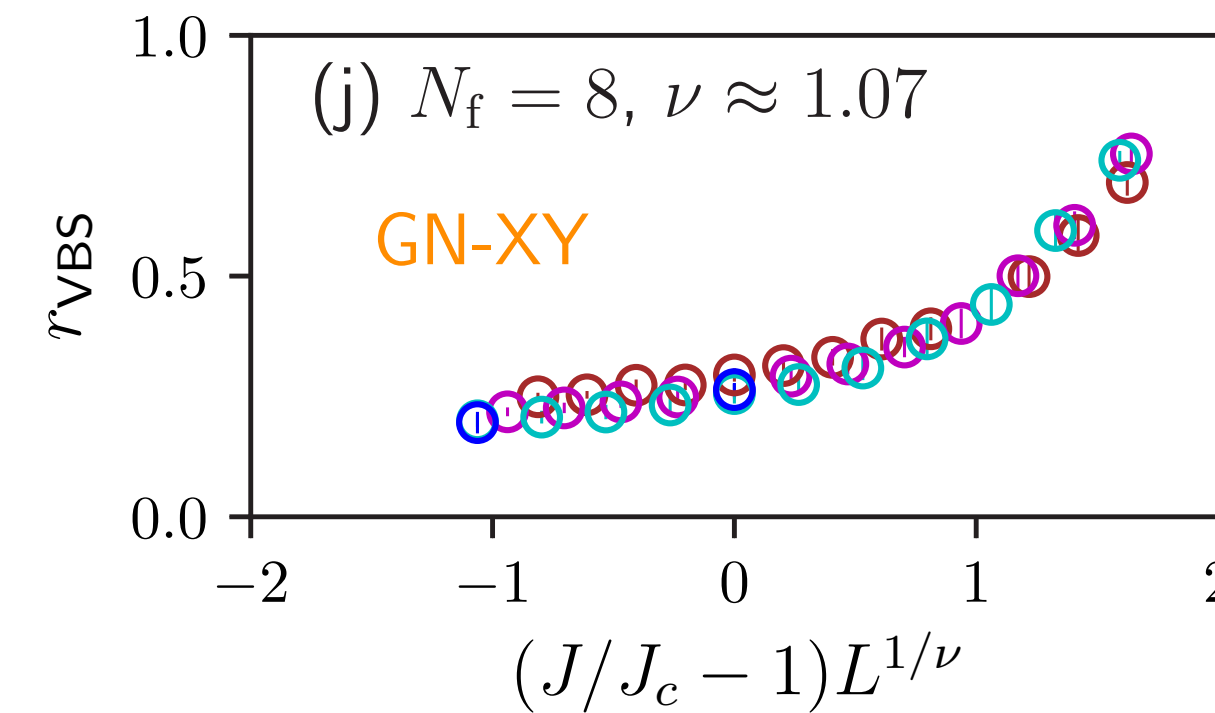
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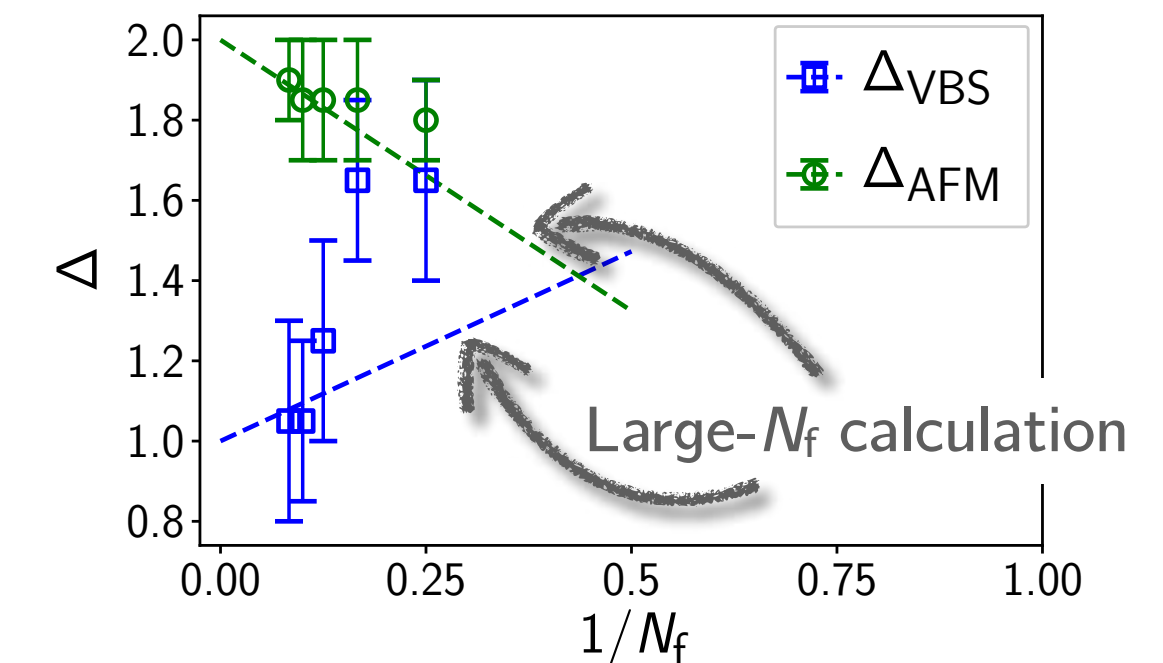
