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Evaluation of Transfer Function Noise Modelling and Dimensionality Reduction Techniques for Karst Systems

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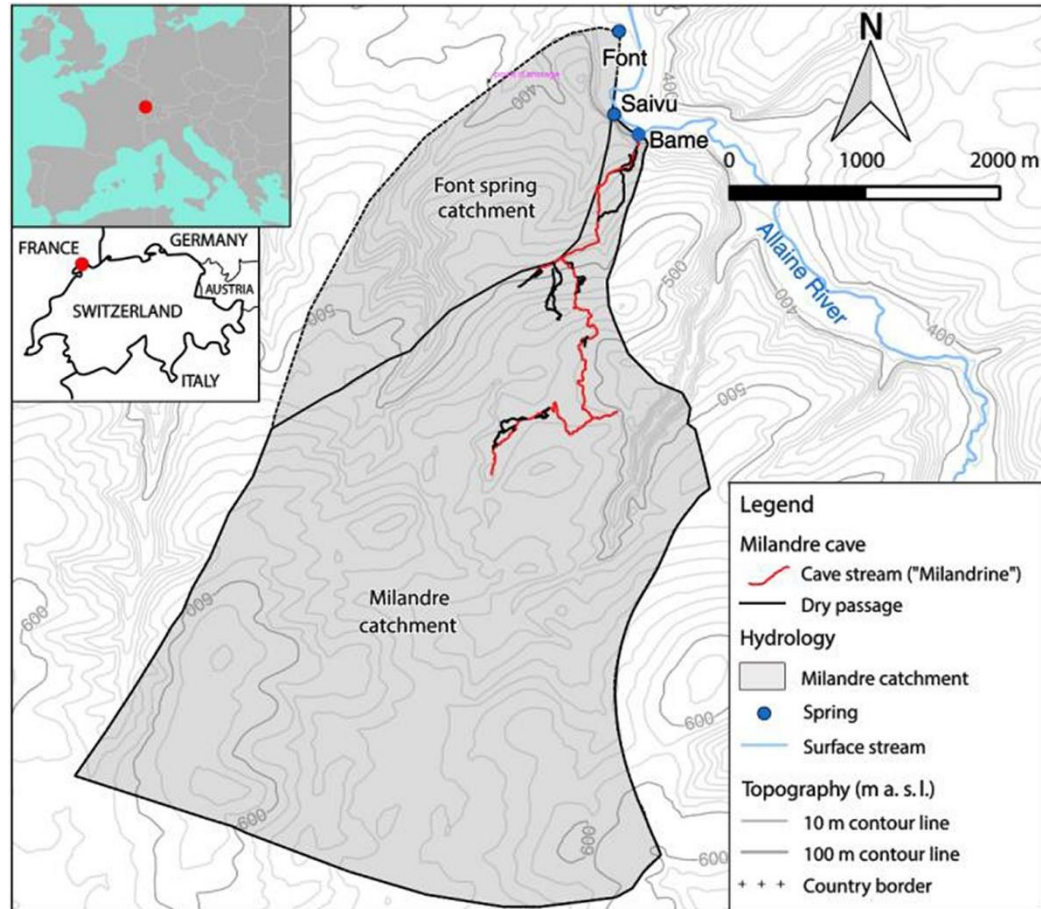
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Approach, Motivation and Aim

- **Modelling** and forecasting of karst system spring discharge **still poses a challenge**
- **Distributed modelling** approaches often suffer from **insufficiently available data**
- **Lumped parameter** models often do not reflect **physical system understanding**

