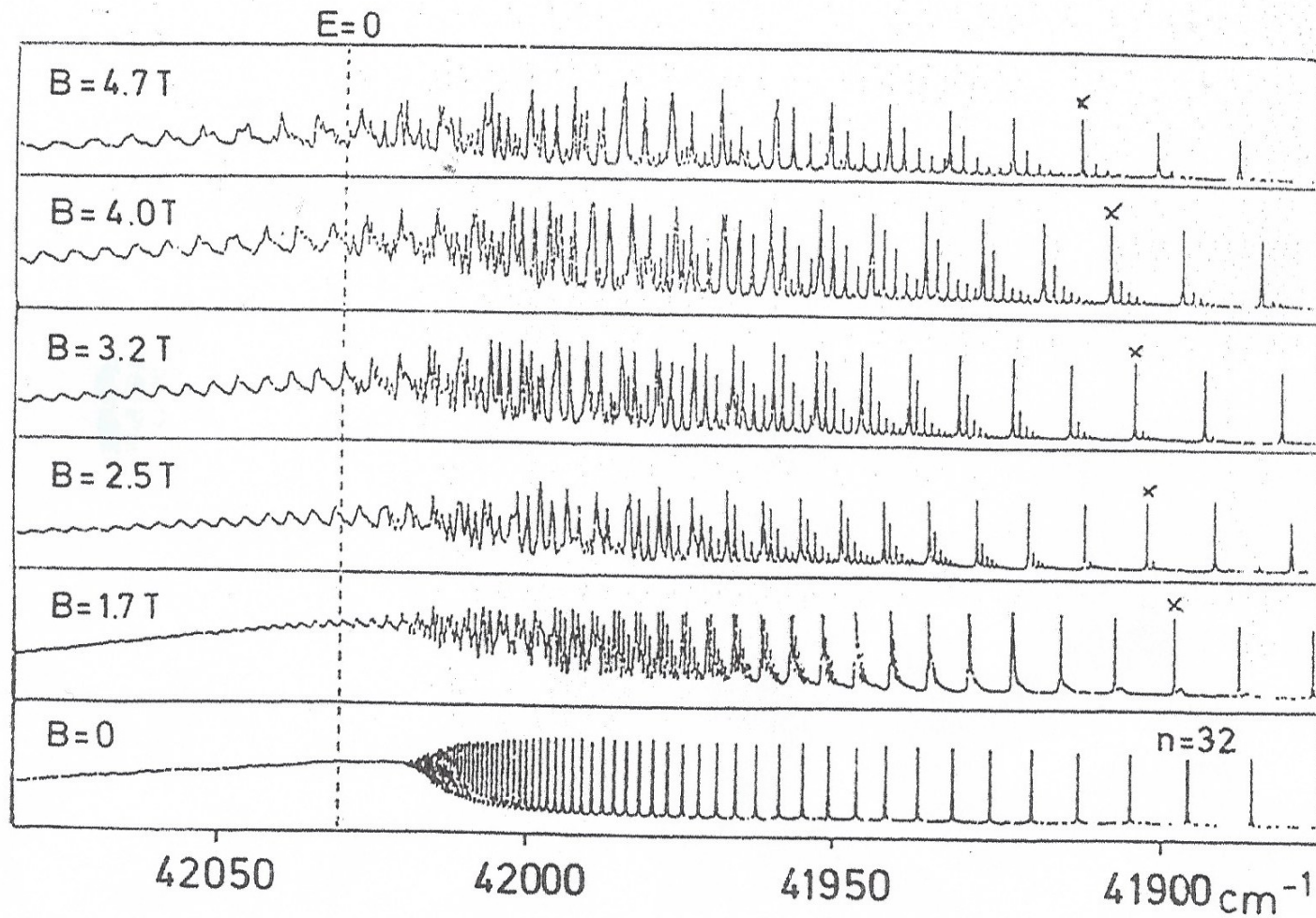
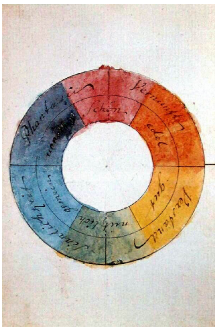