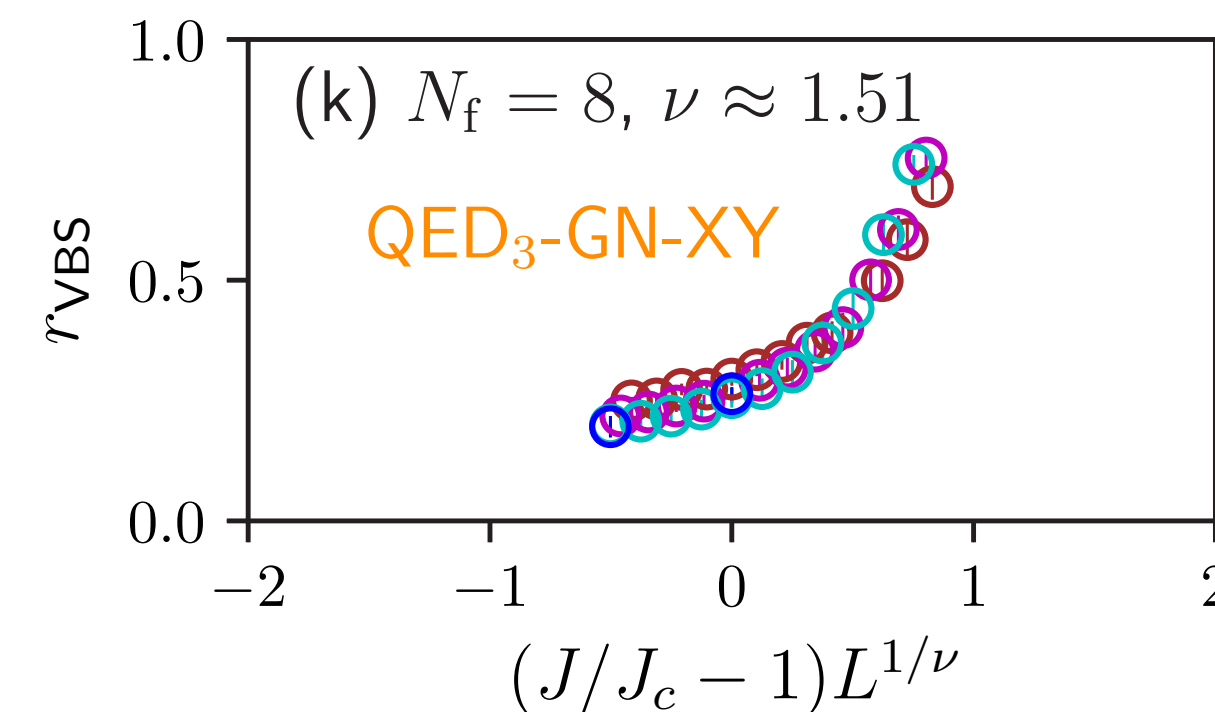
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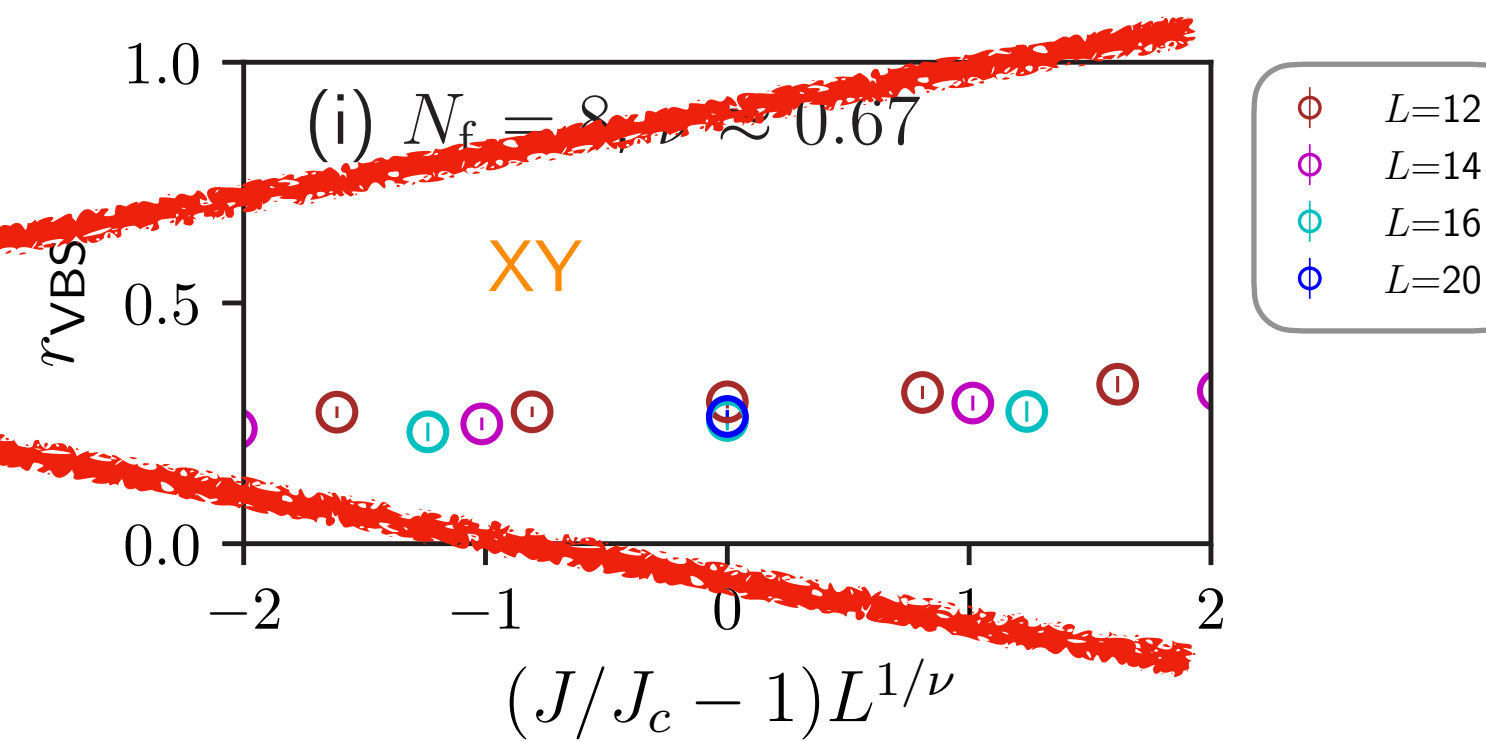