Conceptually and (partially) physically interpretable data-driven model

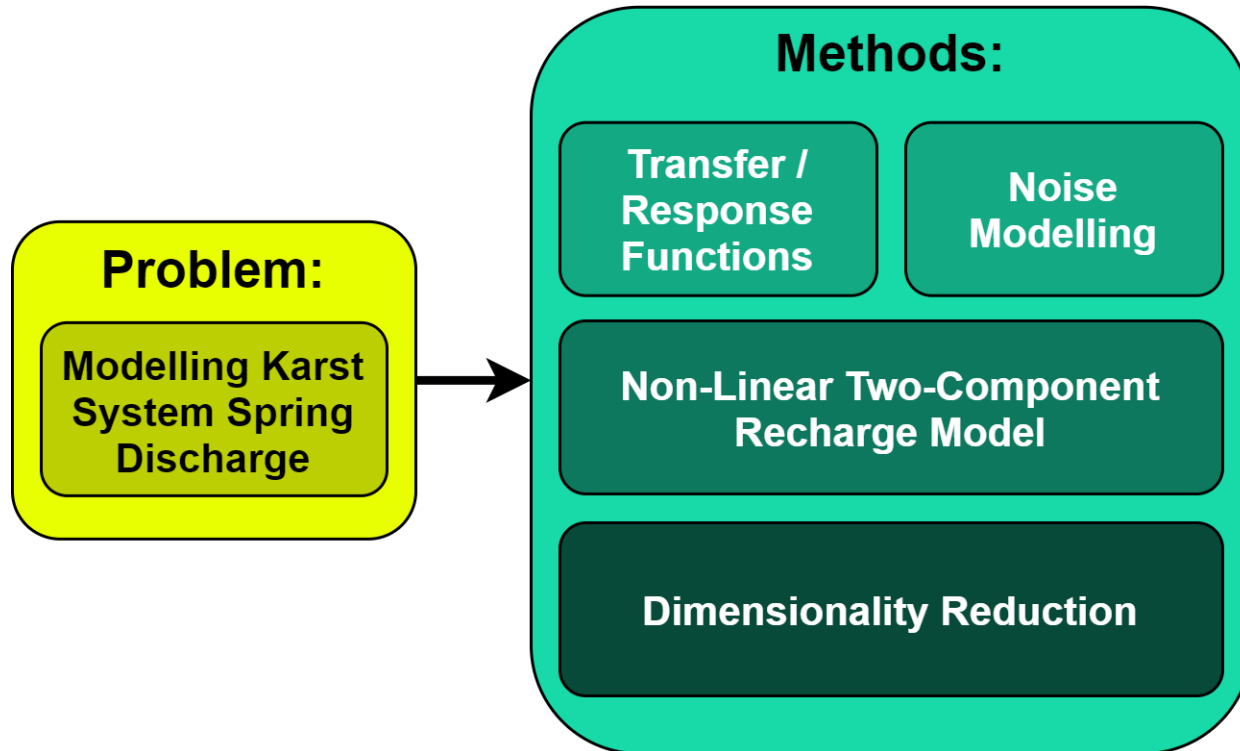
Milandre Karst System



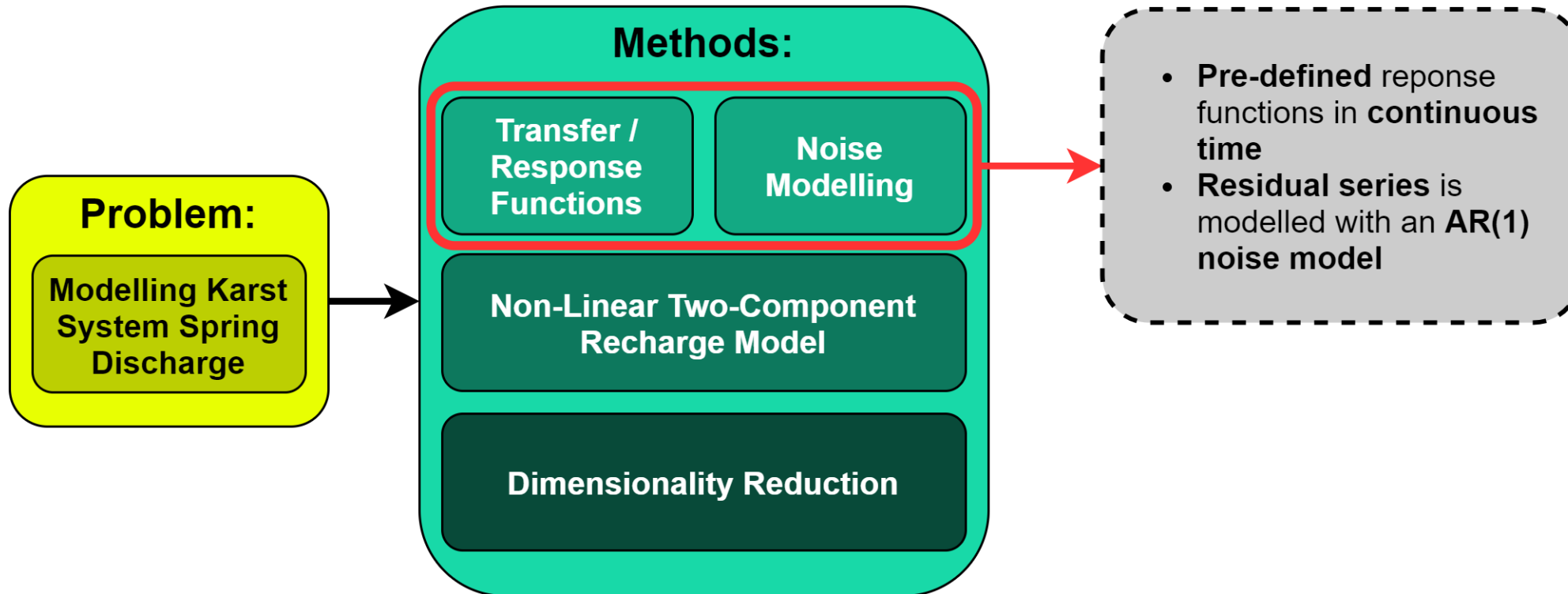
- Rauracian Limestone overlying Oxfordian Marls
- Catchment area approx. 13 km^2
- Two perennial springs (Font, Saivu)
- One overflow-spring (Bâme)
- Autogenic, diffuse recharge regime

Heavily studied and subject to the *Karst Modelling Challenge* (Jeannin et al., 2021)