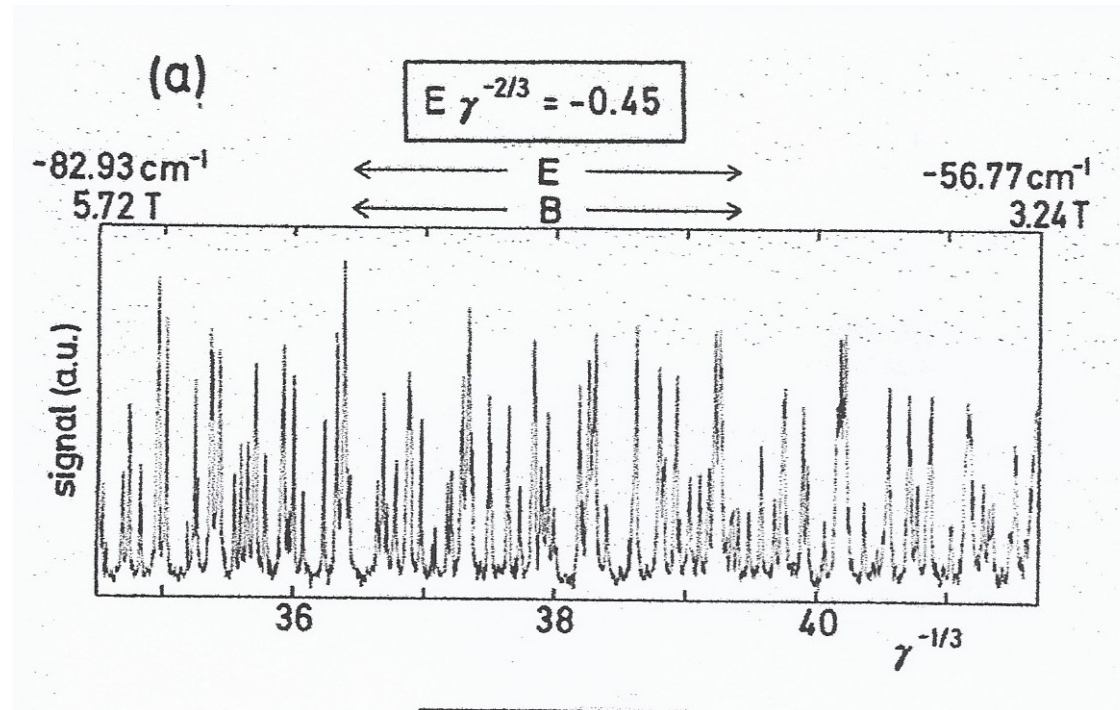
## Spektren und Bahnen: Wasserstoff im Magnetfeld

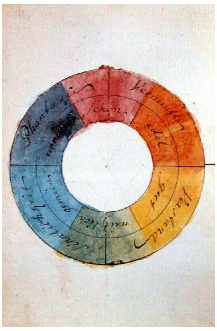


Garton, Tomkins, *Astrophys. J.* 158, 839 (1969)