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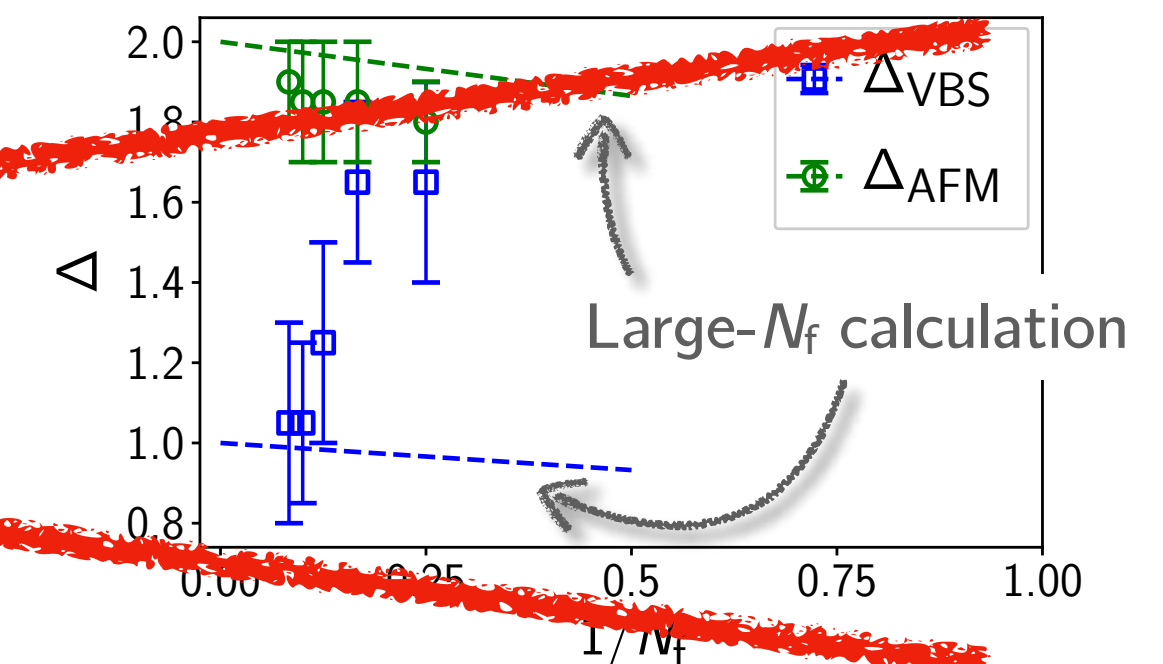