Methodology

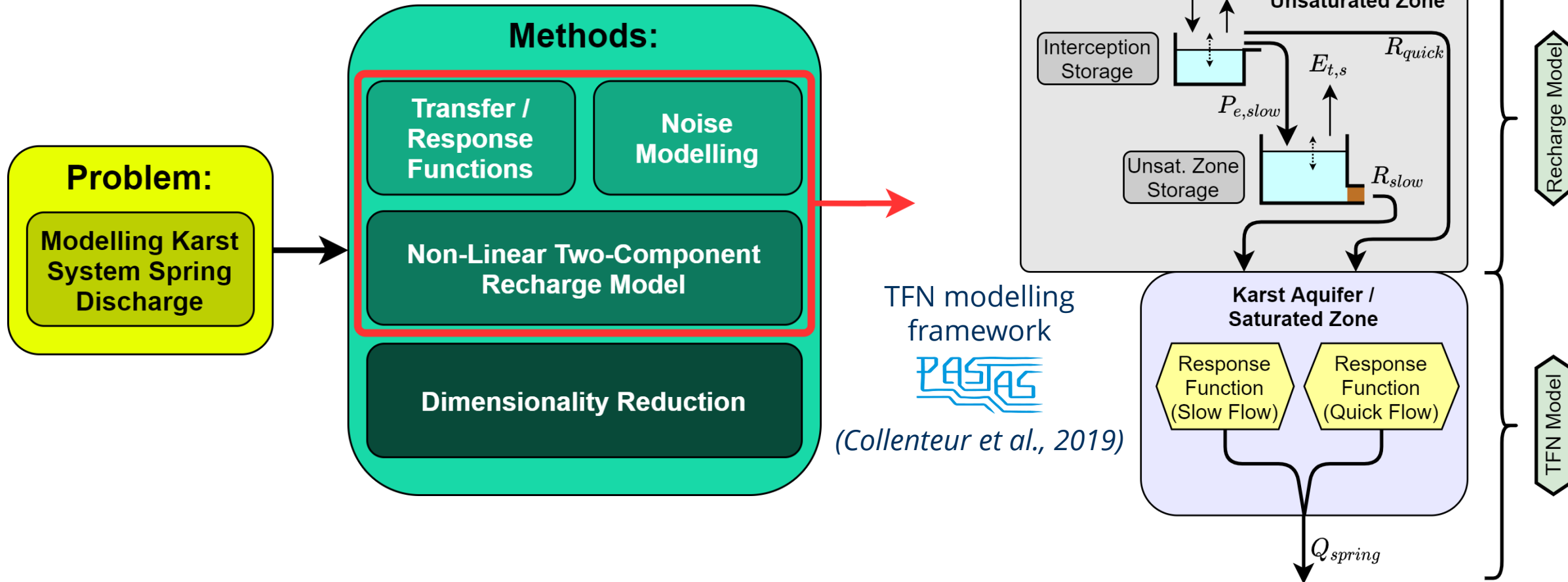


Methodology

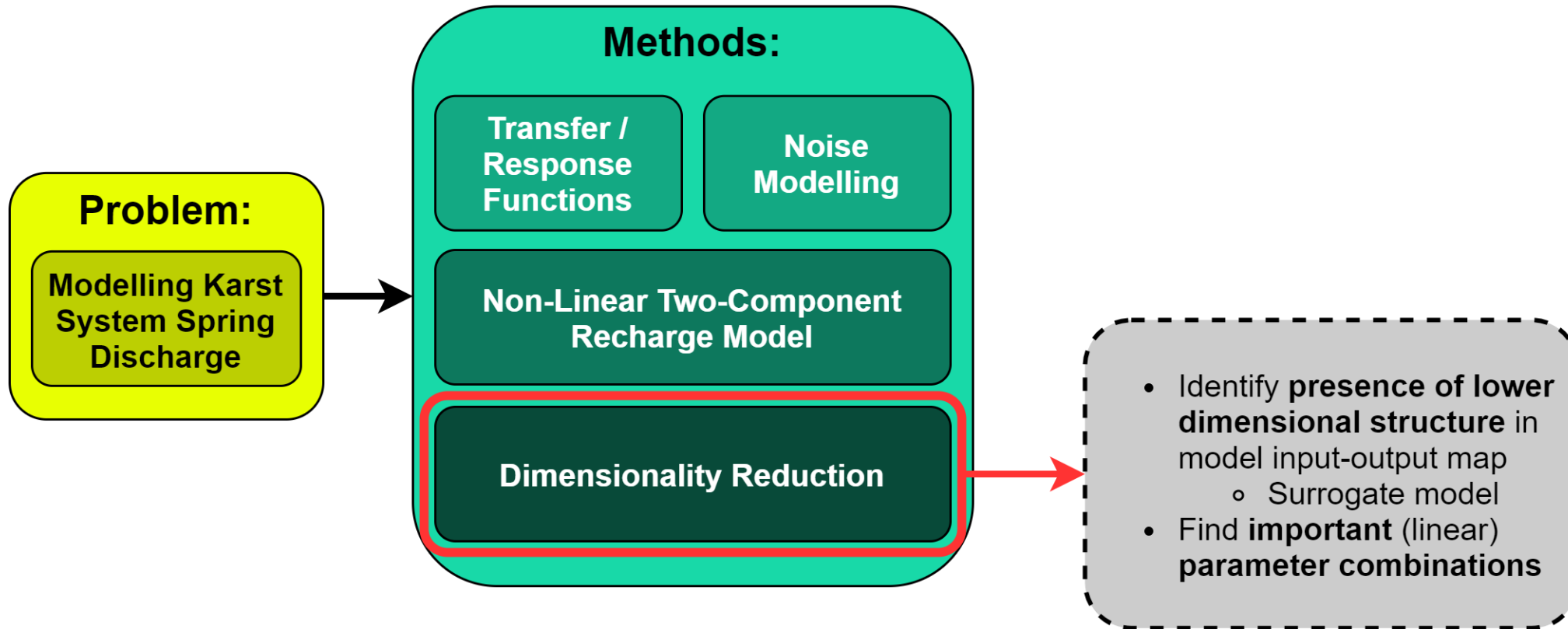


Methodology

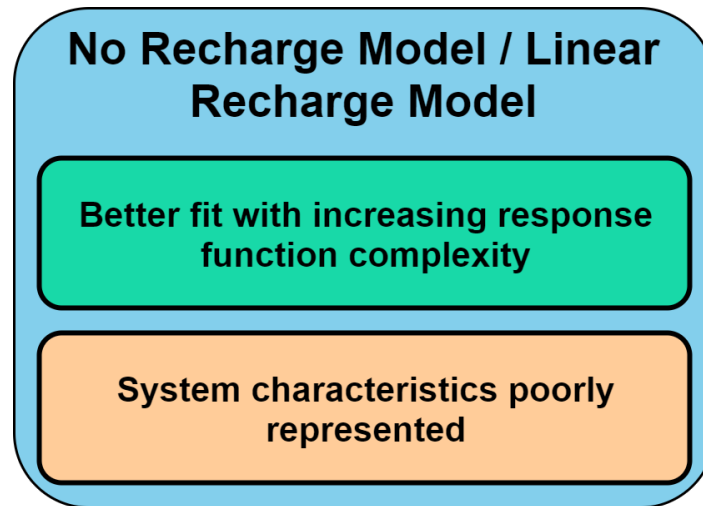
RM based on FlexModel introduced by *Collenteur et al. (2021)*