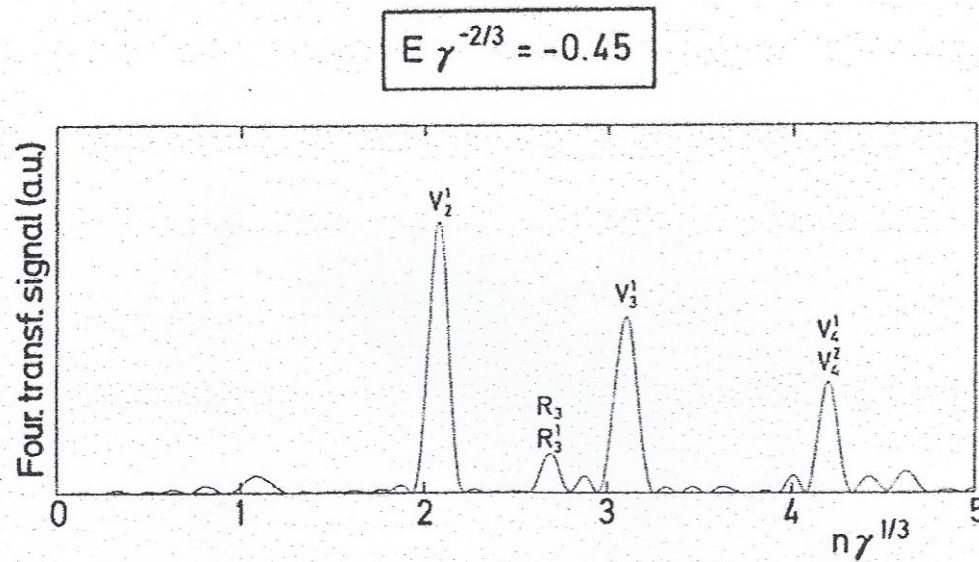


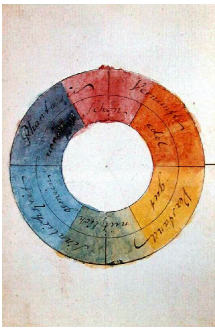
# Spektren und Bahnen: Wasserstoff im Magnetfeld





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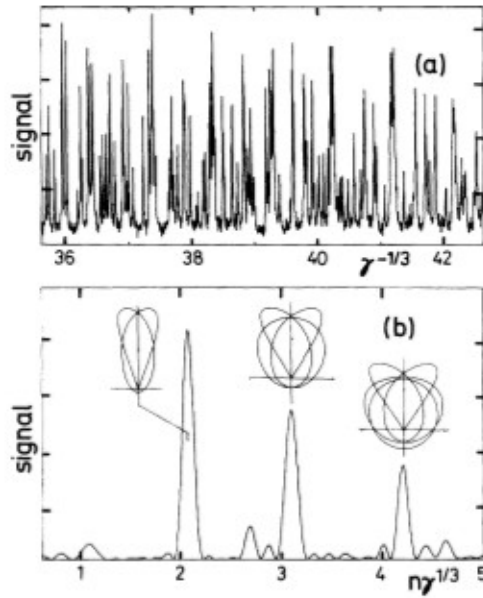
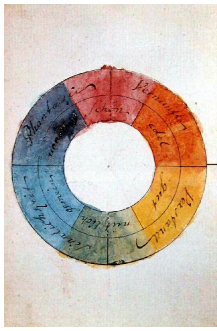


FIG. 1. (a) Scaled-energy spectrum at  $\tilde{E} = -0.45$  as a function of  $\gamma^{-1/3}$ . Range of excitation energy  $-77.7 \text{ cm}^{-1} \leq E \leq -54.3 \text{ cm}^{-1}$  and field strength  $5.19 \geq B \geq 3.03 \text{ T}$ . (b) Fourier-transformed action spectrum of (a); closed orbits correlated to respective resonances in  $(\rho, z)$  projection;  $z$  coordinate vertically.



# Spektren und Bahnen: Wasserstoff im Magnetfeld

VOLUME 61, NUMBER 2

PHYSICAL REVIEW LETTERS

11 JULY 1988

## Quasi-Landau Spectrum of the Chaotic Diamagnetic Hydrogen Atom

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(Received 28 September 1987)

By the employment of "constant-scaled-energy spectroscopy" as a novel spectroscopic technique, the quasi-Landau resonance system of the diamagnetic H atom in even-parity  $m=0$  magnetic final states is observed for the first time in its entirety from the regular  $1/n$  into the chaotic quasi-Landau regime. It evolves, fully unexpectedly, into a systematically structured hierarchy of generations of resonances, correlated to three physically different types of closed classical orbits.