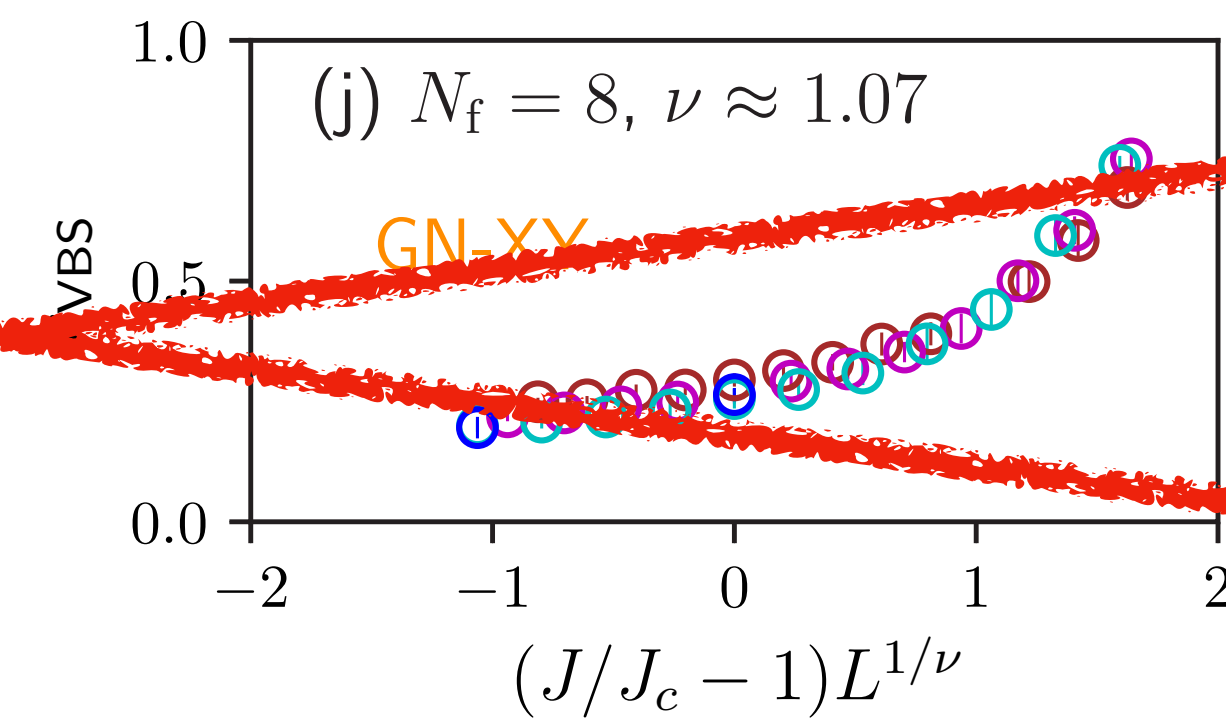
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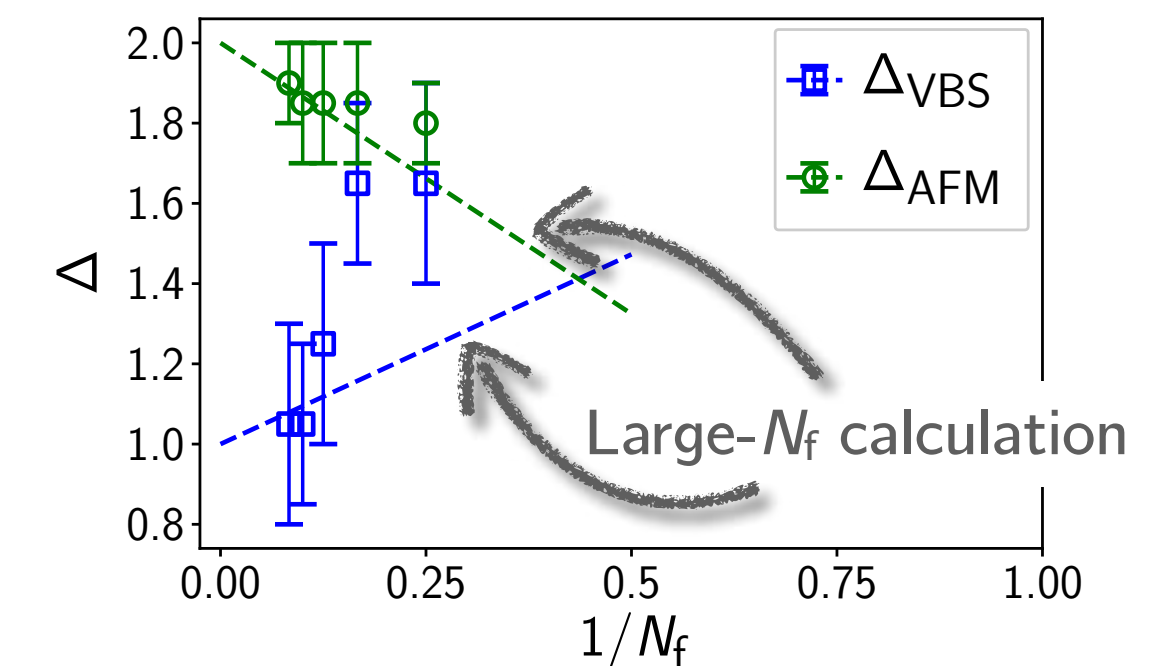