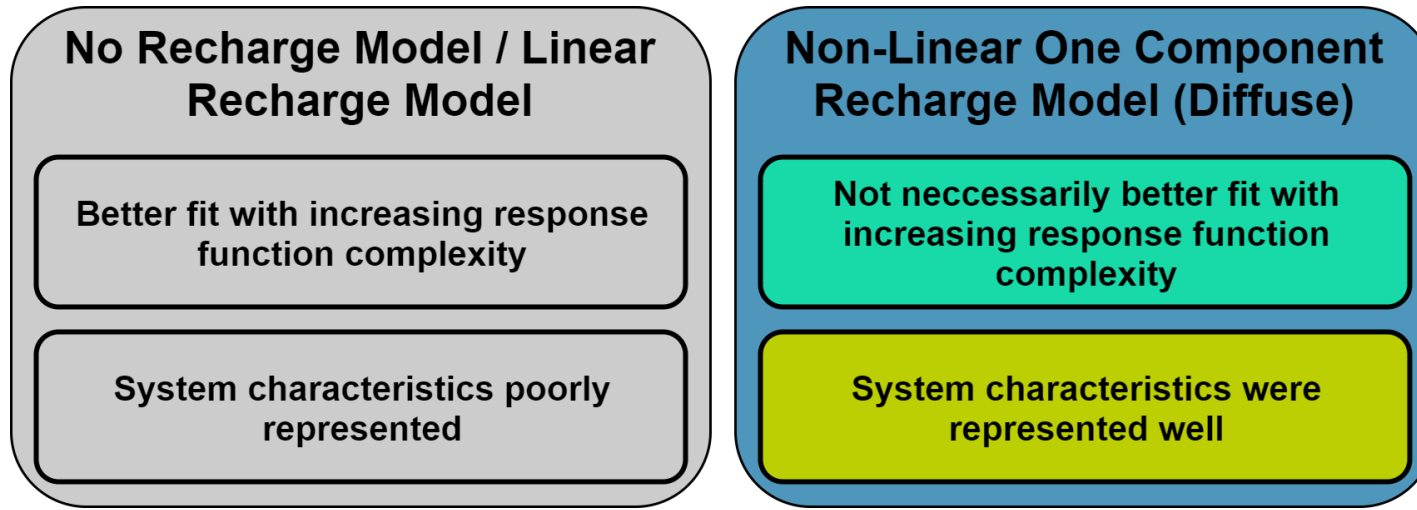
Methodology



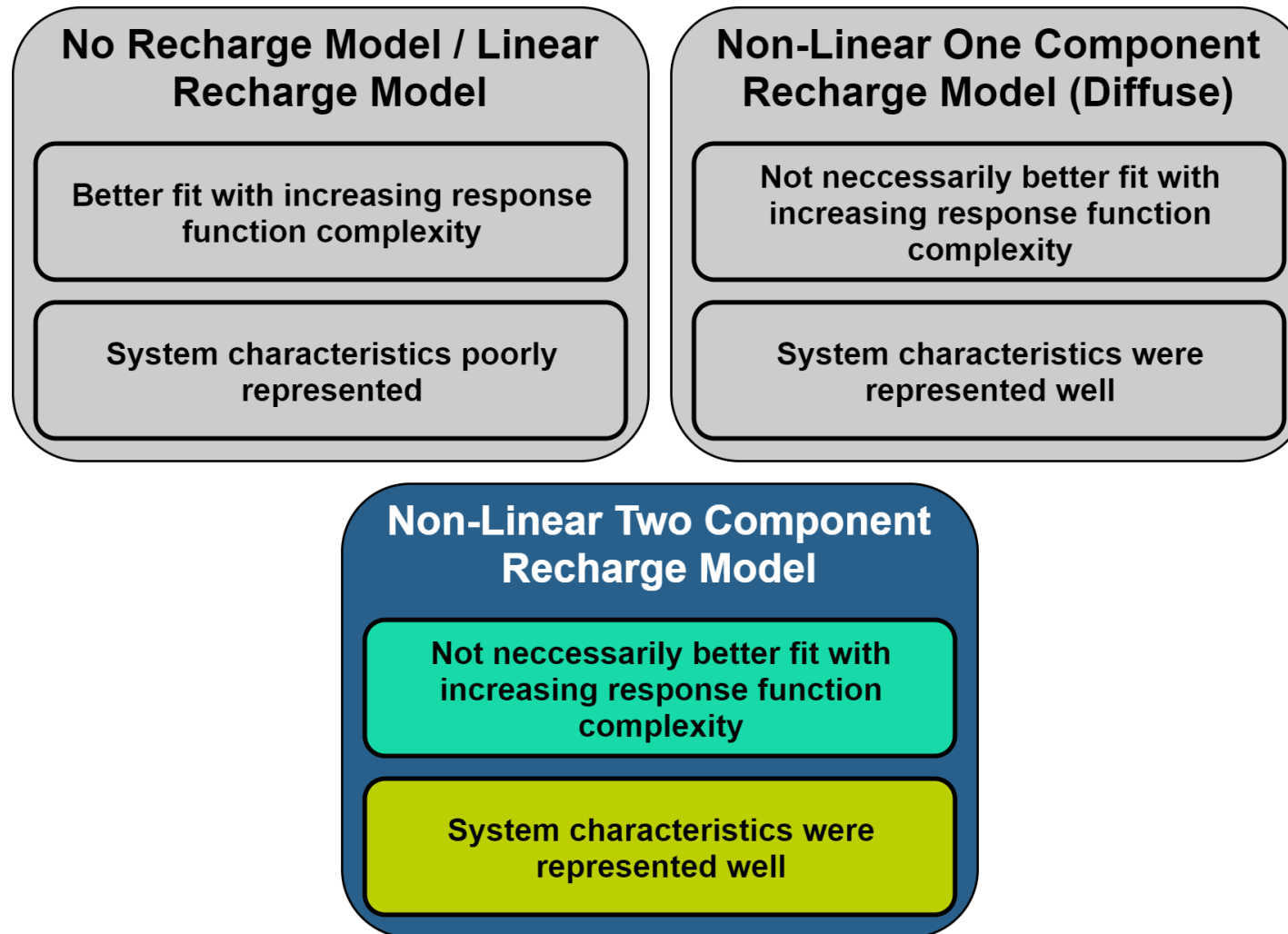
General Results



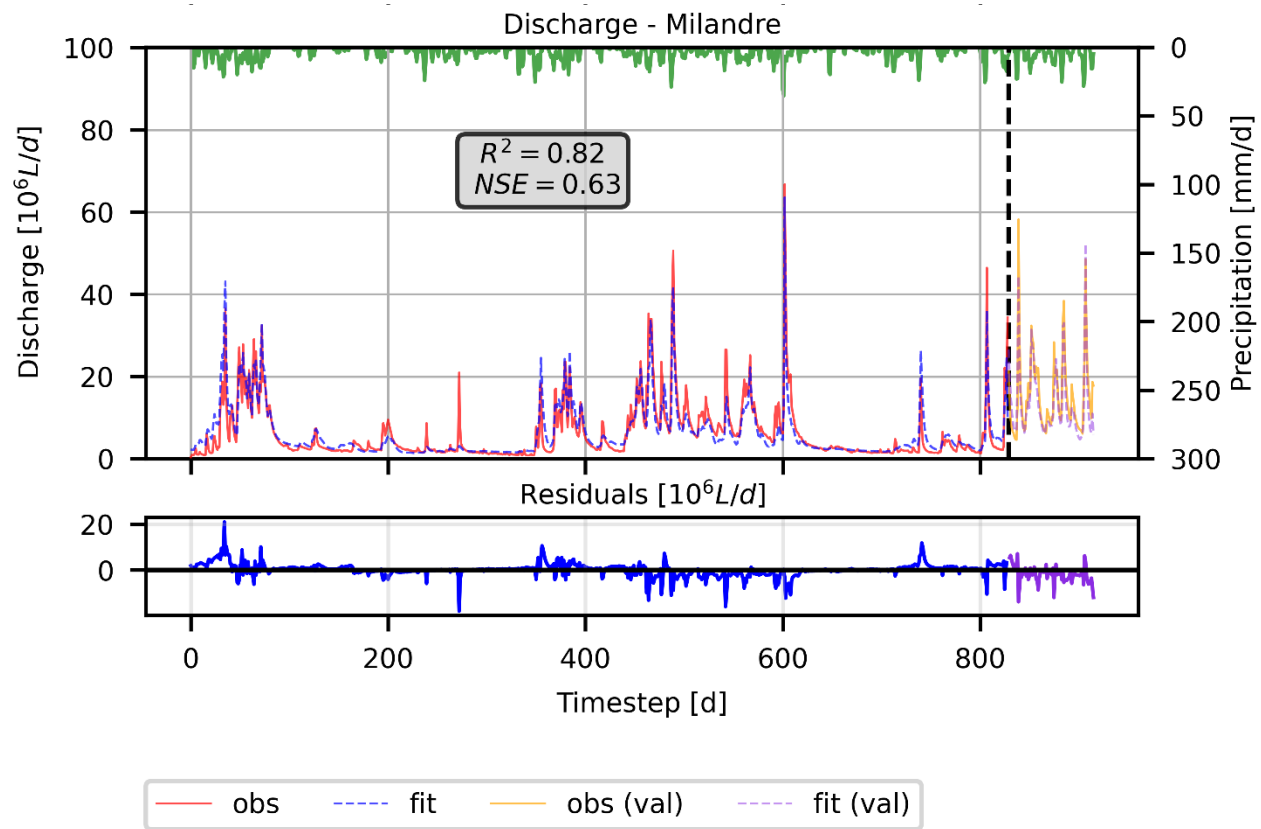