PACS numbers: 32.80.-t, 05.45.+b, 32.60.+i

The physics of the highly excited diamagnetic hydrogen atom has recently attracted much attention,<sup>1-8</sup> largely because this simple nonseparable quantum system turns classically chaotic as it approaches the ionization limit.<sup>6,9</sup> In this context the quasi-Landau (QL) oscillations and their correlation to classical periodic orbits are of particular interest.<sup>10</sup> Until recently, it was accepted that only one QL resonance type, discovered by Garton and Tomkins,<sup>11</sup> exists. Experiments with the H atom<sup>3-5</sup> and theoretical studies<sup>7,8,12,13</sup> have uncovered further, basically new resonances correlated with three-dimensional orbits. Nevertheless, the central question as to the *entire* set of QL resonances resulting from final states with a given  $m$  quantum number and parity evolving from the regular into the chaotic QL regime has remained open.

We have addressed this basic problem and studied the H-atom Balmer spectrum with even-parity  $m=0$  magnetic final states as a function of both the excitation energy  $E$  and the magnetic field  $B$ , employing for the first time "constant-scaled-energy spectroscopy."<sup>1</sup> Different from previous experiments at constant  $B$ ,<sup>3-5</sup> this technique makes a systematic search for, in principal, *all* possible QL resonances associated with closed classical orbits.<sup>12</sup> In analogy to theoretical work, it is based on the scaling property of the classical Hamiltonian<sup>14</sup>:

$$H(\mathbf{r}, \mathbf{p}; \gamma) = \gamma^{2/3} \tilde{H}(\tilde{\mathbf{r}}, \tilde{\mathbf{p}}; \gamma = 1),$$

where scaled variables are defined by  $\tilde{\mathbf{r}} = \gamma^{2/3} \mathbf{r}$ ,  $\tilde{\mathbf{p}} = \gamma^{-1/3} \mathbf{p}$ , and  $\gamma = B / (2.35 \times 10^7 \text{ T})$ . The semiclassical Bohr-Sommerfeld quantization condition<sup>15</sup> for the two nonseparable coordinates  $\rho, z$  (cylindrical coordinates) is transformed accordingly to scaled form<sup>13</sup>

$$(2\pi)^{-1} \oint (\tilde{p}_\rho d\tilde{\rho} + \tilde{p}_z d\tilde{z}) = n\gamma^{1/3} = C_i, \quad (1)$$

where  $i$  denotes a closed classical orbit. Since the scaled action  $C$  depends on the scaled energy  $\tilde{E} = E\gamma^{-2/3}$  only, it has a constant value  $C_i$  for  $\tilde{E} = \text{const}$  and a given  $i$ . In this case,  $C_i = n\gamma^{1/3}$  describes a spectrum of *equidistant* lines on a scale  $\gamma^{-1/3}$ , the Fourier transform of which in the conjugate coordinate,  $n\gamma^{1/3}$ , consists of *one* resonance

for each  $i$ , to which is correlated the respective orbit  $i$ . By application of these theoretical concepts to experiment, constant-scaled-energy spectra have been taken according to our scanning the field strength linearly with  $\gamma^{-1/3}$ , simultaneously adjusting  $E$  (via the laser wavelength) such that  $\tilde{E} = E\gamma^{-2/3} = \text{const}$  was obeyed. Apart from this novel spectroscopic procedure the experiments have been carried out as previously.<sup>1</sup>

Figure 1(a) shows, as a typical example, a  $\gamma^{-1/3}$  spectrum at  $\tilde{E} = -0.45$ , and Fig. 1(b) the corresponding Fourier-transform  $n\gamma^{1/3}$  action spectrum. The orbits shown correlate to the respective resonances, and have been obtained by classical trajectory calculation.<sup>4,13</sup> Such action spectra have been taken (physically with a