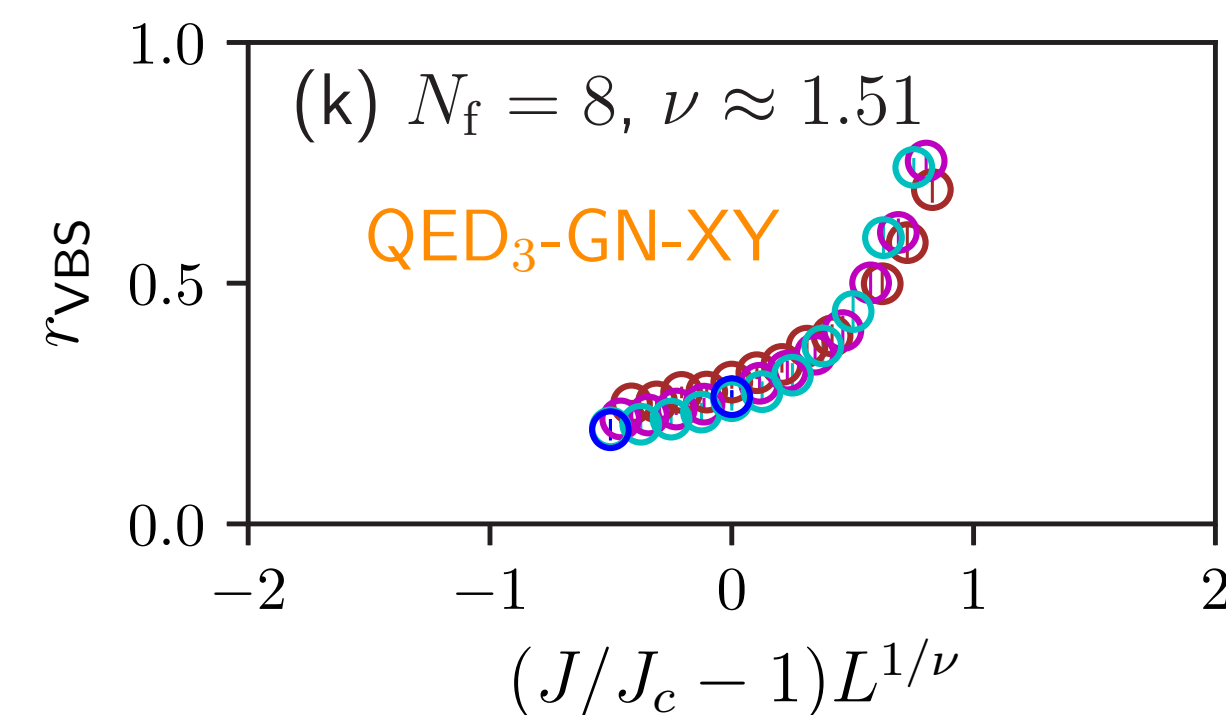


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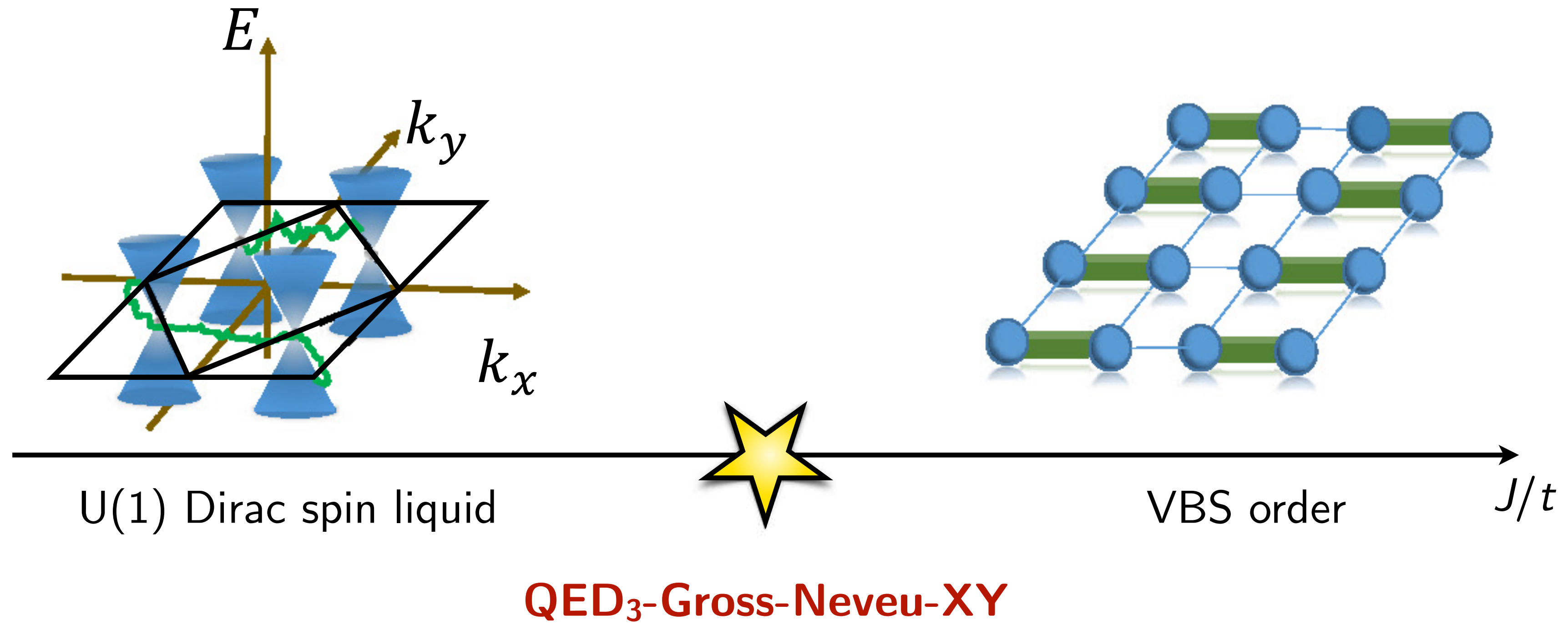