General Results



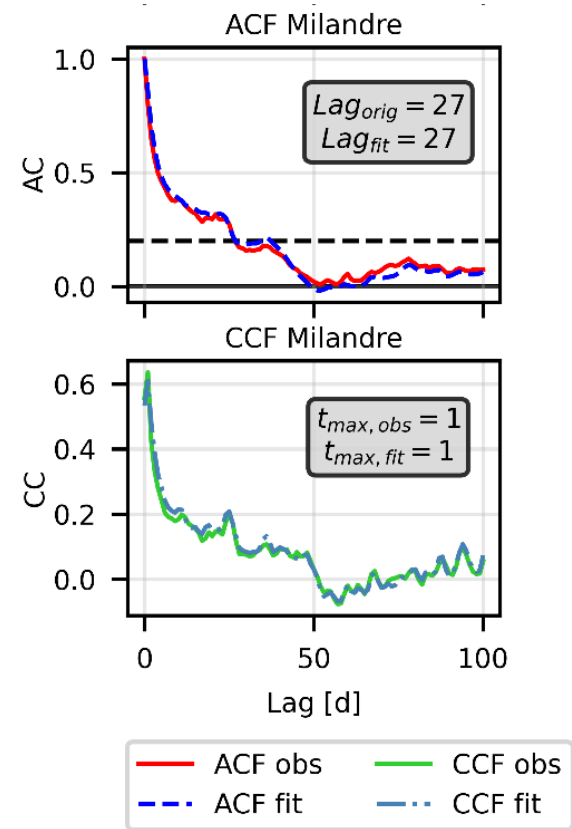
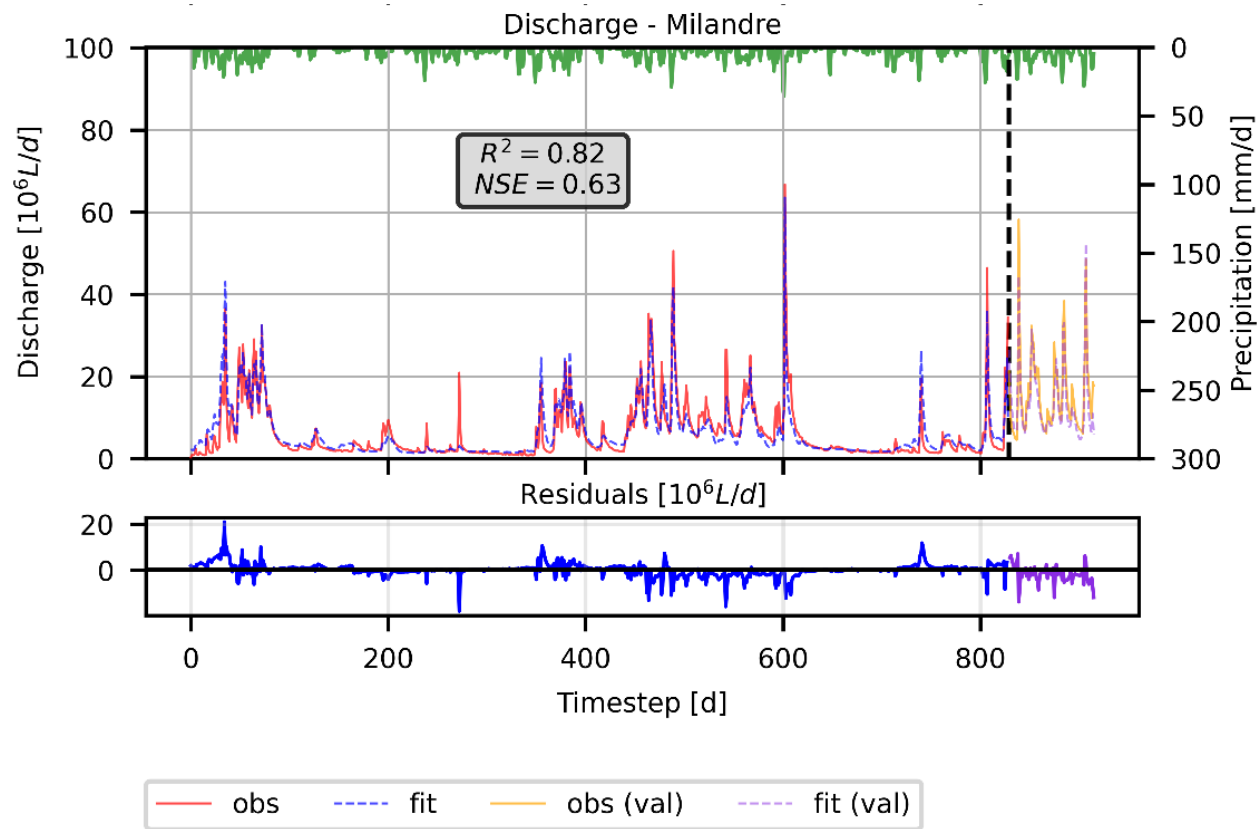
General Results