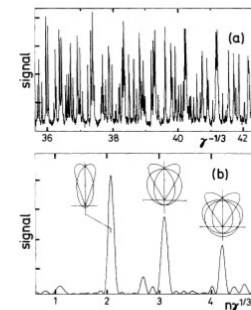
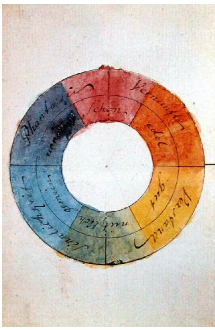
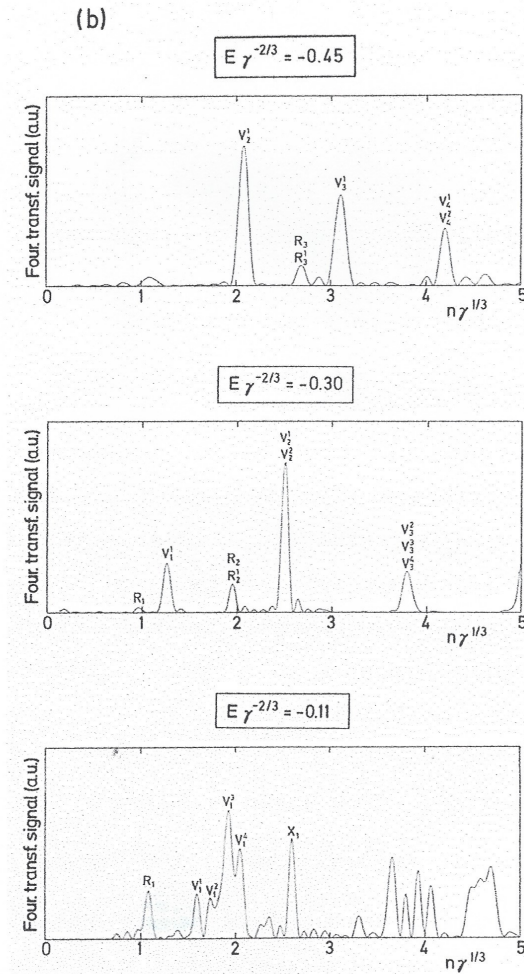
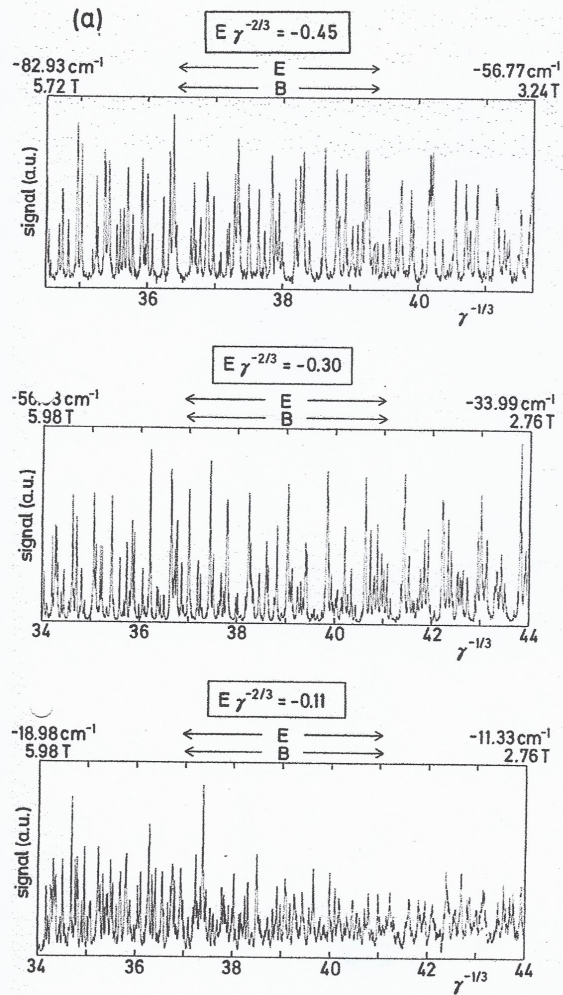
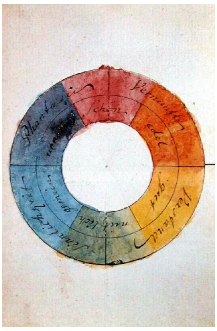


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