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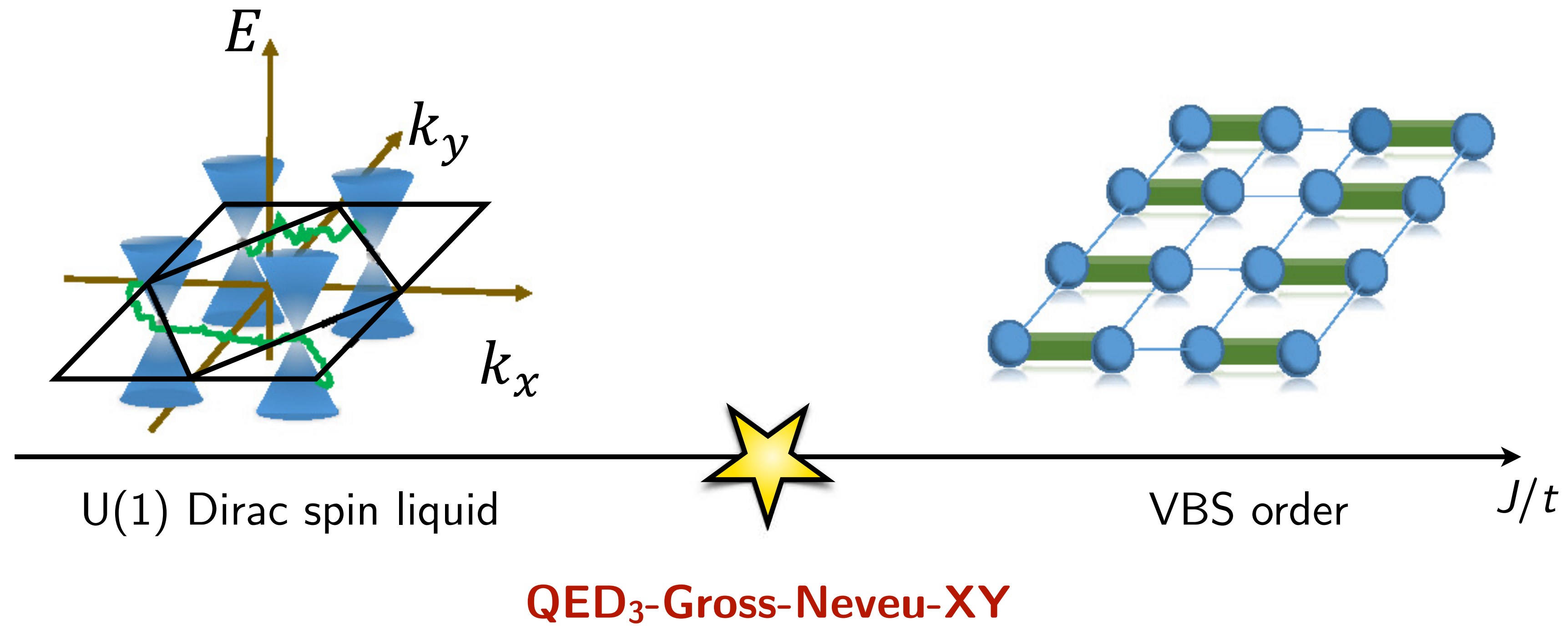




# Conclusions