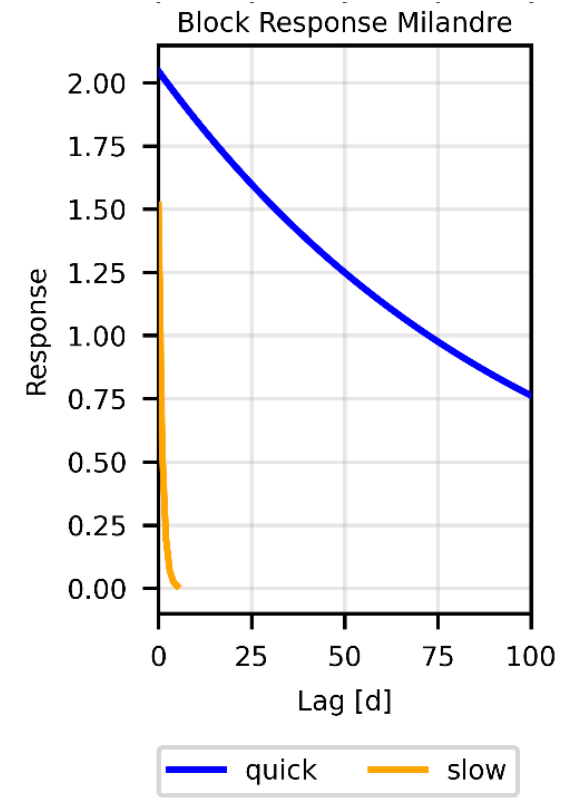
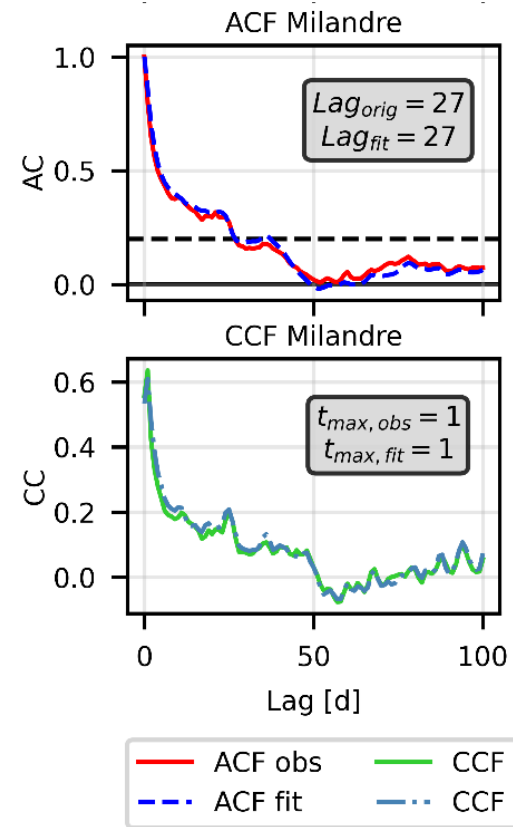
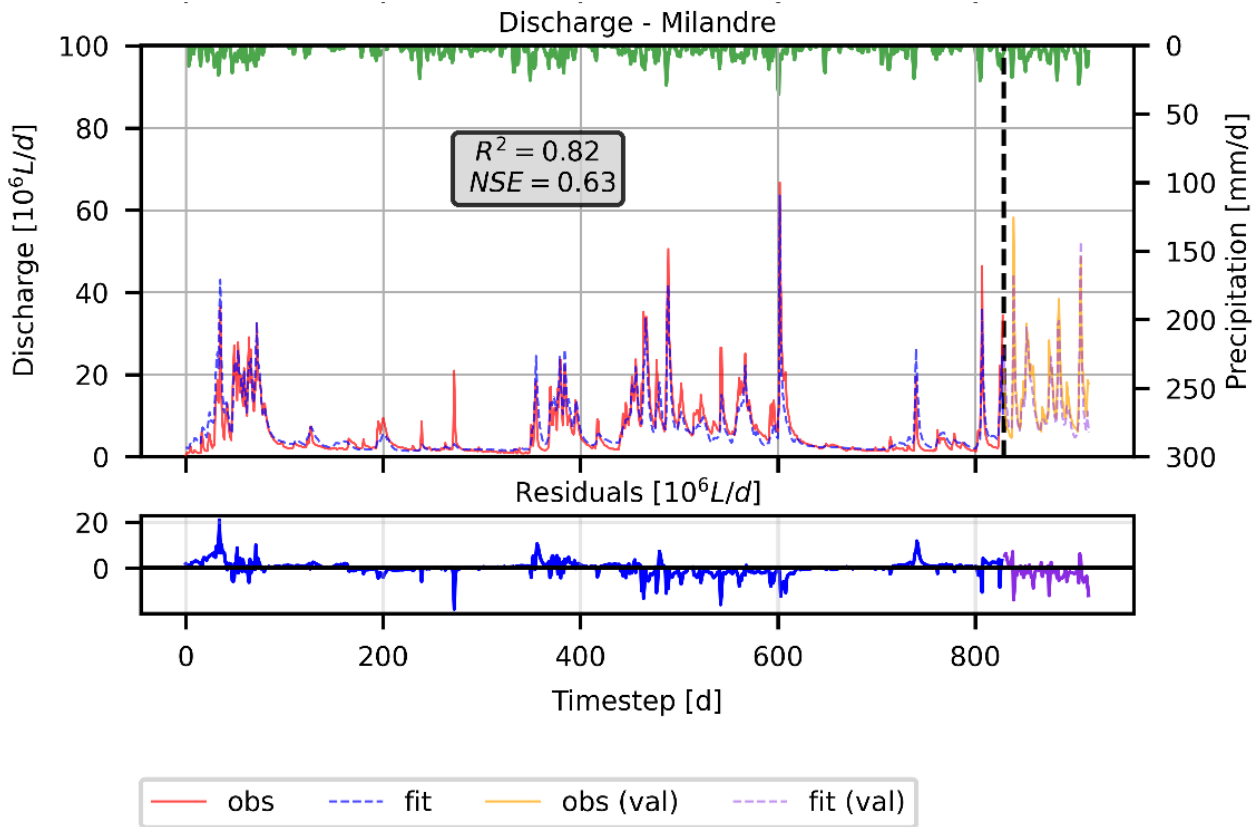
Results - Milandre Karst System



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Results - Milandre Karst System

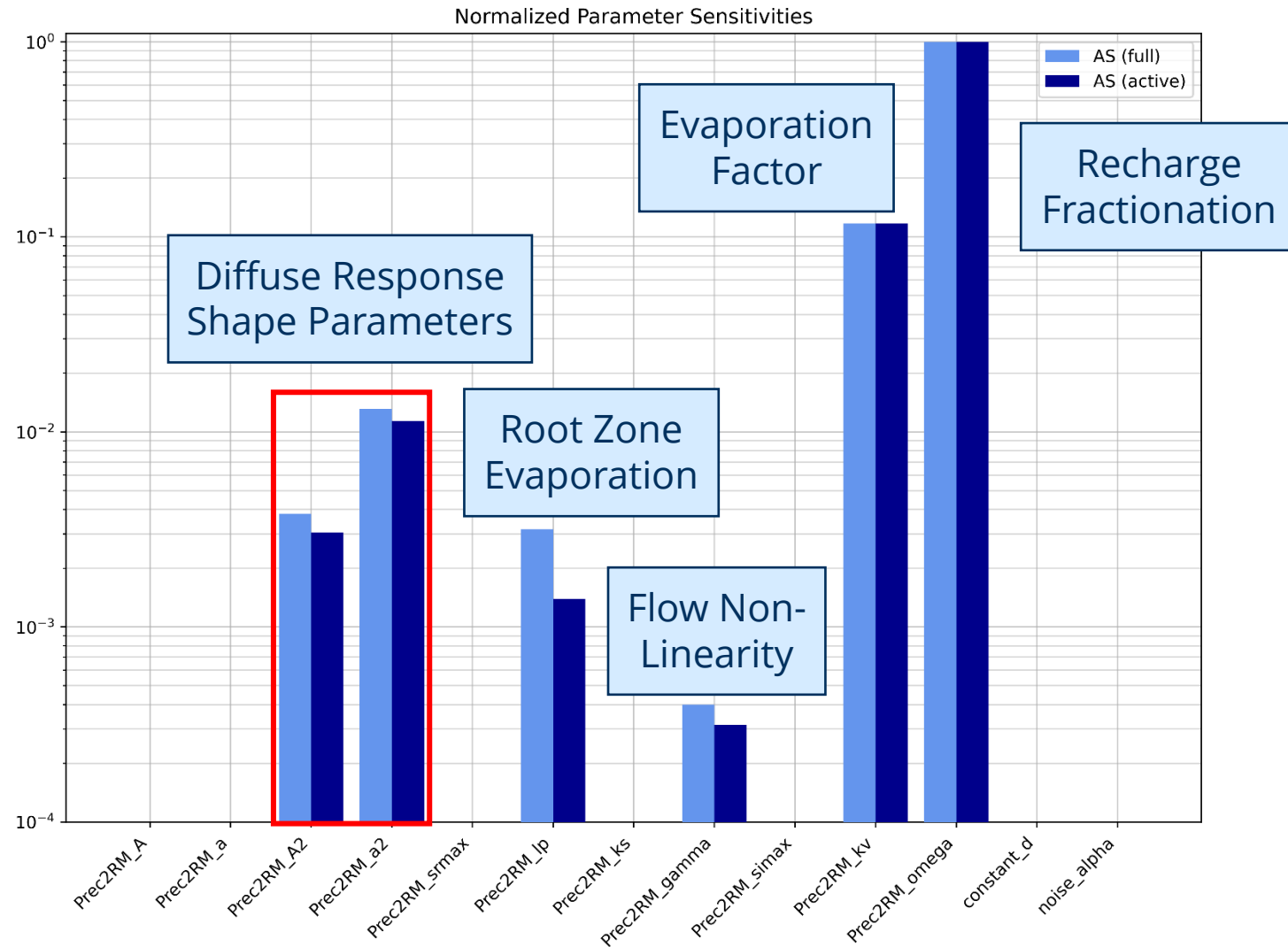


Results – Comparison to Other Modelling Approaches (KMC)

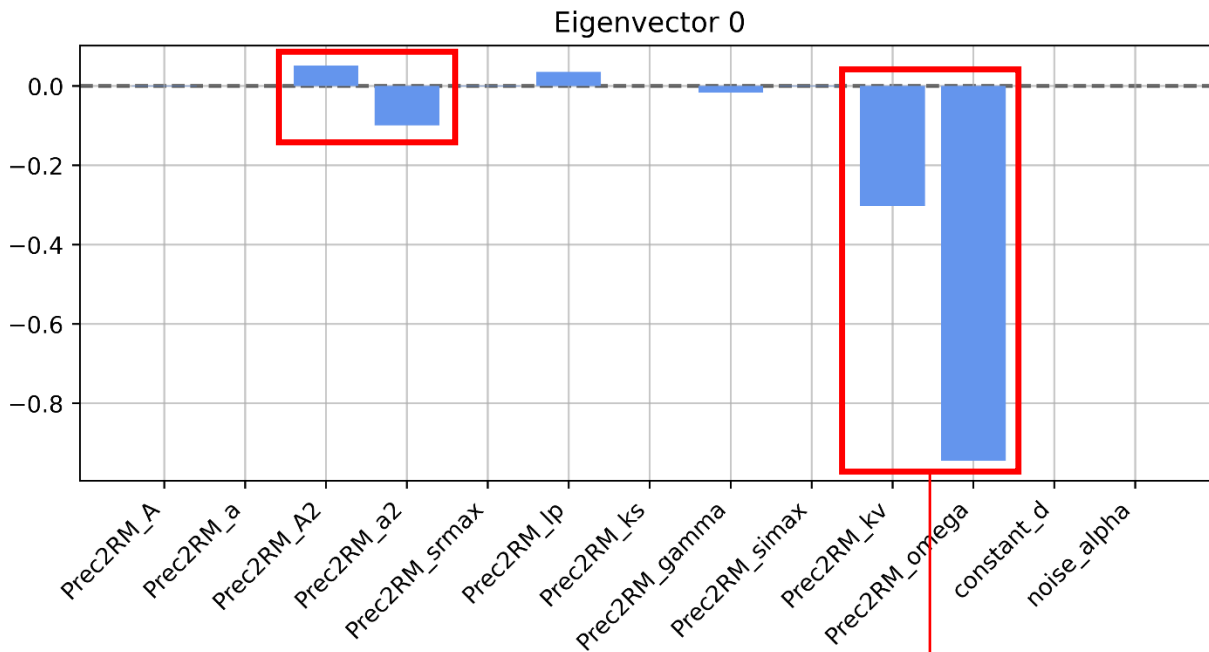
		KGE	VCC	NSE	Effort	Score
BRGM France	Gardenia	0.83	0.854	0.83	1 day	0.84
Uni-Freiburg	Varkarst	0.80	0.85	0.79	1 day	0.82
This Study	TFN Model / Pastas	0.76	0.89	0.72	1 day	0.804
IMT Mines-Alès	ANN / rec_MLP	0.72	0.84	0.61	≈1 day	0.75
SISKA-Switzerland	KRM_1	0.71	0.78	0.63	≈1 day	0.72
IGME Madrid	KarstFLOW	0.71	0.78	0.63	3 days	0.72
TCD Dublin	InfoWorks	0.70	0.82	0.58	2-5 days	0.72
KIT-Karlsruhe	CNN	0.69	0.87	0.40	≈1 day	0.71
KIT-Karlsruhe	NARX	0.68	0.90	0.35	≈1 day	0.70
SNO KARST	KarstMod	0.68	0.72	0.65	1 day	0.69
TU-Dresden	CFP-modified	0.54	0.72	0.25	≈7 days	0.55
TU-Freiberg	RCD-Seasonal	0.47	0.69	0.04	1 day	0.47
Uni-Zürich	CHLEM	0.45	0.71	-0.10	1 day	0.44
KIT-Karlsruhe	LSTM	0.37	0.59	-0.24	1 day	0.34
	Color					
	Rating	Very Good	Good	Fair	Medium	Low

Fit evaluated for a validation period not available for calibration!