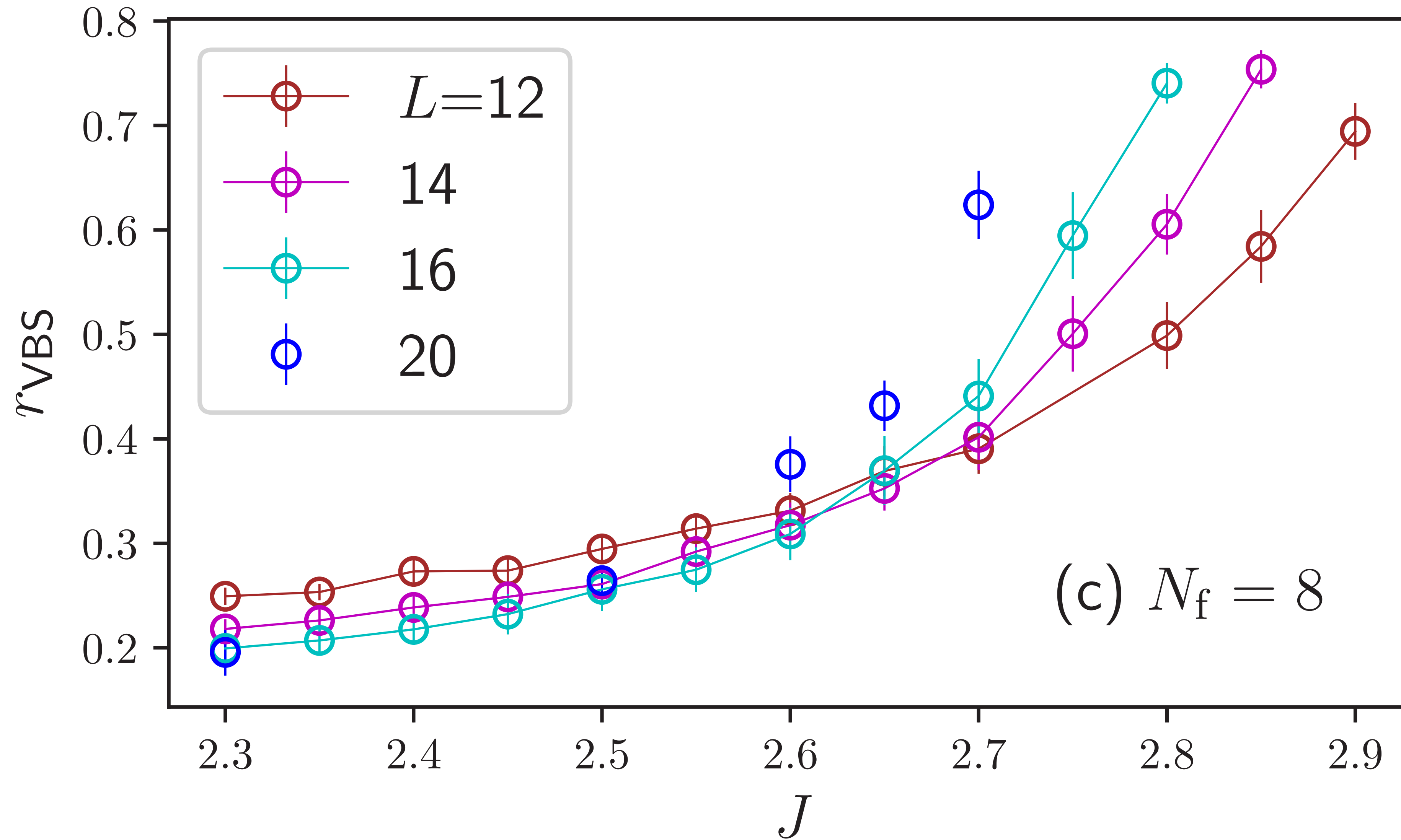
# Conclusions



Quantum critical behavior reveals  
nature of adjacent exotic phase

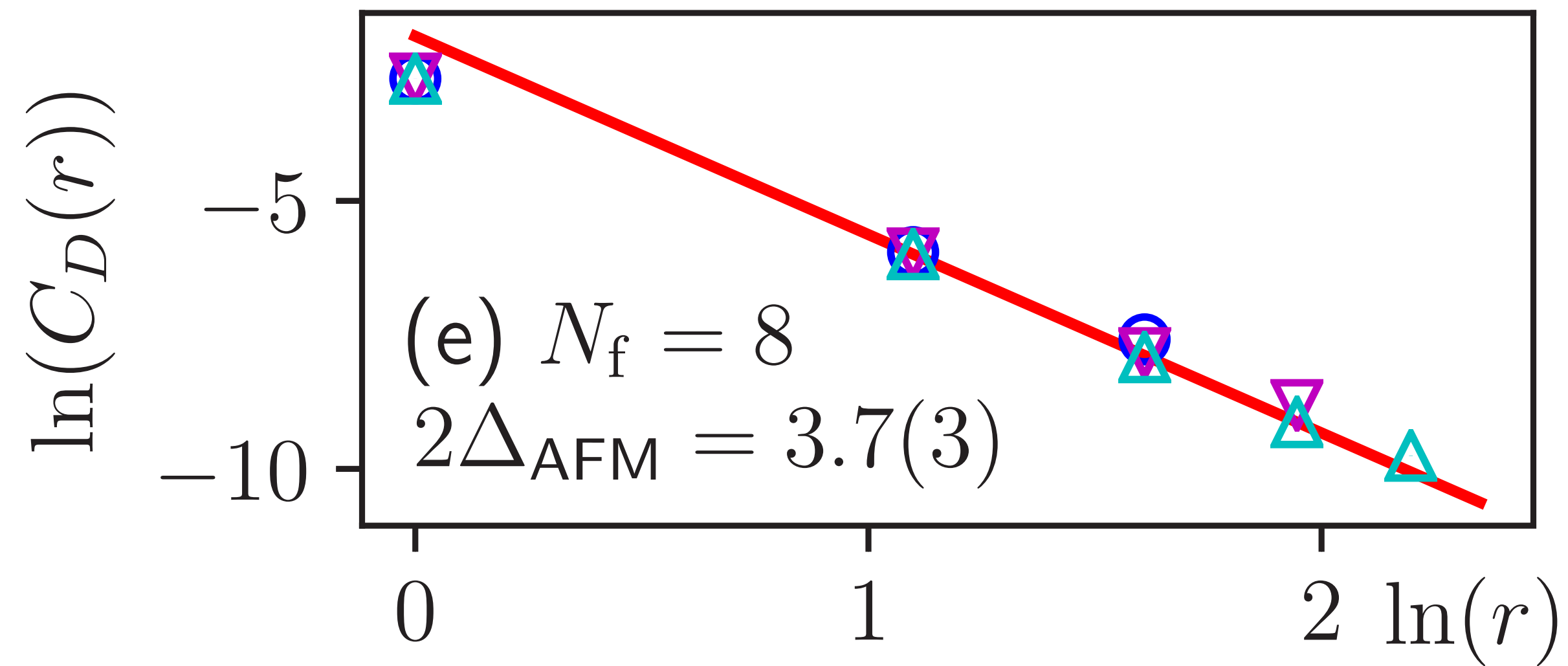


# VBS correlation ratio



# Decay of critical correlators

Dimer correlator



Spin correlator