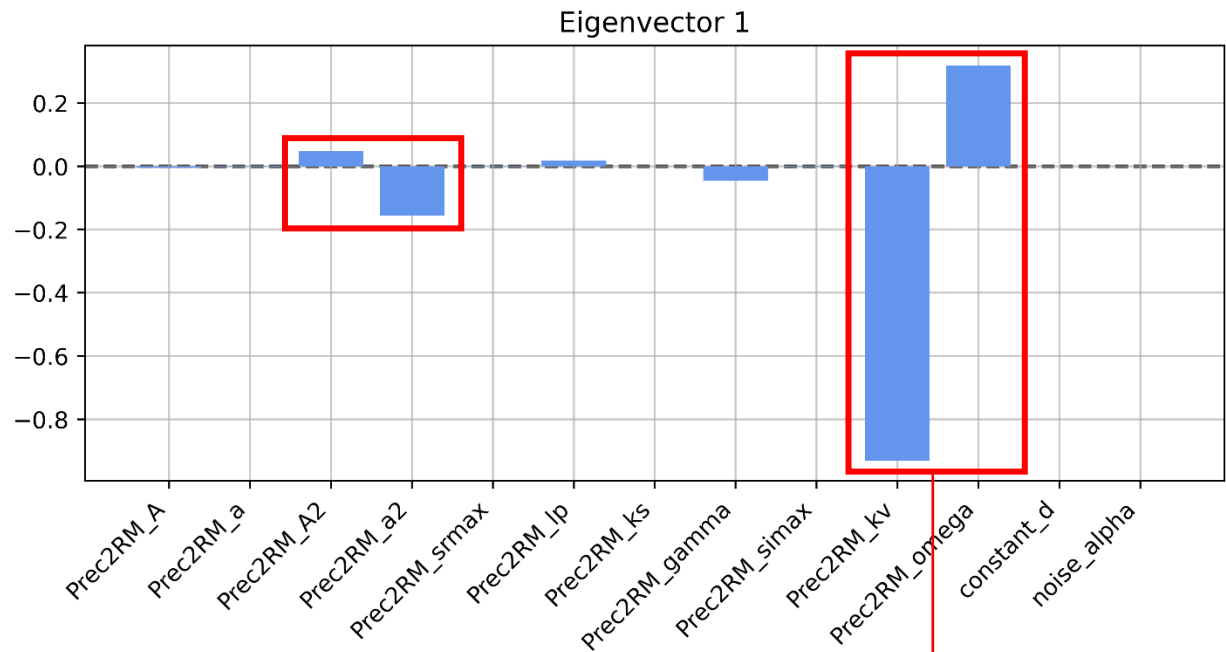
Results – Parameter Sensitivities (Active Subspaces)



Results - Linear Combinations (Active Subspaces)



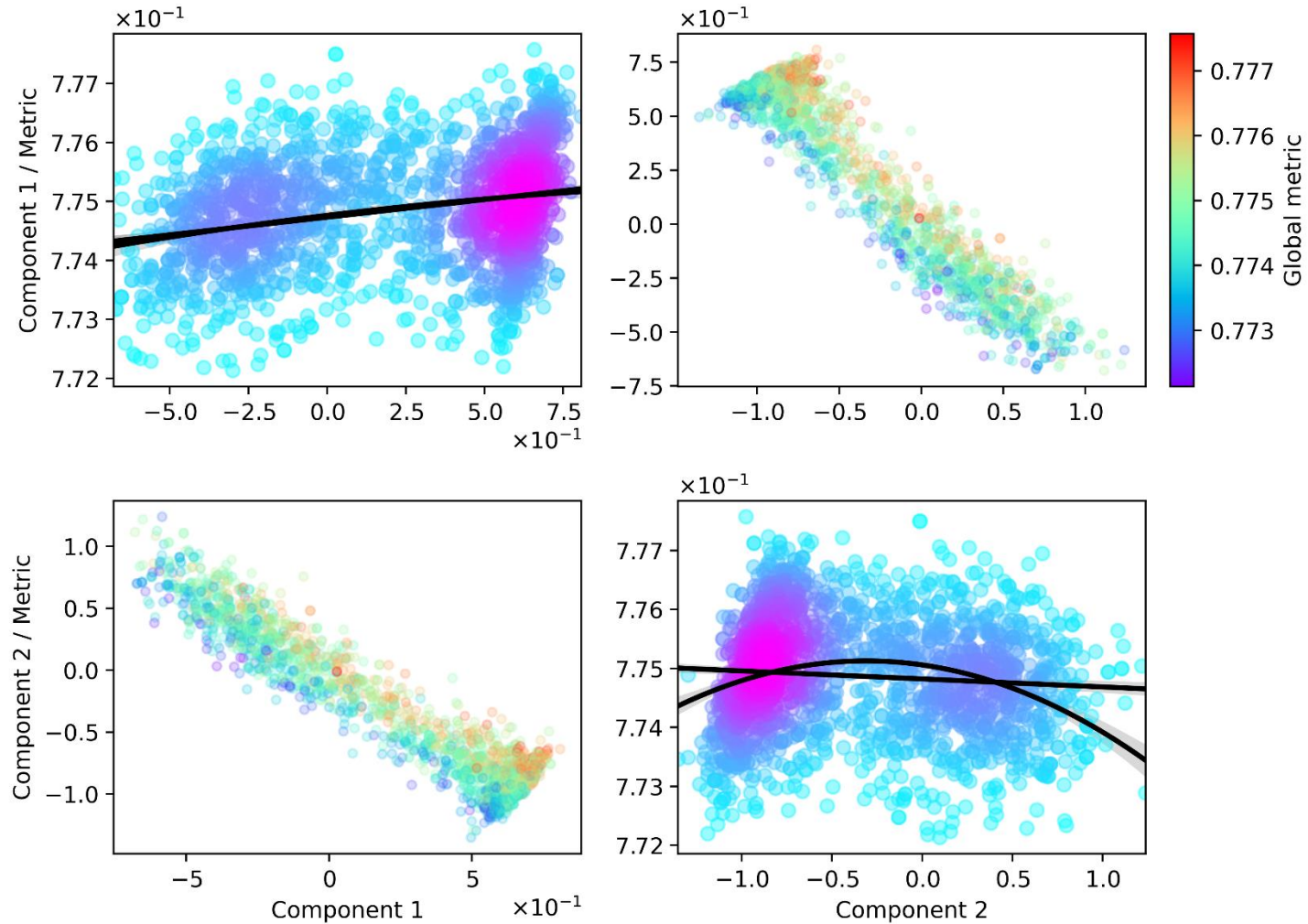
contribution of processes related to recharge fractionation



contribution of processes related to total amount of recharge

Results - Sufficient Summary Plots (Active Subspaces)

Linear Dimension Reduction - 1D and 2D Sufficient Summary Plots



Summary

- **Recharge process** representation is **highly important** and sensitive
- Non-linear **recharge model compensates** for karst system **non-linearity**
- Method is generally **suitable**
- Model **outperformed most other approaches** in the Karst Modelling Challenge

Thank You For Your Attention!

Contact:

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Python

- programming language



Pastas

- open source TFN-model for Python
- available on GitHub

